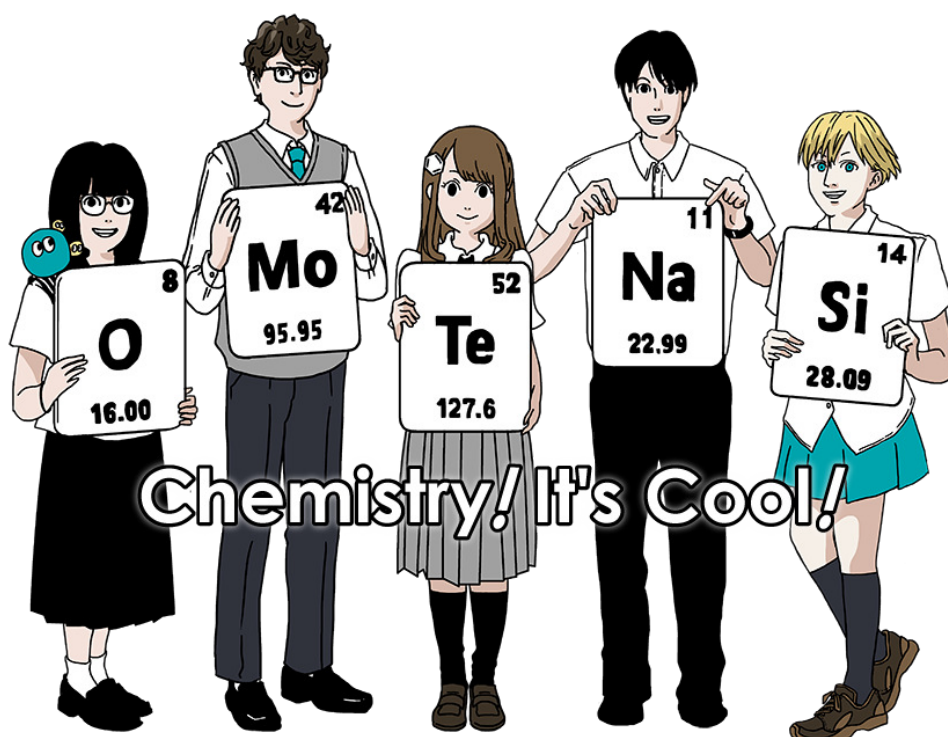




International Chemistry Olympiad 2021 Japan
53rd IChO2021 Japan
25th July – 2nd August, 2021
<https://www.icho2021.org>



Preparatory Problems

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Preface

We are very pleased to introduce the Preparatory Problems for the 53rd International Chemistry Olympiad. These problems cover a wide range of challenging and important topics in modern chemistry. We hope that both students and their mentors will enjoy solving these problems and prepare for the Olympics. The problems include 6 topics of advanced difficulty for the Theoretical part and 3 topics of advanced difficulty for the Practical part, in addition to the subjects normally covered in high school chemistry courses. These topics are explicitly listed under "Fields of Advanced Difficulty" and their applications are shown in the preparatory problems consisting of 31 theoretical problems and 6 practical tasks. The solutions will be emailed to the head mentor of each country by February, 2021 and will be published online in July, 2021. We welcome any comments, corrections and questions about the problems via email to:

preparatory@icho2021.org.

The International Chemistry Olympiad is a great opportunity for young people from all over the world to deepen their understanding of the wonders of chemistry, and inspire each other. At the same time, it is a wonderful opportunity to make friends around the world, and enjoy the history and culture of the host country. COVID-19 is widespread all over the world and the situation is very severe, but we hope that we can meet you in Osaka, Japan in July.

Acknowledgement

We would like to express our deepest gratitude to all the authors for their great efforts in creating both preparatory and competition problems. We would also like to thank the reviewers for their valuable comments and suggestions.

Appendix

The preparatory problems are published to help the students and the mentors prepare for the usual real IChO including the theoretical problems and the practical tasks. However, because of the pandemic of COVID-19, the Organizing Committee finally decided to hold the IChO2021 Japan as the remote IChO to ensure the safety of the participants. Since the practical tasks will not be conducted in the remote IChO2021, the practical tasks in the preparatory problems are out of use for the IChO2021. It is not necessary for the students who want to participate the IChO2021 to study and/or examine the practical tasks and the advanced skills included in the preparatory problems.

Instead of the deletion of the practical tasks from the preparatory problems, however, we moved them to the Appendix part. Even though the practical tasks will not be conducted in IChO2021, the importance of laboratory experiments does not change in the chemistry. We hope to have any opportunity where the practical tasks prepared for the IChO2021 Japan are fully utilized. The practical tasks included in the Appendix part will help such an event.

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Fields of Advanced Difficulty: Theoretical subject

Structure and characterization of inorganic compound:

solid state structure, unit cell, crystal field theory, a concept of hole.

Quantum mechanical behavior of molecules:

molecular vibration, how to read potential energy surface, definition of entropy based on Boltzmann's principle.

Thermodynamics and kinetics:

relationship between electrode potential and Gibbs free energy, adsorption isotherm.

Stereochemistry:

conformation of fused bi- or tri-cyclic alkanes, chirality, stereospecific reaction, stereoselectivity by steric hindrance, axial attack in cyclohexane system.

Number of signals in NMR (^1H , ^{13}C , and heteronuclear NMR) and chemical shift in ^1H NMR.

Reactive intermediate and species:

carbenoid, non-benzenoid aromatics, organic main group-metal compounds, heteroatom–heteroatom bonds.

Notes

Students are not expected to cover the following advanced topics:

Pericyclic reaction other than Diels-Alder reaction, Conservation of orbital symmetry, Polymer chemistry, Phase equilibrium, Catalytic reaction on surface, Normal modes of molecular vibration, Molecular orbital method, Distribution function, Slater rule.

The practical tasks in the Appendix part include the following advanced skills, although the practical examination will not be conducted in the IChO2021 Japan:

Preparation technique:

vacuum filtration following the described procedure.

Purification:

recrystallization and column chromatography following the described procedure.

Physical Constants and Equations

Constants

Speed of light in vacuum, $c = 2.99792458 \times 10^8 \text{ m s}^{-1}$

Planck constant, $h = 6.62607015 \times 10^{-34} \text{ J s}$

Elementary charge, $e = 1.602176634 \times 10^{-19} \text{ C}$

Electron mass, $m_e = 9.10938370 \times 10^{-31} \text{ kg}$

Electric constant (permittivity of vacuum), $\epsilon_0 = 8.85418781 \times 10^{-12} \text{ F m}^{-1}$

Avogadro constant, $N_A = 6.02214076 \times 10^{23} \text{ mol}^{-1}$

Boltzmann constant, $k_B = 1.380649 \times 10^{-23} \text{ J K}^{-1}$

Faraday constant, $F = N_A \times e = 9.64853321233100184 \times 10^4 \text{ C mol}^{-1}$

Gas constant, $R = N_A \times k_B = 8.31446261815324 \text{ J K}^{-1} \text{ mol}^{-1}$
 $= 8.2057366081 \times 10^{-2} \text{ L atm K}^{-1} \text{ mol}^{-1}$

Unified atomic mass unit, $u = 1 \text{ Da} = 1.66053907 \times 10^{-27} \text{ kg}$

Standard pressure, $p = 1 \text{ bar} = 10^5 \text{ Pa}$

Atmospheric pressure, $p_{\text{atm}} = 1.01325 \times 10^5 \text{ Pa}$

Zero degree Celsius, $0^\circ\text{C} = 273.15 \text{ K}$

Ångström, $1 \text{ Å} = 10^{-10} \text{ m}$

Picometer, $1 \text{ pm} = 10^{-12} \text{ m}$

Electronvolt, $1 \text{ eV} = 1.602176634 \times 10^{-19} \text{ J}$

Part-per-million, $1 \text{ ppm} = 10^{-6}$

Part-per-billion, $1 \text{ ppb} = 10^{-9}$

Part-per-trillion, $1 \text{ ppt} = 10^{-12}$

pi, $\pi = 3.141592653589793$

The base of the natural logarithm (Euler's number), $e = 2.718281828459045$

Equations

The ideal gas law:

$$PV = nRT$$

, where P is the pressure, V is the volume, n is the amount of substance, T is the absolute temperature of ideal gas.

The first law of thermodynamics:

$$\Delta U = q + w$$

, where ΔU is the change in the internal energy, q is the heat supplied, w is the work done.

Enthalpy H :

$$H = U + PV$$

Entropy based on Boltzmann's principle S :

$$S = k_B \ln W$$

, where W is the number of microstates.

The change of entropy ΔS :

$$\Delta S = \frac{q_{rev}}{T}$$

, where q_{rev} is the heat for the reversible process.

Gibbs free energy G :

$$G = H - TS$$

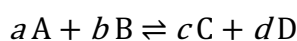
$$\Delta_r G^0 = -RT \ln K = -zFE^0$$

, where K is the equilibrium constant, z is the number of electrons, E^0 is the standard electrode potential.

Reaction quotient Q :

$$\Delta_r G = \Delta_r G^0 + RT \ln Q$$

For a reaction



$$Q = \frac{[C]^c [D]^d}{[A]^a [B]^b}$$

, where $[A]$ is the concentration of A.

Heat change Δq :

$$\Delta q = n c_m \Delta T$$

, where c_m is the temperature-independent molar heat capacity.

Nernst equation for redox reaction:

$$E = E^0 + \frac{RT}{zF} \ln \left(\frac{C_{ox}}{C_{red}} \right)$$

, where C_{ox} is the concentration of oxidized substance, C_{red} is the concentration of reduced substance.

Arrhenius equation:

$$k = A \exp \left(-\frac{E_a}{RT} \right)$$

, where k is the rate constant, A is the pre-exponential factor, E_a is the activation energy.

$$\exp(x) = e^x$$

Lambert–Beer equation:

$$A = \varepsilon lc$$

, where A is the absorbance, ε is the molar absorption coefficient, l is the optical path length, c is the concentration of the solution.

Henderson–Hasselbalch equation:

For an equilibrium



, where equilibrium constant is K_a ,

$$\text{pH} = \text{p}K_a + \log \left(\frac{[\text{A}^-]}{[\text{HA}]}\right)$$

Energy of a photon:

$$E = h\nu = h \frac{c}{\lambda}$$

, where ν is the frequency, λ is the wavelength of the light.

The sum of a geometric series:

When $x \neq 1$,

$$1 + x + x^2 + \dots + x^n = \sum_{i=0}^n x^i = \frac{1 - x^{n+1}}{1 - x}$$

Approximation equation that can be used to solve problems:

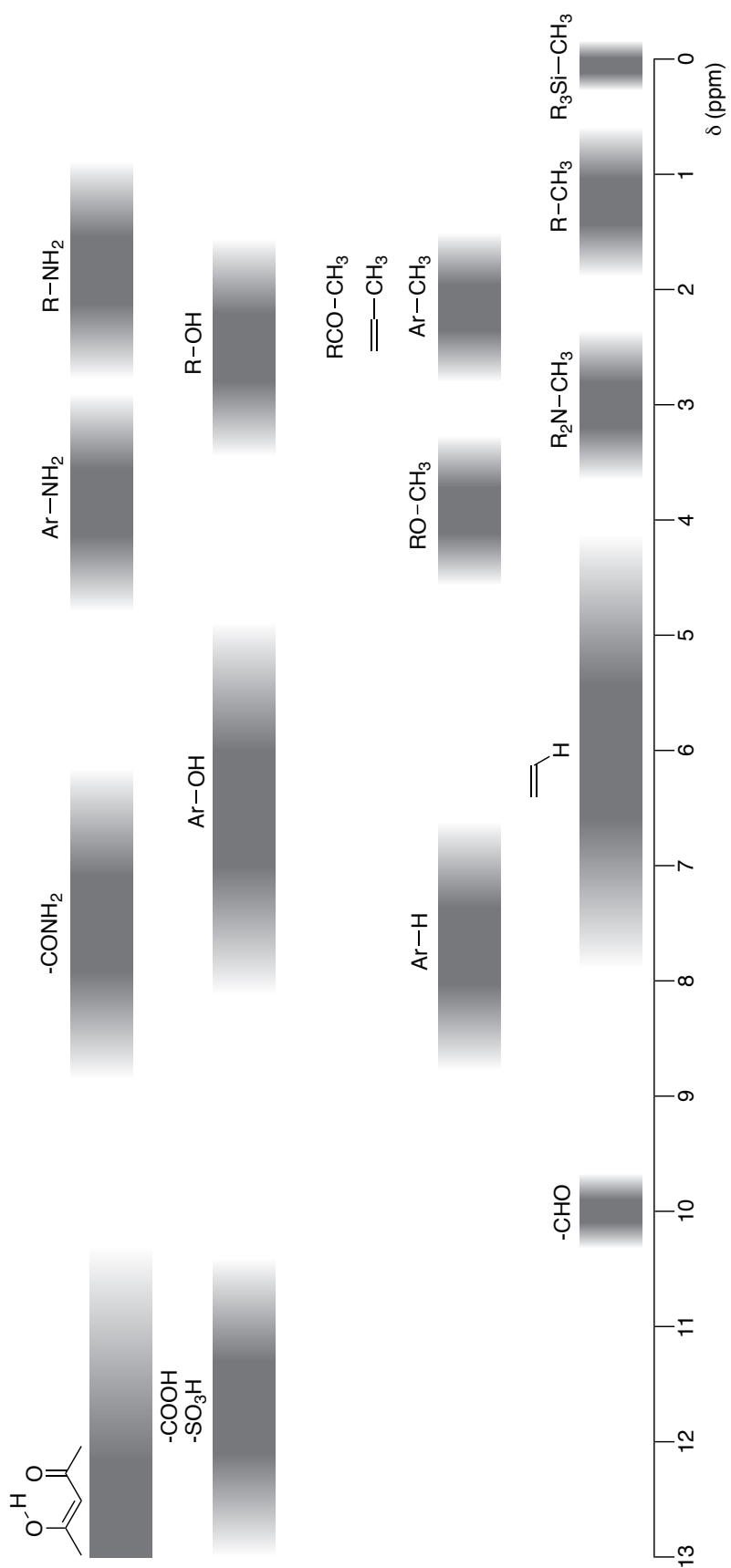
When $x \ll 1$,

$$\frac{1}{1 - x} \sim 1 + x$$

Periodic table

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
1																	
H Hydrogen 1.00798																	
3	4																
Li Lithium 6.968	Be Beryllium 9.012183																
11	12																
Na Sodium 22.989769	Mg Magnesium 24.306																
19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36
K Potassium 39.0983	Ca Calcium 40.078	Sc Scandium 44.955908	Ti Titanium 47.867	V Vanadium 50.9415	Cr Chromium 51.9961	Mn Manganese 54.938044	Fe Iron 55.845	Co Cobalt 58.933194	Ni Nickel 58.6934	Cu Copper 63.546	Zn Zinc 65.38	Ga Gallium 69.723	Ge Germanium 72.630	As Arsenic 74.921595	Se Selenium 78.971	Br Bromine 79.904	Kr Krypton 83.798
37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54
Rb Rubidium 85.4678	Sr Strontium 87.62	Y Yttrium 88.90584	Zr Zirconium 91.224	Nb Niobium 92.90637	Mo Molybdenum 95.95	Tc Technetium [99]	Ru Ruthenium 101.07	Rh Rhodium 102.90550	Pd Palladium 106.42	Ag Silver 107.8682	Cd Cadmium 112.414	In Indium 114.818	Sn Tin 118.710	Sb Antimony 121.760	Te Tellurium 127.60	I Iodine 126.90447	Xe Xenon 131.293
55	56	57-71 La-Lu Lanthanoids	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86
Cs Caesium 132.905452	Ba Barium 137.327	La-Lu Lanthanoids	Hf Hafnium 178.49	Ta Tantalum 180.94788	W Tungsten 183.84	Re Rhenium 186.207	Os Osmium 190.23	Ir Iridium 192.217	Pt Platinum 195.084	Au Gold 196.966569	Hg Mercury 200.592	Tl Thallium 204.384	Pb Lead 207.2	Bi Bismuth 208.98040	Po Polonium [210]	At Astatine [210]	Rn Radon [222]
87	88	89-103 Ac-Lr Actinoids	104	105	106	107	108	109	110	111	112	113	114	115	116	117	118
Fr Francium [223]	Ra Radium [226]	Ac-Lr Actinoids	Rf Rutherfordium [267]	Db Dubnium [268]	Sg Seaborgium [271]	Bh Bohrium [272]	Hs Hassium [277]	Mt Meitnerium [276]	Ds Darmstadtium [281]	Rg Roentgenium [280]	Cn Copernicium [285]	Nh Nihonium [278]	Fl Flerovium [289]	Mc Moscovium [289]	Lv Livermorium [293]	Ts Tennessine [293]	Og Oganesson [294]
57-71 La-Lu Lanthanoids	58	59	60	61	62	63	64	65	66	67	68	69	70	71			
57-71 La-Lu Lanthanoids	Ce Cerium 140.116	Pr Praseodymium 140.90766	Nd Neodymium 144.242	Pm Promethium [145]	Sm Samarium 150.36	Eu Europium 151.964	Gd Gadolinium 157.25	Tb Terbium 158.92535	Dy Dysprosium 162.500	Ho Holmium 164.93033	Er Erbium 167.259	Tm Thulium 168.93422	Yb Ytterbium 173.045	Lu Lutetium 174.9668			
	90	91	92	93	94	95	96	97	98	99	100	101	102	103			
89-103 Ac-Lr Actinoids	Th Thorium 232.0377	Pa Protactinium 231.03568	U Uranium 238.02891	Np Neptunium [237]	Pu Plutonium [239]	Am Americium [243]	Cm Curium [247]	Bk Berkelium [247]	Cf Californium [252]	Es Einsteinium [252]	Fm Fermium [257]	Md Mendelevium [258]	No Nobelium [259]	Lr Lawrencium [262]			

¹H NMR Chemical Shifts



$\Delta\delta$ for one alkyl group-substitution: *ca.* +0.4 ppm

Safety

Participants in the Olympiad must be prepared to work in a chemical laboratory and be aware of all relevant rules and safety procedures. The organizers will strictly enforce the safety rules given in Appendix A of the IChO Regulations during the Olympiad.

The Preparatory Problems are designed to be carried out in properly equipped chemical laboratories under competent supervision **only**. We did not include specific and detailed safety and disposal instructions as regulations are different in each country. Mentors must carefully adapt the problems accordingly.

The GHS hazard statements (H-phrases) associated with the materials used are indicated in the problems. Their meanings are as follows:

Physical Hazards

- H225 Highly flammable liquid and vapor.
- H226 Flammable liquid and vapor.
- H227 Flammable liquid.
- H228 Flammable solid.
- H271 May cause fire or explosion; strong oxidizer.
- H272 May intensify fire; oxidizer.
- H290 May be corrosive to metals.

Health Hazards

- H301 Toxic if swallowed.
- H302 Harmful if swallowed.
- H303 Maybe harmful if swallowed.
- H304 May be fatal if swallowed and enters airways.
- H305 May be harmful if swallowed and enters airways.
- H311 Toxic in contact with skin.
- H312 Harmful in contact with skin.
- H313 May be harmful in contact with skin.
- H314 Causes severe skin burns and eye damage.
- H315 Causes skin irritation.
- H316 Causes mild skin irritation.
- H317 May cause an allergic skin reaction.
- H318 Causes serious eye damage.
- H319 Causes serious eye irritation.
- H320 Causes eye irritation.
- H331 Toxic if inhaled.
- H332 Harmful if inhaled.
- H333 May be harmful if inhaled.
- H334 May cause allergy or asthma symptoms or breathing difficulties if inhaled.
- H335 May cause respiratory irritation.
- H336 May cause drowsiness or dizziness.
- H351 Suspected of causing cancer.
- H361 Suspected of damaging fertility or the unborn child.
- H361d Suspected of damaging the unborn child.
- H361f Suspected of damaging fertility.
- H362 May cause harm to breast-fed children.
- H370 Causes damage to organs.

- H371 May cause damage to organs.
- H372 Causes damage to organs through prolonged or repeated exposure.
- H373 May cause damage to organs through prolonged or repeated exposure.

Environmental Hazards

- H400 Very toxic to aquatic life.
- H401 Toxic to aquatic life.
- H402 Harmful to aquatic life.
- H410 Very toxic to aquatic life with long lasting effects.
- H411 Toxic to aquatic life with long lasting effects.
- H412 Harmful to aquatic life with long lasting effects.
- H413 May cause long-lasting harmful effects to aquatic life.

Chemicals or substrates with GHS hazard statement H300, H310, H330, H340, H350, and H360 are not allowed to be used in IChO and according activities.

Problem 1. Revision of SI unit

The definitions of the SI base units were fully revised on May 20, 2019. Let us examine some of the definitions related to chemistry.

Part 1.

Before the new definition, the Avogadro number, N_A , was defined as ‘the number of atoms contained in 0.012 kg of the carbon isotope ^{12}C ’. In other words, a collection of N_A atoms of ^{12}C has a mass of 0.012 kg.

To determine N_A experimentally, 0.012 kg of ^{12}C must be accurately measured, which requires a weight ‘standard’. Traditionally, the kilogram prototype has served this purpose.

In practice, an international research consortium consisting of eight institutes including a Japanese one made a single crystal of silicon (Si) composed solely of ^{28}Si , from which a true sphere was cut for the determination of N_A . The single crystal of Si has a diamond-type crystal system with the cubic unit cell as shown in Figure 1.

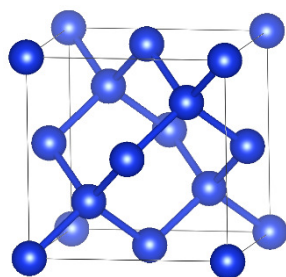


Figure 1. Single crystal of Si.

1-1. **Determine** the number of atoms of Si, n , involved in the unit cell.

Let us consider the density of the true sphere of the single crystal of Si. The length of each side of the unit cell is a [m]. The atomic mass of ^{28}Si is $m = 28.09 u$, where u is defined in the former fashion as:

$$u = \frac{1 \times 10^{-3}}{N_A} \text{ [kg]}$$

which has the same meaning as the atomic mass unit Dalton (Da).

1-2. **Write** an equation for the density, d [kg m^{-3}], using n , m , and a .

The radius, r , of the true sphere of Si was measured to be $r = 4.69 \text{ nm}$. Using the kilogram prototype, the mass of the sphere was determined to be $w = 1.00 \text{ kg}$. The lattice length of the unit cell was determined to be $a = 0.357 \text{ nm}$ by an X-ray diffraction analysis.

1-3. **Calculate** the Avogadro number, N_A , using the measured parameters with three significant figures.

Part 2.

In the new definition, N_A is defined with a finite number of digits (Table 1). In this situation, a collection of N_A atoms of ^{12}C does not exactly have a mass of 0.012 kg.

The new definition enables calculating mass using the equation found in Q1-3. In fact, mass can now be determined without using the kilogram prototype if the volume is accurately measured. The kilogram prototype itself is not easy to access, and replicas are also not easily available worldwide. In addition, the aging of the prototype cannot be ignored. Determining mass without using the prototype has therefore a significant merit. As a result, seven fundamentally important constants have been determined using the newest measurement data based on the consensus of multiple research institutes.

Three of these constants are presented in **Table 1**.

Table 1. Three re-defined constants

Constant	Notation	Newly defined value	Unit
Avogadro constant	N_A	$6.02214076 \times 10^{23}$	mol^{-1}
Planck constant	h	$6.62607015 \times 10^{-34}$	J s
Velocity of light	c	2.99792458×10^8	m s^{-1}

Here, the product of the Avogadro and Planck constants is theoretically also a constant.

2-1. Based on these facts, **select** all the appropriate options for the determination of mass.

To determine mass:

☐ N_A alone is sufficient ☐ both N_A and h are required ☐ h alone is sufficient

Let us define mass by considering the units of the constants. The Avogadro constant has the unit mol^{-1} . Since this unit has no apparent unit of mass, discussion of mass based on this constant would be difficult. On the other hand, the unit of the Planck constant, J s, can be rewritten as $\text{kg m}^2 \text{s}^{-1}$, which seems more suitable for obtaining a definition of mass. To use this approach, we must understand the definitions of 1 s of time and 1 m of distance.

In the new definitions of the SI units, 1 s is based on the experimental observation that the energy difference of the hyperfine energy splitting of ^{133}Cs in a magnetic field (details are omitted here) is expressed in units of Hz as:

$$\Delta\nu_{\text{Cs}} = 9192631770 \text{ Hz}$$

This highly accurate piece of information can be rewritten using the definition of $\text{Hz} = \text{s}^{-1}$ as:

$$\Delta\nu_{\text{Cs}} = 9192631770 (1 \text{ s})^{-1}$$

We then obtain the following definition:

$$1 \text{ s} = \frac{9192631770}{\Delta\nu_{\text{Cs}}}$$

This means that 1 s is 9192631770 times longer than the time of the $\Delta\nu_{\text{Cs}}$ transition, which is the new definition of 1 s.

In a similar manner, 1 m of distance is defined by using the velocity of light, $c = 299792458 \text{ m s}^{-1}$. In other words, 1 m is defined as the distance that light travels in 1 s divided by 299792458. The definition of 1 s can be substituted into this definition of 1 m to afford:

$$1 \text{ m} = \frac{9192631770}{299792458} \frac{c}{\Delta\nu_{\text{Cs}}} = 30.663319 \frac{c}{\Delta\nu_{\text{Cs}}}$$

, which is the new definition of 1 m.

2-2. **Write** a new definition for 1 kg of mass using these new definitions with eight significant digits.

On the other hand, mass can also be discussed in terms of energy. The mass of a particle at rest, m , is equivalent to the energy having a frequency of ν (*i.e.*, the rest energy):

$$h\nu = mc^2$$

In this definition, a photon can also be recognized to have mass.

2-3. **Calculate** the apparent mass of a photon, m [kg], emitted from a laser pointer with a wavelength of 635 nm.

Problem 2. Does water boil or evaporate?

When an ideal gas is isothermally expanded from pressure p [bar] to p' [bar] ($p > p'$), the entropy change ΔS of the gas is

$$\Delta S \text{ [J K}^{-1} \text{ mol}^{-1}] = -R \ln \left(\frac{p'}{p} \right) \quad (1).$$

The enthalpy change when liquid water evaporates to water vapor at p_0 [bar] is ΔH_v° [J mol⁻¹], and the entropy change is ΔS_v° [J K⁻¹ mol⁻¹]. Let us suppose these values do not depend on temperature, and the gas is an ideal gas. In this case, when liquid water evaporates to water vapor at p_1 [bar], the enthalpy change is ΔH_v [J mol⁻¹] = ΔH_v° , and the entropy change is ΔS_v [J K⁻¹ mol⁻¹] = (a).

1. **Write** the appropriate formula for blank (a).

For the following questions, assume that $\Delta H_v^\circ = 4.070 \times 10^4$ J mol⁻¹ and that, $\Delta S_v^\circ = 1.091 \times 10^2$ J K⁻¹ mol⁻¹ at $p_0 = 1$ bar.

2. **Calculate** the boiling point of water at 1 bar.
3. **Calculate** the saturated vapor pressure of water at 87 °C.
4. **Calculate** the Gibbs energy change per mole when water evaporates at 87 °C at a humidity of 50%. The humidity represents the ratio of the actual partial pressure of water vapor relative to the saturated vapor pressure of water.

A container with a piston like that shown in Figure 1 is filled with 0.10 mol of Ar and 1.00 mol of water (liquid and vapor). The temperature of the entire container is 87 °C and the total pressure is 1 bar. It is assumed that the volume of the liquid or cup is negligible with respect to that of the gas, and that the temperature of water and Ar is always maintained at 87 °C. In this initial situation, the partial pressure of Ar is (b) bar, the partial pressure of water vapor is (c) bar, the volume of the gas is (d) L, and the number of moles of liquid water is (e) mol.

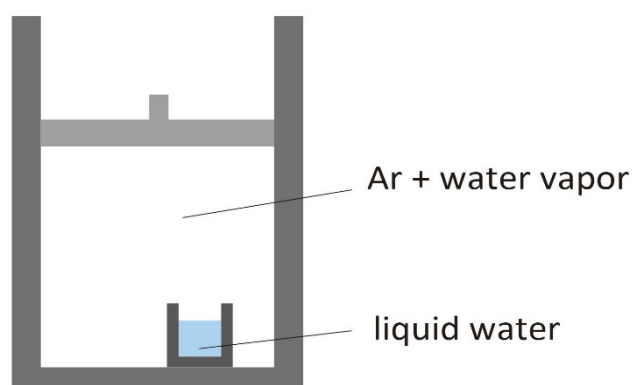


Figure 1. A container with a piston containing Ar gas, water vapor and liquid water in a cup.

The piston is then pulled back quickly to fix the gas volume to 15.8 L. At the moment when the piston is pulled, the partial pressure of Ar decreases to (f) bar and the partial pressure of water vapor decreases to (g) bar. In this situation, the water will boil, because the total pressure of the gas is lower than the saturated vapor pressure of water at 87 °C. The partial pressure of water vapor increases due to the boiling until the boiling eventually stops. When the boiling stops, the number of moles of

liquid water is mol. After that, evaporation proceeds until equilibrium is reached. At equilibrium, the number of moles of liquid water is mol.

5. **Calculate** the appropriate numerical values for blanks (b) - (i).

Problem 3. Molecules meet water and metals

I. Dissolution of gases in water

For gases that are slightly soluble in water, there is a proportional relationship between the partial pressure, P , and the mole fraction, x , of the gas molecules dissolved in water (Henry's law):

$$P = k_H x$$

Here, k_H is the Henry coefficient. The Henry coefficients of nitrogen, oxygen, and argon at 25 °C for water are 8.57×10^4 , 4.42×10^4 , and 4.02×10^4 bar, respectively. In the following questions, the compression of the water by the pressurized gas can be ignored.

Part 1. Decompression sickness

When a diver spends prolonged time at high depths, the high water pressure causes nitrogen molecules in the body to dissolve in the blood. If the diver rises too quickly to the surface, this dissolved nitrogen will form bubbles that damage the blood vessels and tissues. With the decompression sickness phenomenon in mind, answer the following questions regarding the dissolution of gas in water in a closed container.

- 1-1. **Calculate** the pressure [bar] underwater at a depth of 20.0 m. Here, the density of water is 1.00 g cm^{-3} , the specific gravity of seawater is 1.02, the gravity acting on a mass of 1 kg is 9.81 N, and the atmospheric pressure is 1.01 bar.
- 1-2. At a temperature of 25 °C, 5.00 L of water, which is approximately equivalent to the blood volume of an adult, is added to a container with a piston, and the container is filled with nitrogen. Then, the pressure of the nitrogen is adjusted to the value calculated in Q1-1 by pushing down the piston, and sufficient time is allowed to pass for the gas–liquid equilibrium to be established. **Calculate** the amount of nitrogen [mol] dissolved in water.
- 1-3. The piston is then moved to lower the pressure to 0.800 bar, which is approximately equal to the partial pressure of nitrogen in the atmosphere, and sufficient time is allowed for the vapor–liquid equilibrium to be established. **Calculate** the volume [L] of nitrogen at 25 °C that is released into the gas phase from the nitrogen dissolved in water in Q1-2.

Part 2. Sparkling beverages

The dissolution of high-pressure gas in water in a closed container is also relevant to sparkling beverages.

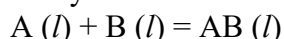
- 2-1. A container ($V = 570 \text{ mL}$) is filled with water ($V_l = 500 \text{ mL}$) and pressurized with CO_2 gas ($P_0 = 50 \text{ atm}$), before it is allowed to stand at 10 °C until the vapor–liquid equilibrium is established. **Calculate** the pressure of CO_2 [atm] in the container and the amount of CO_2 [mol] dissolved in the water. The Henry coefficient of CO_2 for water at 10 °C is $k_H = 0.104 \times 10^4 \text{ atm}$, and we will consider that the reaction of CO_2 in water can be ignored.
- 2-2. Carbon dioxide ($N \text{ L}$) dissolved in water (1 L) is called $N \text{ GV}$ (Gas Volume), where N is the volume of this gas at 0 °C and 1 atm. **Calculate** how many GV the aqueous solution obtained in Q2-1 corresponds to.
- 2-3. When this container is heated to 50 °C, **calculate** the pressure of the gas [atm] in the container and the amount of CO_2 [mol] dissolved in water. Here, the Henry constant of CO_2 at 50 °C is $0.283 \times 10^4 \text{ atm}$.

Part 3. Removal of dissolved oxygen

- 3-1. A container (2.0 L) filled with water (1.0 L) has been left exposed to air for a long time at 1.0 bar and 25 °C. **Calculate** the mole fraction and mass of oxygen [mg] dissolved in the water. Here, assume that the atmosphere contains 21% oxygen.
- 3-2. The atmosphere in contact with this water is replaced with 1.0 bar argon and sealed, and the mixture is stirred sufficiently for the gas–liquid equilibrium to be established at 25 °C. **Calculate** the mole fraction of oxygen dissolved in the water. Here, the evaporation of water can be ignored during the gas replacement.
- 3-3. **Calculate** how many times the above operation must be repeated to reduce the mole fraction of dissolved oxygen to 1 ppt ($= 10^{-12}$) or less.

Part 4. Complex formation in water

Consider a mixture of two different gases (A and B) for which Henry's law holds. When gas molecules A and B do not interact with each other in either the gas phase or in water, the amount of each that will be dissolved in water is determined only by its partial pressure and does not depend on the partial pressure of the other gas. However, let us now consider the case in which A and B form a complex AB when they are dissolved in water:



Let x_i ($i = A, B, AB$) be the mole fraction of the dissolved species, and let K_{AB} be the equilibrium constant for the above equation:

$$K_{AB} = x_{AB}/x_A x_B.$$

Suppose that water ($V_l = 1.00$ L) and a gas mixture are filled into a container ($V = 2.00$ L) at 25° C. The Henry coefficients of A and B are 1.0×10^4 , and 2.0×10^4 bar, respectively, and $K_{AB} = 500$. Answer the following questions:

- 4-1. The initial partial pressures of each gas, P_A^0 and P_B^0 , are both 2 bar. **Calculate** the pressure of each gas and the mole fractions of the dissolved gas molecules after the equilibrium is established.
- 4-2. **Calculate** the percentage of the mole fraction of dissolved gas B relative to that found in Q4-1 when the initial partial pressure of gas A is increased to 10 bar.

II. Adsorption of molecules on a metal surface

Let us consider the adsorption of gas molecules on a metal surface under the following assumptions: (1) There are specific sites on the metal surface where the gas molecules are adsorbed; (2) when a gas molecule occupies an adsorption site, the site is blocked so that other molecules cannot be adsorbed at the occupied site; (3) the probability of the adsorption of a molecule onto an empty site does not depend on whether or not a molecule is adsorbed at the neighboring sites; *i.e.*, molecules adsorbed on the metal surface do not interact with each other. Here, we define parameters relevant to the adsorption: S_0 [mol m⁻²] is the density of adsorption sites; $\theta = a/S_0$ is the coverage, where a [mol m⁻²] is the number of adsorbed molecules per unit surface area; S [mol m⁻²] is the number of empty sites per unit area. Answer the following questions:

Part 5. Adsorption isotherm

- 5-1. The surface is exposed to a gas at a pressure P . Let the reaction rate constants of adsorption and desorption be k_a and k_d , respectively. **Write** an expression for the rates of adsorption and desorption in terms of P, k_a, k_d, a , and S .
- 5-2. Adsorption–desorption equilibrium is achieved when the adsorption and desorption rates are equal.

Let the equilibrium constant be $K = k_a/k_d$. **Write** an expression for the coverage θ at equilibrium in terms of K and P .

5-3. **Express** P in terms of θ and K for the case of extremely low coverage ($\theta \ll 1$).

5-4. Metal particles ($m = 100$ g) are placed in a container ($V = 1.00$ m³) and a gas A is introduced into the container at an initial pressure of $P_0 = 100$ Pa. The gas pressure decreases and then reaches a constant value. **Calculate** the pressure of the gas [Pa] in the container and the amount of gas molecules [mol] adsorbed on the surface of the metal particles. Here, assume that the surface area of the metal particles per unit mass is $A = 10.0$ m² g⁻¹; $S_0 = 1.66 \times 10^{-5}$ mol m⁻²; $K = 10.0$ Pa⁻¹; the temperature of the system is constant at $T = 300$ K and the volume of the metal particles is negligible.

Part 6. Adsorption of mixed gas

6-1. Consider the case in which two gases (A and B) are adsorbed on the metal surface. Assume that these gases do not interact or react with each other (neither in the gas phase nor on the surface after adsorption), and that an adsorption site can be occupied by either A or B. **Express** the coverage of A and B (θ_A and θ_B) in terms of the partial pressures of the gases (P_A and P_B) as well as the adsorption and desorption equilibrium constants (K_A and K_B).

6-2. When gases A and B are filled into the same container as in Q5-4, the partial pressures of each gas after reaching equilibrium are measured to be $P_A = 70.0$ Pa and $P_B = 30.0$ Pa. **Calculate** the coverage of each gas adsorbed on the surface of the metal particles. Let the adsorption and desorption equilibrium constants of gases A and B be $K_A = 10.0$ Pa⁻¹ and $K_B = 20.0$ Pa⁻¹, respectively.

6-3. Under the conditions where $K_A P_A \ll 1$ and $K_B P_B \ll 1$, how can the coverage θ_A and θ_B be approximated? **Write** approximate expressions in terms of P_A , P_B , K_A , and K_B .

6-4. Gases A and B are introduced into the container described in Q5-4 and the system reaches adsorption-desorption equilibrium. The partial pressure of gas A is found to be 70.0 Pa, which is the same as in Q6-2, whereas the partial pressure of gas B is 60.0 Pa, which is twice that in Q6-2. **Calculate** the percentage of coverage of gas A compared to that under the conditions of Q6-2.

III. Note

Comparing Part 4 and 6, we understand the following difference between gas dissolution in liquid and adsorption on metal surface. Under conditions where Henry's law holds, the dissolution of molecules into a liquid depends only on the partial pressure of the gas of interest. The same applies to adsorption onto a metal surface when the coverage is sufficiently low. However, even under conditions where Henry's law holds, if there is interaction and association between the molecules of the different species in the liquid, the amount of each species dissolved will depend not only on the partial pressure of the gas, but also on the partial pressure of the molecules of the other species. In contrast, as the coverage increases in the case of adsorption, the amount of adsorption for a given species will depend on the partial pressure of the molecules of the other species even if there is no interaction between the molecules of the different species. This is due to the finite number of sites where the molecules can be adsorbed on the metal surface.

Problem 4. Synthesis of diamonds

Diamond, one of the allotropes of carbon, is used not only for jewelry, but also in various tools that take advantage of its extremely high hardness. Natural diamond is considered to be produced under high-pressure and high-temperature conditions in the bowels of the earth. Currently, several techniques to synthetically generate diamonds are available, and massive amounts of artificial diamonds are used industrially.

Let us examine the stability of diamonds at ambient pressure and temperature. The enthalpies of combustion ($\Delta_c H^\circ$) for 1 mole of graphite, diamond, and C_{60} , as well as the standard entropy changes (ΔS°) for the conversion of 1 mole of graphite to diamond or C_{60} under ambient conditions (1 bar, 298.15 K) are summarized in Table 1. For graphite and diamond, 1 mole represents 12.01 g.

Table 1. Thermodynamic data for carbon allotropes

	$\Delta_c H^\circ / \text{kJ mol}^{-1}$	$\Delta S^\circ / \text{J K}^{-1} \text{mol}^{-1}$
Graphite	-393.5	(0)
Diamond	-395.3	-3.25
C_{60}	-25965	1.54

1. **Calculate** the change in enthalpy, entropy, and Gibbs free energy for the transformation of 1 mole of graphite into diamond and into C_{60} under ambient conditions. Then, **rank** graphite, diamond, and C_{60} in order of decreasing stability in terms of Gibbs free energy.
2. Under ambient conditions, diamond does not transform into graphite, which is energetically more stable than diamond. **Explain** why this transformation does not occur.

The enthalpies of combustion for graphite and diamond are comparable, and therefore, it is difficult to determine the change in enthalpy from graphite to diamond precisely via the calculation method used in Q1. To overcome this difficulty, the temperature dependence of the electromotive force of the following battery was measured:



This is a solid-state battery in which diamond is used as the cathode (positive electrode) and graphite is used as the anode (negative electrode). On the cathode, the diamond is reduced and CaC_2 is produced. On the anode, CaC_2 is oxidized and graphite is produced.

3. **Write** the half-reactions occurring on the cathode and the anode.
4. The electromotive force of this battery over the temperature range 940–1260 K can be expressed as a function of the absolute temperature T according to:

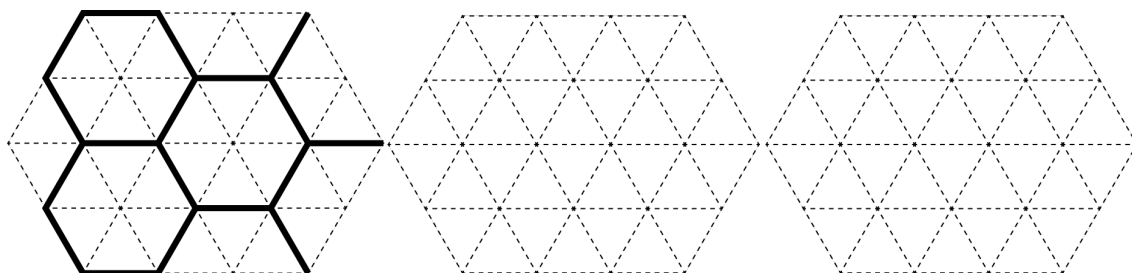
$$E = 11.4 + 0.0481T \text{ [mV]} \quad (2)$$

Calculate the change in enthalpy and entropy for the conversion of 1 mole of graphite to diamond in this temperature range.

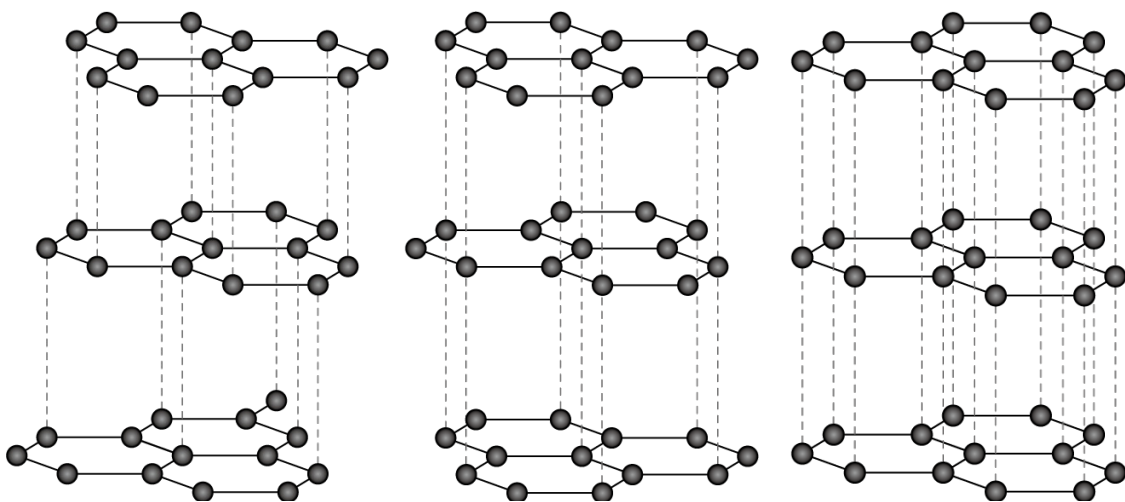
One of the techniques to synthesize diamond is the direct conversion of graphite into diamond by applying high pressure to graphite. The mechanism underlying this conversion is known as the puckering mechanism.

Graphite is composed of stacked layers of graphene. For each layer, there are three possible relative positionings in which the graphene layer can be placed. From here on, these geometries are referred to as A, B, and C. The crystal structures of graphite can exhibit one of three stacking patterns: AAAAAA... (1H where H stands for hexagonal), ABABAB... (2H), and ABCABC... (3R where R stands for rhombohedral). The most stable structure is 2H, and typical graphite also contains a small amount of the 3R structure.

5. One of the geometries of graphene is shown below (left, set as A). **Draw** the other two geometries (B and C, you do not have to distinguish these two).

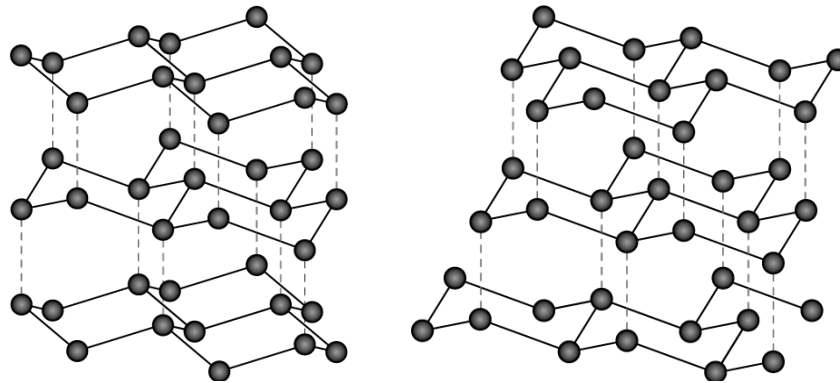


6. **Assign** the following three crystal structures as the 1H, 2H, and 3R structures.

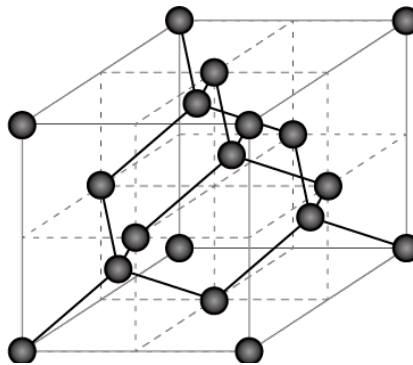


Diamond (cubic crystal) is generated from the 3R structure by displacing each carbon atom in a direction perpendicular to the plane. A crystal structure similar to that of diamond is obtained by displacing each carbon atom of the 1H structure in a direction perpendicular to the plane. The crystal structure generated from the 1H structure is called lonsdaleite, and is a hexagonal crystal. It has been theoretically predicted that pure lonsdaleite would be harder than diamond.

7. **Assign** the following crystal structures as diamond and lonsdaleite.



8. Under ambient conditions, the distance between covalently bonded carbon atoms in graphite is $1.42 \text{ \AA}$, while the distance between the graphene layers of graphite is $3.35 \text{ \AA}$; the distance between covalently bonded carbon atoms in diamond is $1.54 \text{ \AA}$. **Calculate** the density of graphite and diamond under ambient conditions. The unit cell of diamond is shown below:



In the puckering mechanism, there are two energy barriers: The barrier for the transformation from the 2H structure to the 3R structure (Step 1), and the barrier for the transformation of the carbon atoms from a planar to a tetrahedral configuration via puckering (Step 2).

9. The activation energy in Step 2 will be small if there is no volume change between graphite and diamond. **Calculate** the distance between the graphene layers of graphite for which there would be no volume change. Assume that the distances between the covalently bonded carbon atoms in graphite and diamond do not change on account of the applied pressure.

[Note] The direct conversion method described above requires high temperature (3000–4000 K) to increase the reaction rate in addition to high pressure ($\sim 10 \text{ GPa}$). A new conversion method, in which the graphite is first melted with metals to break the covalent bonds among the carbon atoms before new covalent bonds are generated under high-pressure conditions where diamond is thermodynamically stable, has been developed.

In addition to the direct conversion method, diamond can also be synthesized by a chemical vapor deposition (CVD) method. In this technique, a thin layer of diamond is grown on a substrate exposed to a gas containing hydrocarbon radicals prepared by heating or electrical discharge.

As an example, let us consider a diamond synthesis using methane and hydrogen molecules as sources. The reaction rates for the synthesis of diamond and graphite on the substrate, v_d and v_g , can be expressed in terms of the concentration of active hydrocarbons (such as CH_3 radicals) near the surface

of the substrate, C_C , and the rate constants, k_d and k_g , according to:

$$v_d = k_d C_C \quad (3)$$

$$v_g = k_g C_C \quad (4)$$

At the same time, diamond and graphite on the substrate are removed in the form of gaseous species (typically hydrocarbon radicals) due to reaction with hydrogen atoms near the surface. This process is called etching. The reaction rates for the etching of diamond and graphite from the substrate, v'_d and v'_g , are expressed in terms of the concentration of hydrogen atoms near the surface of the substrate, C_H , and the rate constants, k'_d and k'_g , according to:

$$v'_d = k'_d C_H \quad (5)$$

$$v'_g = k'_g C_H \quad (6)$$

10. **Write** an expression for the concentration of hydrogen atoms near the surface of the substrate in terms of C_C and the appropriate rate constants when the amount of graphite on the substrate remains constant.
11. **Write** an expression for the net growth rate of diamond on the substrate in terms of v_d and the appropriate rate constants under the condition where the amount of graphite on the substrate remains constant. (Based on this result, the condition that the reaction constants must satisfy can be obtained.)

To determine the activation energy of this process experimentally, the growth rate of diamond on the substrate is used. The measured growth rates of the thicknesses of the diamond layer on the diamond substrate for different substrate temperatures and gas compositions are shown in Table 2. In the case where only hydrogen gas was used, the substrate became thinner due to etching (eq. 5).

Table 2. Growth rates of diamond prepared by the chemical vapor deposition method

Substrate temperature	900 °C	1100 °C
CH ₄ 13% + H ₂ 87%	30.34 $\mu\text{m h}^{-1}$	63.43 $\mu\text{m h}^{-1}$
H ₂ 100%	-1.58 $\mu\text{m h}^{-1}$	-5.52 $\mu\text{m h}^{-1}$

Although the elementary steps of the synthesis and etching of diamond are not known, it is reasonable to define the activation energy for the total reaction, because the reaction rates for the synthesis and etching on the substrate follow the Arrhenius equation.

12. **Calculate** the activation energy of the synthesis of diamond when the composition of the source gas is CH₄ (13%) + H₂ (87%). Assume that the effect of etching by hydrogen gas is negligible compared to the synthesis of diamond.
13. **Calculate** the pre-exponential factor of the Arrhenius equation and the activation energy for the etching of diamond by hydrogen atoms.

14. When the experiment is conducted using a CH_4 (1%) + H_2 (99%) source gas mixture at 1000 °C, the thickness of the substrate does not change. Assuming that the etching of diamond by hydrogen atoms and the synthesis of diamond occur independently, *i.e.*, that the pre-exponential factor of the etching and the activation energies of the etching and diamond synthesis are the same as the values obtained in the previous questions, **calculate** the temperature of the substrate where the growth rate of diamond is $0.50 \mu\text{m h}^{-1}$ using the CH_4 (1%) + H_2 (99%) source gas. By controlling the reaction rate of the synthesis of diamond and etching appropriately as shown in this problem, a very thin diamond coating can be achieved.

Problem 5. Count the number of states

Boltzmann defined entropy as a measure of the number of possible microscopic states of a system, W , as:

$$S = k_B \ln W$$

Here, k_B is the Boltzmann constant. Hereafter, it is assumed that neither energy nor particles are exchanged between the system of interest and the surrounding environment, and that the system is in equilibrium at a constant temperature. In addition, the gas atoms and molecules (henceforth referred to as ‘molecules’) are assumed to behave as an ideal gas.

Now, let us explore the entropy of gas molecules using this definition in Questions 1–7.

Assume that ten molecules are arranged in two chambers separated by a wall, A and B, with four molecules in A and six in B. We describe this microscopic state as (4,6).

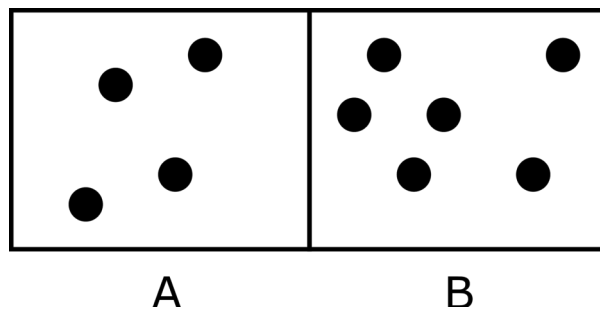


Figure 1. Example of a microscopic state in which ten molecules are distributed in two chambers.

The number of cases in which 10 molecules result in a (4,6) arrangement is calculated as:

$$W(4,6) = {}_{10}C_4 = 10! / 6! 4! = 210$$

For (5,5):

$$W(5,5) = {}_{10}C_5 = 10! / 5! 5! = 252$$

Thus, $W(5,5)$ is larger than $W(4,6)$. In this system, the number of cases represents the number of states for a specific arrangement of gas molecules in the two chambers.

1. **Calculate** $W(40,60)$ and $W(50,50)$ with 2 significant digits using the following approximate formula for a factorial:

$$n! \approx \sqrt{2\pi n} \left(\frac{n}{e}\right)^n$$

Removing the boundary wall that separates the two chambers in Figure 1 allows the molecules to move throughout the entire container. Assume that it is possible to measure the arrangement of the molecules instantly after the removal of the wall. If this measurement is performed a sufficiently high number of times, the probability that a state with an arrangement (n,m) will be found can be calculated.

2. **Calculate** the arrangement $(n^*, N - n^*)$ with the highest probability of occurrence for $N = 10$ and 100, as well as the corresponding probability of occurrence for each state. Moreover, **calculate** the probability of observing a state in which n^* is in the range $n^* - 0.02 N \leq n^* \leq n^* + 0.02 N$ for $N = 10$ and $N = 100$. Here both N and n^* are integers.

Let us consider the space inside chamber A, whose volume V_1 is composed of small subsections ΔV . As a molecule in the chamber is located in one subsection at any given time, the total number of possible locations of the molecule in the chamber W_A is given by $W_A = V_1 / \Delta V$. Likewise, the number of possible locations for a molecule that can access the whole chamber, whose volume is V_2 , can be

written as $W_{AB} = V_2/\Delta V$. Thus:

$$\frac{W_{AB}}{W_A} = \frac{V_2/\Delta V}{V_1/\Delta V} = \frac{V_2}{V_1}$$

Now suppose that chamber A is filled with n moles of gas molecules, while no molecules are present in chamber B (State 1), *i.e.*, chamber B is a vacuum. Then, the boundary wall is removed so that the gas in chamber A expands spontaneously throughout the entire container (State 2) at a constant temperature.

3. **Express** the change in entropy $\Delta S = S_2 - S_1$ in terms of the gas constants R , V_1 , and V_2 .
4. **Calculate** the difference in entropy for an isothermal expansion of the two-chamber system described above when chamber A is initially filled with oxygen molecules (0.30 mol). Use $V_1 = 0.10 \text{ m}^3$ and $V_2 = 0.40 \text{ m}^3$.

As shown in Figure 2, let State 1 be the case in which chambers A and B, whose volumes are identical, are each filled with a different kind of gas molecules. Suppose that these gases are mixed isothermally in a chamber with the same volume as chambers A and B (State 2).

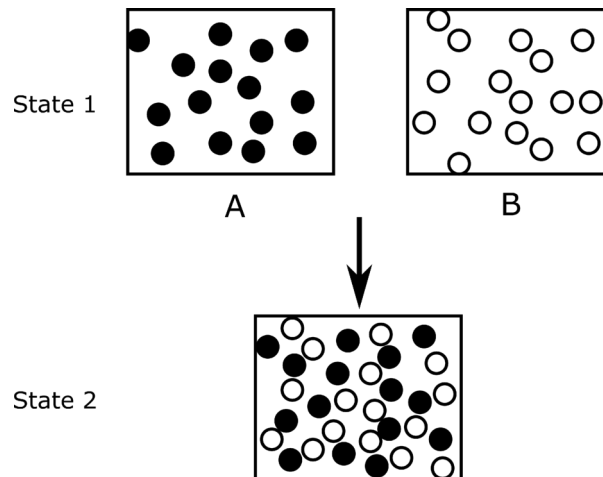


Figure 2. Isothermal mixing of different kinds of gas molecules in chambers with the same volumes.

5. **Calculate** the difference in entropy associated with the mixing process.

As shown in Figure 3, two kinds of gas molecules, α (n_α moles) and β (n_β moles), are separately filled into chambers A (volume V_A) and B (volume V_B), respectively, at a temperature T and a pressure P (State 1). Let State 2 represent the complete mixture of the gas molecules after removing the boundary wall.

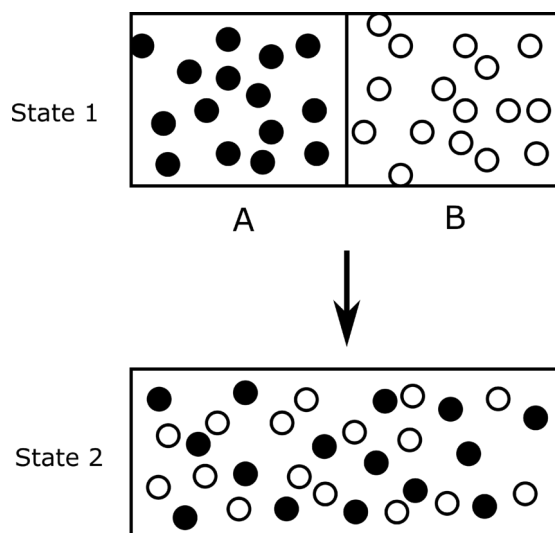


Figure 3. Mixing of different kinds of gas molecules accompanied by expansion.

6. **Express** the entropy change $\Delta S = S_2 - S_1$ from State 1 to State 2 in terms of R , n_α , and n_β .
7. Instead of being filled with molecules of gas β as in Q6, assume that chamber B is filled with molecules of gas α (n_β moles) (State 1), before the boundary wall is removed (State 2). **Calculate** the entropy difference from State 1 to State 2.

In Questions 8 and 9, we will explore the entropy associated with the orientation of molecules in a crystal.

According to the third law of thermodynamics, the entropy of a pure and perfect crystal approaches zero as the absolute temperature approaches 0 K. However, in a real molecular crystal, the molecules in the crystal may not be completely aligned at low temperatures. Thus, even when the absolute temperature approaches 0 K, the crystal can retain a finite nonzero entropy value. This is called residual entropy. For example, because carbon monoxide (CO) is a heterogeneous diatomic molecule, CO molecules have a definite orientation in the CO crystal. Figure 4A shows that the orientation of some molecules is disordered. Because a CO molecule can exhibit two different orientations in the crystal, the residual entropy per mole if the molecular orientations are completely random in the crystal would be:

$$S = k_B \ln 2^{N_A} = R \ln 2 = 5.7 \text{ J K}^{-1} \text{ mol}^{-1}$$

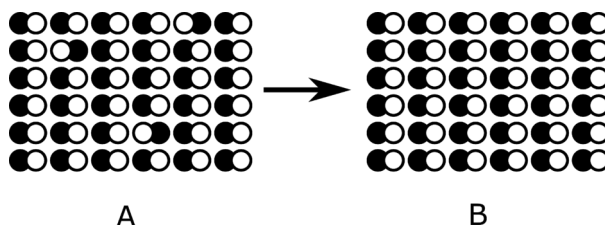


Figure 4. Schematic representation of disorder in the molecular orientation in a CO crystal. A: Some CO molecules are oriented in the opposite direction. B: An ideal crystal without any disorder in the molecular orientation.

8. Every methane (CH_4) molecule in a crystal is surrounded by four methane molecules in a tetragonal fashion. **Calculate** the molar residual entropy of isotopically labeled methane, H_3CD , when the molecules are completely randomly oriented.

Figure 5 shows a molecular arrangement of ice (solid H_2O); a central water molecule is coordinated by four water molecules in a tetragonal fashion.

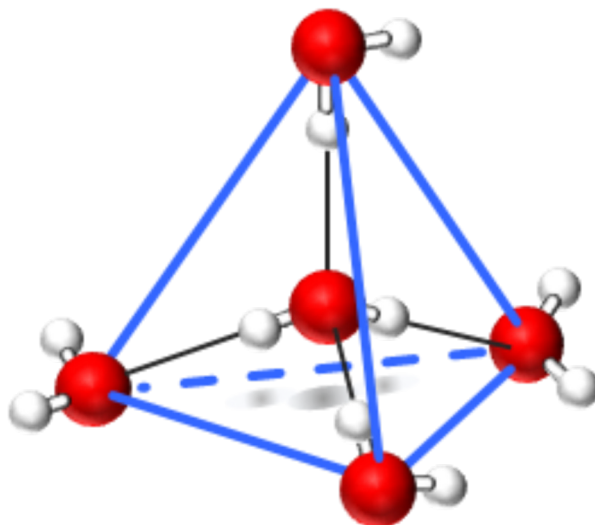


Figure 5. Arrangement of water molecules in an ice crystal.

All the water molecules are arranged in the crystal according to the so-called ‘ice rules’:

- (1) Each hydrogen atom must be located between two adjacent oxygen atoms.
- (2) Two of the four hydrogen atoms that surround each oxygen atom must be positioned closer to that oxygen than to the neighboring oxygen atoms, while the other two hydrogens should be located closer to one of the neighboring oxygen atoms.

9. Now, let us estimate the molar residual entropy of ice using the following procedures.

9-1. There are two stable sites for a hydrogen atom between two adjacent oxygen atoms. **Calculate** the number of possible configurations of hydrogen atoms in a crystal composed of 1 mole of water (N_A molecules) without any constraints of the ice rules.

9-2. **Calculate** the number of possible configurations for four hydrogen atoms around the central oxygen atom in Figure 5.

9-3. Some of the configurations calculated in Q9-2 such as $(\text{H}_3\text{O})^+$, in which three protons are arranged closest to one oxygen atom, violate the ice rules. **List** all chemical species that break the ice rules and **calculate** the number of configurations for each species. Then, **calculate** the number of configurations that satisfy the ice rules.

9-4. Based on these considerations, **calculate** the molar residual entropy when the orientation of water molecules is completely random in ice.

Problem 6. The path of chemical reactions

The structure of a molecule and its changes can be understood in terms of the potential energy. Consider the motion of the two atoms that make up a diatomic molecule AB. The velocity of the atoms A and B, whose masses are m_A and m_B , are denoted as v_A and v_B . The kinetic energy of the system is given by

$$T = \frac{1}{2}m_A v_A^2 + \frac{1}{2}m_B v_B^2 \quad (1)$$

Each atom, A and B, has three degrees of freedom, and there are six degrees of freedom in total. Because the motion of the molecule AB consists of the part of the translation and rotation of the whole molecule and that of the relative motion of the two atoms, the above equation can be rewritten as

$$T = \frac{1}{2}M_1 v_1^2 + \frac{1}{2}\mu(v_A - v_B)^2 \quad (2)$$

where μ is the effective mass defined as

$$\mu = \left(\frac{1}{m_A} + \frac{1}{m_B} \right)^{-1} \quad (3)$$

1. **Calculate** M_1 and v_1 in Equation (2). M_1 and v_1 are quantities with dimensions of mass and velocity, respectively.

The geometry of a diatomic molecule is determined only by the relative position (coordinates) of the two atoms, *i.e.*, the distance between them, R , which corresponds to the vibrational motion of the molecule. The potential energy E as a function of R near the equilibrium structure can be approximated by

$$E(R) - E_0 = \frac{1}{2}k(R - R_0)^2 \quad (4)$$

where E_0 is the reference energy and R_0 is the equilibrium internuclear distance. Under normal conditions, the molecule adopts a stable structure with the lowest energy. In this equation, k is a physical quantity corresponding to the spring constant that increases with increasingly stronger bonds. This quadratic representation is called the harmonic oscillator approximation, and k is linked to the frequency ν via the effective mass.

$$\nu = \frac{1}{2\pi} \sqrt{\frac{k}{\mu}} \quad (5)$$

2. Suppose that diatomic molecule XY forms either single or double bonds. What relationship can be expected for each k (k^S and k^D) and their corresponding equilibrium internuclear distances (R^{S_0} and R^{D_0})? **Choose** only one answer.

☐ $k^S > k^D$ and $R^{S_0} > R^{D_0}$	☐ $k^S > k^D$ and $R^{S_0} = R^{D_0}$	☐ $k^S > k^D$ and $R^{S_0} < R^{D_0}$
☐ $k^S = k^D$ and $R^{S_0} > R^{D_0}$	☐ $k^S = k^D$ and $R^{S_0} = R^{D_0}$	☐ $k^S = k^D$ and $R^{S_0} < R^{D_0}$
☐ $k^S < k^D$ and $R^{S_0} > R^{D_0}$	☐ $k^S < k^D$ and $R^{S_0} = R^{D_0}$	☐ $k^S < k^D$ and $R^{S_0} < R^{D_0}$

For diatomic molecules in reality, bonds break when R becomes sufficiently large; then atoms no longer interact with each other and the energy remains unchanged. The following equation, the so-called Morse potential approximation, is often used instead of the quadratic equation described above to better describe the potential energy of a molecule.

$$E(R) - E_0 = D_e \{1 - e^{-a(R-R_0)}\}^2 \quad (6)$$

where D_e , a , and R_0 are constants.

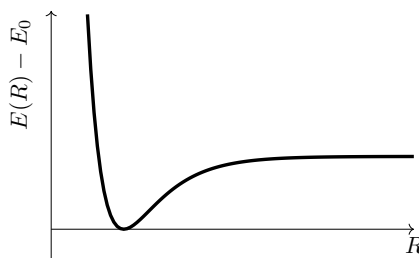
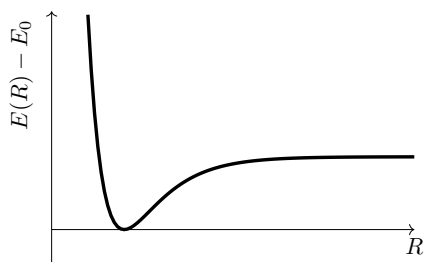


Figure 1. Morse potential

3. **Draw** D_e and R_0 in the figure below.



4. **Choose** all correct explanations for the harmonic and Morse potential approximation energy curves.

- ☐ For the harmonic oscillator approximation (Eq. 4) and the Morse potential approximation (Eq. 6), the equilibrium internuclear distance is the same.
- ☐ In the region where R is long, the Morse potential approximation is lower in energy than the harmonic oscillator approximation.
- ☐ In the region where R is short, the Morse potential approximation and the harmonic oscillator approximation coincide.
- ☐ As a increases in the Morse potential approximation, the width of the well becomes narrower.

For diatomic molecules, the energy E is represented as a one-dimensional curve that depends only on R (Figure 1), while for general polyatomic molecules, it is a multi-dimensional surface, *i.e.*, a point on such an energy surface corresponds to the structure of the molecule. Figure 2 shows a bird's-eye view of the energy surface, wherein the direction of the x -axis is the Morse oscillator and the direction of y -axis is the harmonic oscillator.

$$E(x, y) = 5.0\{1 - e^{-2.0(x-1.0)}\}^2 + 20.0(y - 2.0)^2$$

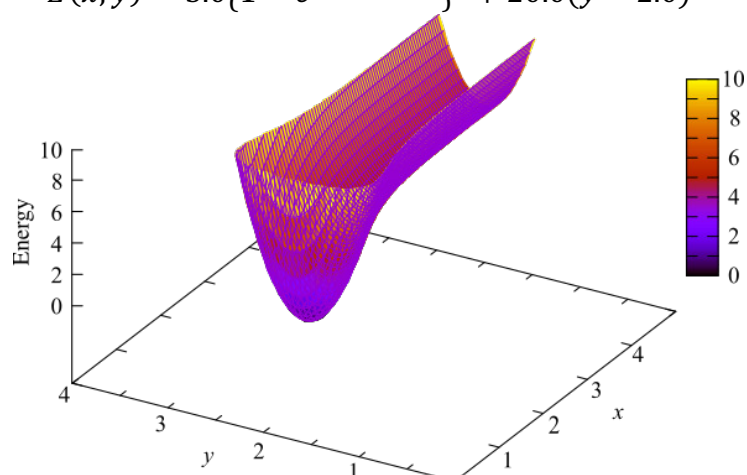
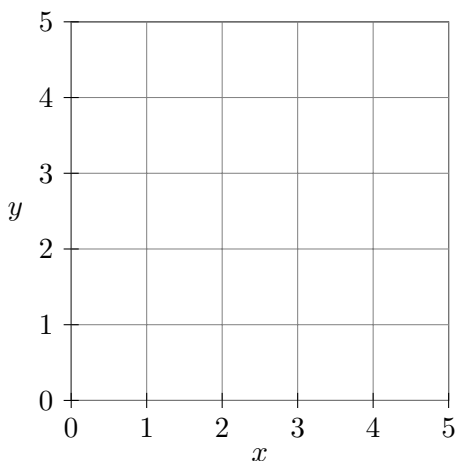


Figure 2. Energy surface in two dimensions

5. **Sketch** the contour map of this energy surface with the x axis as the horizontal axis and the y axis as the vertical axis.



The molecular geometry of a triatomic molecule can be determined by specifying three parameters that characterize the structure, such as both internuclear distances and the bond angle. A contour map of the potential energy surface of a typical triatomic molecular reaction $A+BC \rightarrow AB+C$ is shown in Figure 3.

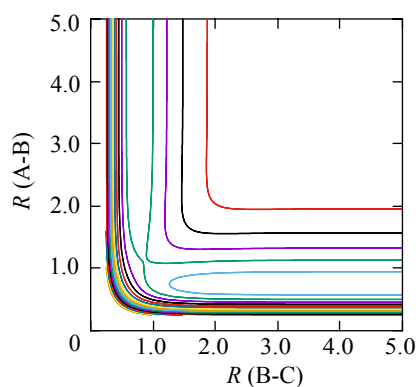
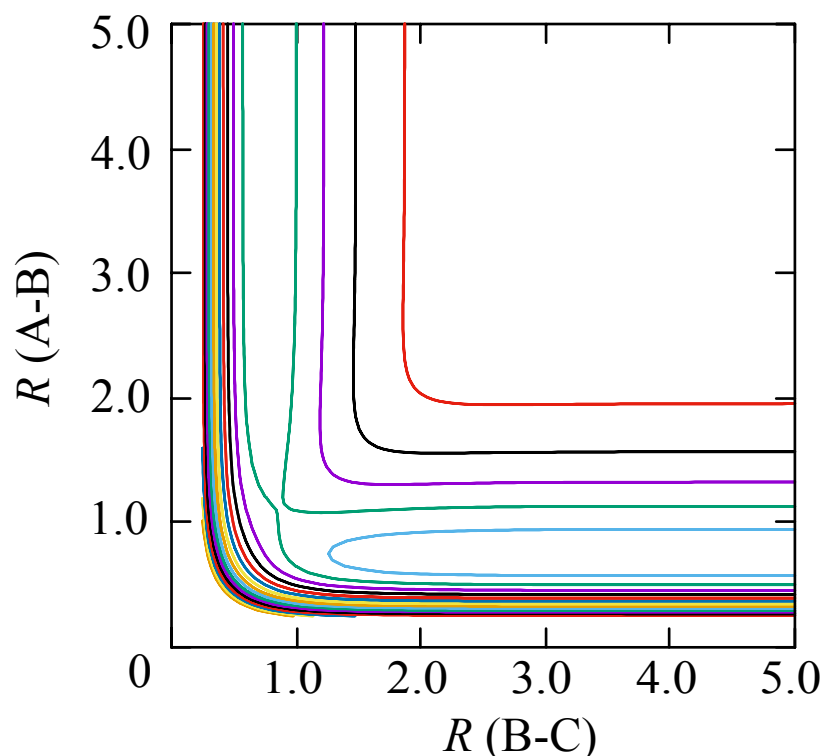


Figure 3. Contour map of the reaction $A+BC \rightarrow AB+C$

Here, A collides with a diatomic molecule BC, producing a new diatomic molecule AB and monatomic C. Assuming that the three atoms are always on the same line, two degrees of freedom allow us to completely determine the arrangement of the three atoms in the reaction process. In Figure 3, the vertical axis represents the internuclear distance of AB while the horizontal axis represents the internuclear distance of BC.

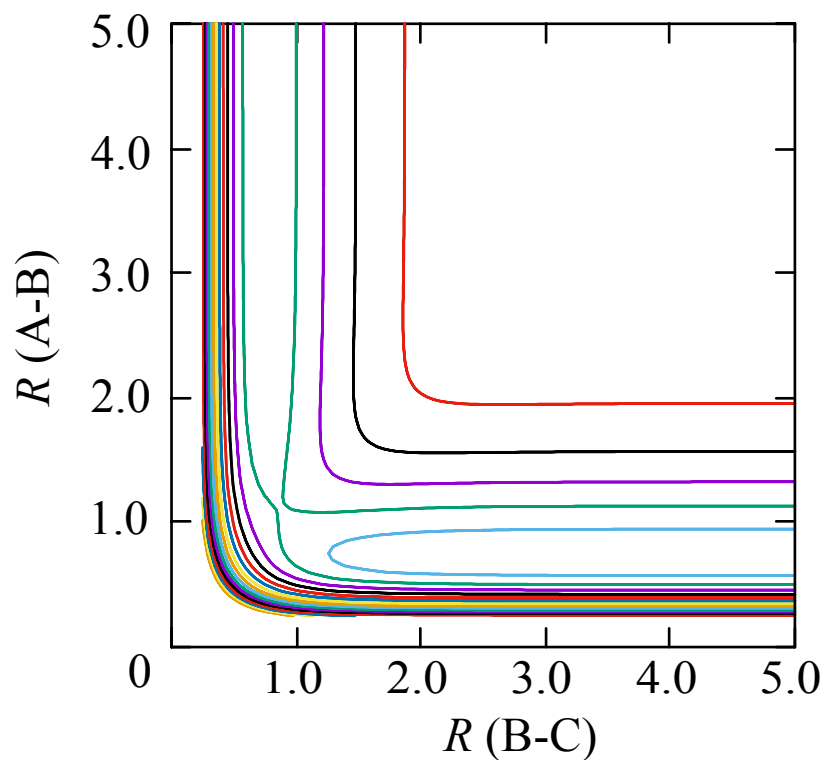
Thus, the structural change in the reaction can be interpreted as a pathway on the potential energy plane. Fukui has defined this pathway as the intrinsic reaction coordinate (IRC).

6. As a reaction path, consider a path that always minimizes the potential energy in any direction other than the reaction path. **Sketch** this path in the figure below.



In the actual reaction, the nuclei, which do not participate directly in the recombination of atoms, also oscillate and do not stop, which is the so-called ‘bobsleigh effect’. This corresponds to a motion in the direction perpendicular to the reaction coordinates.

7. Suppose that BC is vibrating before A collides, and that AB is also vibrating after the collision. **Sketch** a path of this reaction in the figure below.



Let's generalize further to consider reactions in more complex molecules.



As a result of this dissociation reaction, all the atoms change their position, bond length, and angles.

Let's focus on the distances shown in Figure 4.

R_{CC} : The distance between the carbon atoms

R_{HF} : The distance between H_α and fluorine (F)

R_{CH} : The average of the four hydrogen (H) -carbon distances

R_{CM} : The distance between the center of mass of HF and CH_2CH_2 moieties.

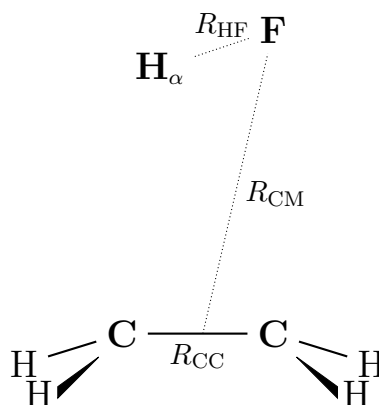


Figure 4. R_{CC} , R_{HF} , R_{CH} , and R_{CM} in the reaction $\text{CH}_3\text{CH}_2\text{F} \rightarrow \text{CH}_2=\text{CH}_2 + \text{HF}$

Figure 5 shows how the structure of the molecule changes while the reaction progresses. The vertical axis of the graph is the change in the interatomic distance ΔR from the beginning of the reaction, while the horizontal axis is the reaction coordinates, quantifying the progress of the reaction, which proceeds from left to right.

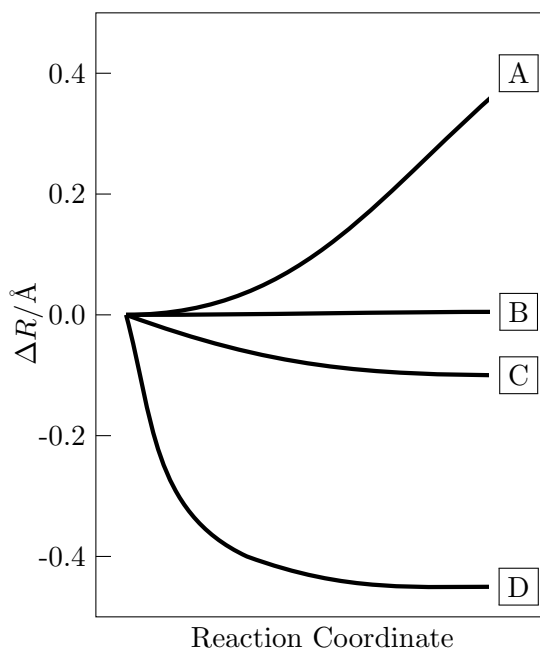


Figure 5. The change of R_{CC} , R_{HF} , R_{CH} , and R_{CM} during the reaction $\text{CH}_3\text{CH}_2\text{F} \rightarrow \text{CH}_2=\text{CH}_2 + \text{HF}$

8. **Match** A to D in the graph and the four distances mentioned above (R_{CC} , R_{HF} , R_{CH} , and R_{CM}).

Problem 7. Molecular vibrations and infrared spectroscopy

Consider the molecular vibration of hydrogen fluoride (HF). When HF diluted with a large excess of argon (Ar) is sprayed onto a cold cesium iodide (CsI) substrate at 12 K, the gas mixture condenses to generate a thin film on the substrate, which is known as the ‘Ar matrix’. In this matrix, the rotation of HF can be ignored, and vibrational interactions between Ar and HF are also negligible. As a result, the molecular vibration of an isolated HF molecule can be measured independently using infrared (IR) spectroscopy, which quantitatively reveals molecular vibrations. Since CsI does not absorb IR irradiation, the spectrum of HF in the Ar matrix film can be readily measured using IR spectroscopy, and a strong IR absorption peak appears at 3953.8 cm^{-1} in the spectrum.

The frequency of the molecular vibration of HF, ν_{HF} , is given by:

$$\nu_{\text{HF}} = \frac{1}{2\pi} \sqrt{\frac{k}{\mu_{\text{HF}}}}$$

Here, k denotes the spring constant of the chemical bond between H and F, which increases with increasing bond order. The reduced mass, μ_{HF} , is defined by:

$$\mu_{\text{HF}} = \frac{m_{\text{H}}m_{\text{F}}}{m_{\text{H}} + m_{\text{F}}},$$

where m_{H} and m_{F} are the atomic masses of H and F, respectively.

1. **Calculate** the wavenumber of the absorption peak of deuterium fluoride (DF) in an IR spectrum recorded using the Ar matrix technique. Let the spring constant of D–F be the same as that of H–F. The atomic masses of F, H, and D are 18.998, 1.0079, and 2.0141, respectively.

The quantized energy levels of molecular vibration, E_v , are defined by:

$$E_v = \left(v + \frac{1}{2}\right)h\nu \quad (v = 0, 1, 2, \dots).$$

Here, v is the quantum number of vibration.

The molecular vibrational energy is distributed over the quantized energy levels, and the distribution ratio is proportional to the following factor:

$$\exp\left(-\frac{E_v}{k_{\text{B}}T}\right).$$

This factor is known as the Boltzmann factor. Here, k_{B} and T are the Boltzmann constant and absolute temperature, respectively. Although this factor is proportional to the distribution ratio, it is not equal to the probability for each level. Therefore, when all the Boltzmann factors are summed up, the sum is not unity, but instead yields q_{vib} , *i.e.*, the ‘distribution function’. The actual distribution ratio at each level can be determined using the distribution function as the normalization constant.

2. **Write** the equation for the distribution function at a temperature, T , as the summation of a geometric series using the vibrational temperature, θ , which is defined as $\theta = h\nu/k_{\text{B}}$.
3. **Calculate** the vibrational temperature of HF.

When the substrate temperature is raised to 26 K, the HF molecules begin to move in the Ar matrix, which yields a molecular associate of two HF molecules, $(\text{HF})_2$, via hydrogen bonding as observed via a hydrogen-bonding-specific absorption peak in the IR spectrum. The hydrogen bond is generated from the overlapping wave functions of the electron of a lone pair and of a hydrogen atom. The molecule

donating the hydrogen is called the ‘donor’, whereas the molecule receiving the hydrogen on the lone pair is called the ‘acceptor’. The hydrogen bond between two HF molecules is most stabilized when the lone pair of the acceptor and the H–F bond of the donor are aligned linearly. In this situation, the hydrogen atom is shared by the two fluorine atoms.

4. Based on this description, **draw** a chemical scheme for the molecular associate (HF)₂. Use a dotted line to represent the hydrogen bond, and show apparently the lone pairs of the acceptor fluorine atom.
5. In the IR spectrum, a new absorption peak corresponding to the hydrogen-bonded acceptor is encountered. Does this new peak appear at a lower or higher wavenumber relative to the IR peak of the isolated HF molecule? **Choose** the correct shift with the most appropriate reason. Consider the fact that the H–F vibration becomes an F–H–F vibration with a different apparent mass, and that the bond order of the H–F bond is reduced when the hydrogen atom is shared by the two fluorine atoms.
 - (1) k becomes smaller and μ becomes smaller; a prediction of the peak shift is difficult.
 - (2) k becomes smaller and μ becomes larger, which results in a shift to a lower wavenumber.
 - (3) k becomes larger and μ becomes smaller, which results in a shift to a higher wavenumber.
 - (4) k becomes larger and μ becomes larger; a prediction of the peak shift is difficult.

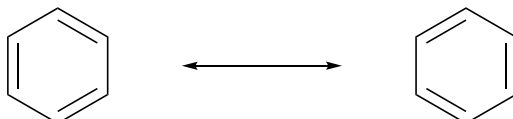
Active IR absorption modes are those with a vibrational energy transition of $\Delta v = +1$; such transitions are observed between various energy levels. At low temperature, however, only the $v = 1 \leftarrow v = 0$ transition needs to be considered. Here, the leftward arrow indicates an upward energy transition. This approximation is allowed because the occupation number at $v = 1$, g_1 , is much lower than that at $v = 0$, g_0 . As a result, higher energy transitions such as $v = 2 \leftarrow v = 1$ can be ignored.

6. **Calculate** the ratios g_1/g_0 at temperatures of 12 K and 25 °C for an absorption peak at 3953.8 cm⁻¹.
 - ¹. The occupation number for a given level is proportional to the distribution ratio at that level.

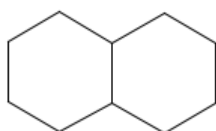
Problem 8. Quantum chemistry of aromatic molecules

The behavior of π -electrons is of paramount importance for understanding the reactivity and photophysical properties of aromatic compounds. In the electronic theory of organic chemistry, the electronic structure is considered to be a superposition of several ‘resonating’ electronic states.

- Following the example below, **draw** all possible resonance structures for the compounds listed below. It should be noted that the positions of the atoms (nuclei) must remain unchanged. As only the skeletons of the structures are shown, add bonds as appropriate according to the chemical formulae. Do not include resonance structures with separated charges or unpaired electrons.

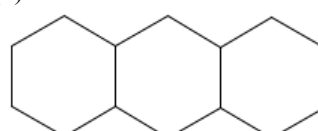


(a)



C₁₀H₁₈

(b)



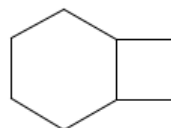
C₁₄H₂₄

(c)



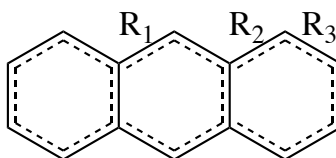
C₁₄H₂₄

(d)



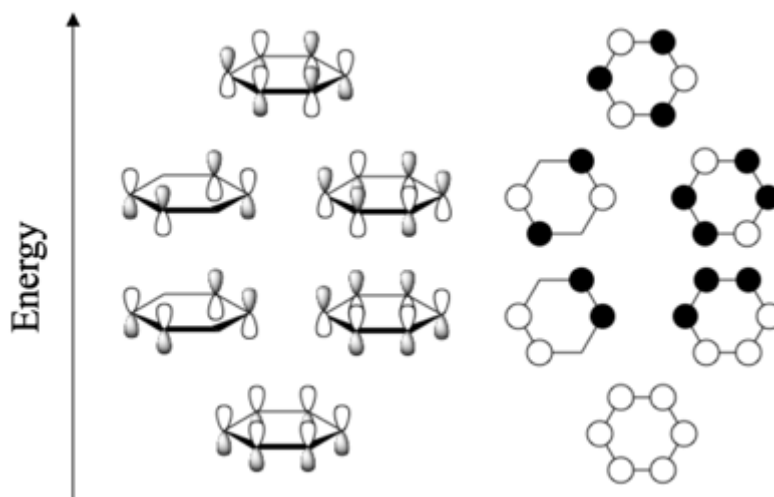
C₇H₁₂

- In real benzene, all carbon–carbon bonds have the same bond length (1.399 Å), which means that the two cyclohexatriene resonance structures are extremes, and their superposition represents the real molecule. With this in mind, we will consider the bond lengths R_1 , R_2 , and R_3 in anthracene. Assuming that R_S is the typical length of a carbon–carbon single bond (1.53 Å) and R_D that of a typical C=C double bond (1.34 Å), **arrange** R_S , R_D , R_1 , R_2 , and R_3 in order of length.



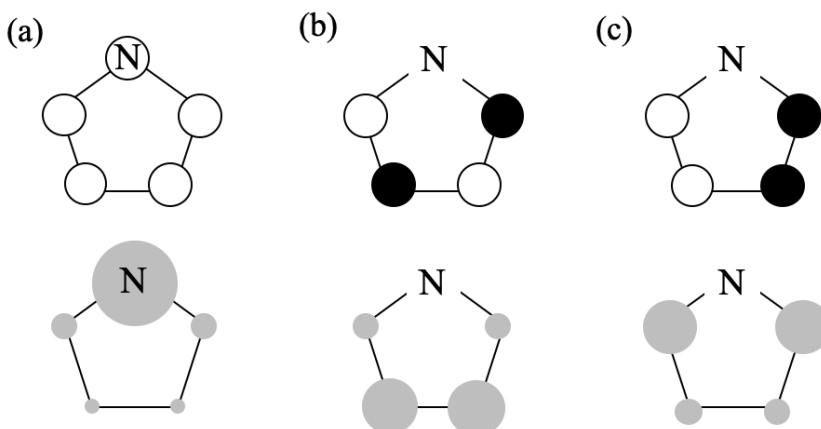
Following Questions are optional:

The properties of molecules are governed by their wavefunctions. Although resonance structures are useful for discussing various physical properties, it is difficult to use them to predict reactivity. The frontier orbital theory, proposed by Fukui and co-workers, is suitable for discussing reactivity based on molecular orbitals. For example, the six molecular orbitals of benzene are shown in the figure below.



The π -orbitals consist of p-orbitals perpendicular to the molecular plane of each atom (left panel); the white and black parts of each correspond to positive and negative values of the wavefunction. The right panel shows the same information more simply.

3. **Give** the number of orbitals occupied by π -electrons in benzene, naphthalene, and pyrrole.
4. Based on the following facts, **choose** the right pyrrole HOMO (highest occupied molecular orbital) from the options (a)-(c) below. The positive and negative values of wave functions are represented with white and black in the upper panel. In the lower panel, the circles on the atoms are drawn with a size proportional to the electron density.
 - The reaction readily takes place at the position with the largest electron density in the HOMO.
 - The electrophilic substitution reaction of pyrrole occurs faster at the 2 position than at the 3 position.



5. **Arrange** these orbitals in order of their energy, from lowest energy to highest energy. The diagram of benzene can be used as a guide.

Problem 9. Protic ionic liquids

Water undergoes autoprotolysis according to:



The product of the concentration of dissociated ions is constant and known as the autoprotolysis equilibrium constant.

$$[\text{H}_3\text{O}^+][\text{OH}^-] = K_w = 1.00 \times 10^{-14} \quad (25^\circ\text{C}) \quad (2)$$

The negative decadic logarithm of the concentration of H_3O^+ is known as the pH value, which is used as a scale of the acidity of an aqueous solution:

$$\text{pH} = -\log_{10}[\text{H}_3\text{O}^+] \quad (3)$$

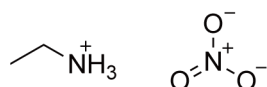
When the concentration of the cations and the anions generated by autoprotolysis is the same, the solution is said to be neutral. In the case of water at 25°C , the neutral condition, *i.e.*, $[\text{H}_3\text{O}^+] = [\text{OH}^-]$, holds when $\text{pH} = 7$.

1. Autoprotolysis also occurs in liquids other than water. For example, the autoprotolysis equilibrium constant of methanol is $10^{-16.7}$ at 25°C .

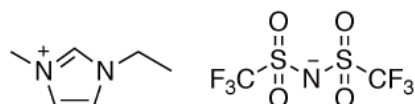
1-1. **Write** the chemical equation for the autoprotolysis of methanol.

1-2. **Calculate** the concentration of the cation of methanol under neutral conditions at 25°C .

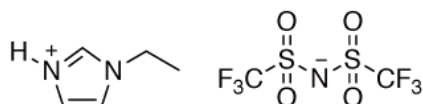
Substances composed of ionic bonds, such as sodium chloride, usually exist in solid form at room temperature. In 1914, ethylammonium nitrate was reported as a unique salt that exists as a liquid even at room temperature. Such salts are known as ionic liquids, and these have attracted considerable attention recently.



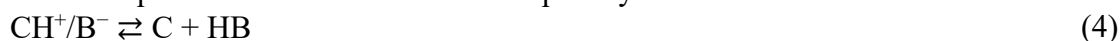
1-Ethyl-3-methylimidazolium bis(trifluoromethanesulfonyl)imide (hereafter denoted as CM^+/B^-) is a commonly used ionic liquid.



1-Ethylimidazolium bis(trifluoromethanesulfonyl)imide (hereafter denoted as CH^+/B^-), which has a similar structure to CM^+/B^- except that the methyl group on the imidazole ring is replaced by a proton, is also an ionic liquid.



CH^+/B^- shows an equilibrium that is similar to autoprotolysis:



$$K_s = [\text{C}][\text{HB}] \quad (5)$$

To determine the K_s of CH^+/B^- , electrochemical measurements have been conducted (Figure 1). Using CH^+/B^- as a solvent, a 0.35 mol L^{-1} bis(trifluoromethanesulfonyl)imide solution (henceforth: HB solution) and a 3.2 mol L^{-1} 1-ethylimidazole solution (henceforth: C solution) were prepared.

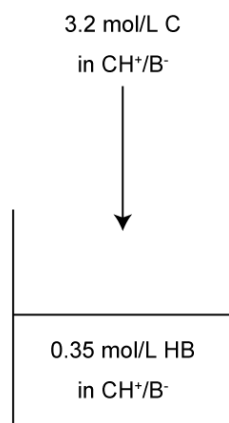


Figure 1. Schematic illustration of the experimental setup.

7.3 mL of the HB solution was titrated with the C solution, and the electromotive force was measured during the titration using an electrode that responds to HB. The obtained electric voltage, E_i , can be expressed by:

$$E_i = E^\circ + RT/F \ln[\text{HB}] \quad (6)$$

The resulting electric voltages as a function of the amount of the C solution added, V_i , are shown in Figure 2.

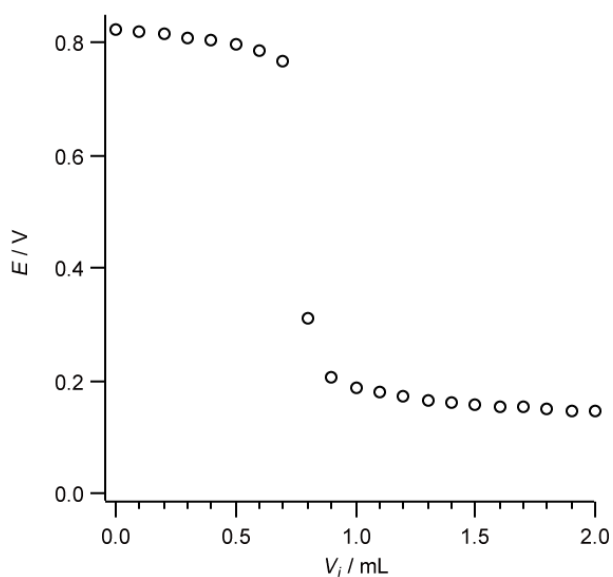


Figure 2. Electric voltages during the titration of the HB solution as a function of the amount of the C solution added (V_i).

The total concentration of protons, C_H , and the total concentration of imidazole, C_{im} , can be expressed by:

$$C_H = [\text{HB}] + [\text{CH}^+] \quad (7)$$

$$C_{im} = [\text{C}] + [\text{CH}^+] \quad (8)$$

In the following problems, assume that the temperature of the solutions is 25 °C.

- First, let us consider the case where there is an excess of HB. At the point of neutralization, the observed electric voltage changes drastically. This indicates that K_s is very small, and therefore almost all C added prior to the point of neutralization is protonated ($[\text{C}] \ll [\text{CH}^+]$).

2-1. Consider the case where the initial concentration of HB solution is $[\text{HB}]_0 (= 0.35 \text{ mol L}^{-1})$, the concentration of C solution is $[\text{C}]_0 (= 3.2 \text{ mol L}^{-1})$, the concentration of CH^+ originating from the solvent is $[\text{CH}^+]_{\text{sol}}$, and the volume of HB solution before the titration is $V_0 (= 7.3 \text{ mL})$. **Write** an expression for C_{H} and C_{im} in terms of V_0 , V_i , $[\text{HB}]_0$, $[\text{C}]_0$, and $[\text{CH}^+]_{\text{sol}}$. Assume that $[\text{CH}^+]_{\text{sol}}$ does not change during the titration.

2-2. When 0.50 mL of the C solution was added, E_i was 0.796 V. **Calculate** the value of E° . Note that the concentration of HB can be approximated as $[\text{HB}] = C_{\text{H}} - C_{\text{im}}$.

To analyze the obtained result, Figure 2 is replotted with $(V_0 + V_i)\exp(\pm E_i F/RT)$ as the vertical axis (Figure 3).

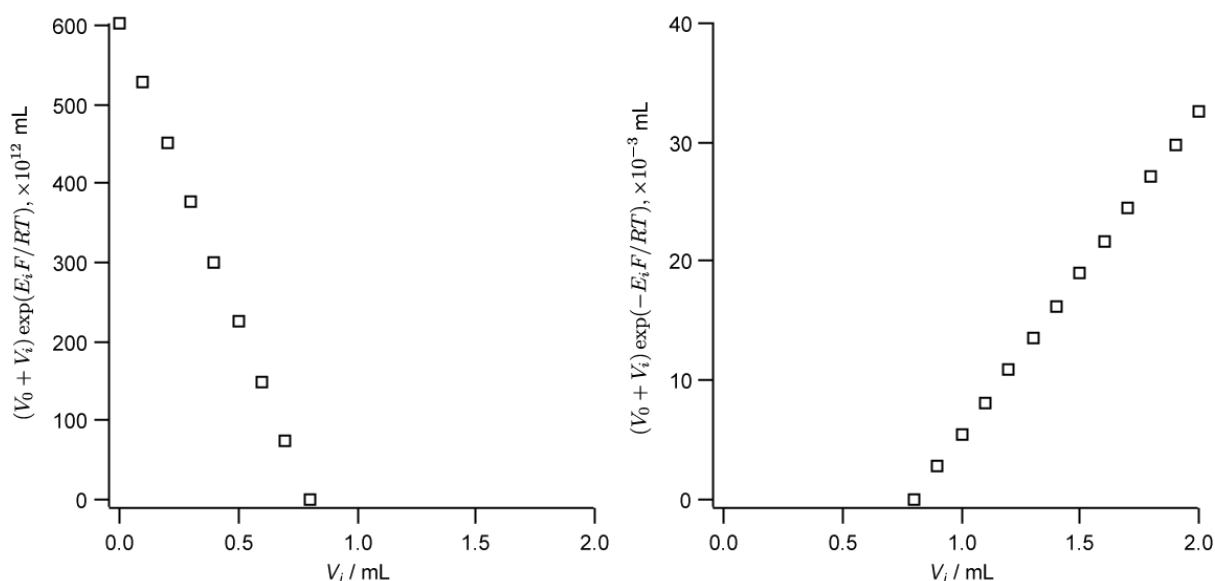


Figure 3. Replotted graphs of Figure 2.

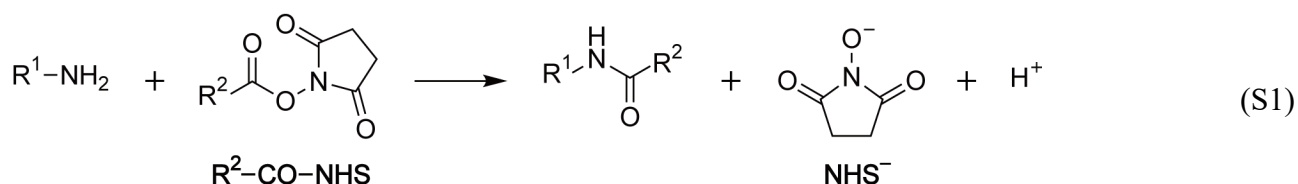
(Left) Before the point of neutralization. (Right) After the point of neutralization.

3. When the C solution is added beyond the point of neutralization, there is an excess of C. In this case, almost all the protons bind to C, and there are few protons that exist in the form of HB.

3-1. **Write** an expression for $[\text{HB}]$ beyond the point of neutralization in terms of C_{H} , C_{im} , and K_{s} . Assume that $C_{\text{H}} = [\text{HB}] + [\text{CH}^+] \approx [\text{CH}^+]$, which holds when there is an excess of C.

3-2. The slope of $(V_0 + V_i)\exp(-E_i F/RT)$ as a function of V_i is 0.0271 beyond the point of neutralization. **Calculate** K_{s} .

Let us consider how to control the reaction rate of the following chemical reaction.



An amide bond is produced by the reaction between the amine and the active ester. In the following problems, assume that all of the produced *N*-hydroxysuccinimide ($\text{p}K_{\text{a}} = 6.0$ in water) exists in the

deprotonated form (NHS⁻). Ignore the degradation reaction of the active ester. The temperature of the solutions is 25 °C.

First, let us consider reaction S1 in a buffered aqueous solution. In an aqueous solution, the acid–base equilibrium of R¹–NH₂ is expressed by:



$$K_a = [\text{R}^1\text{--NH}_2] [\text{H}_3\text{O}^+] / [\text{R}^1\text{--NH}_3^+] = 10^{-9.27} \quad (10)$$

The reaction rate of S1 is expressed as a second-order reaction:

$$d[-\text{NH--CO-}]/dt = k [\text{R}^1\text{--NH}_2][\text{R}^2\text{--CO--NHS}] \quad (11)$$

The variation of $[-\text{NH--CO-}]$ over time is obtained by integrating eq. 11, which gives:

$$[-\text{NH--CO-}] = ([\text{R}^1\text{--NH}_2]_0 + [\text{R}^1\text{--NH}_3^+]_0)(1 - \exp(-k[\text{R}^2\text{--CO--NHS}] f_a t)) \quad (12)$$

$[\text{R}^1\text{--NH}_2]_0$ and $[\text{R}^1\text{--NH}_3^+]_0$ represent the initial concentrations of R¹–NH₂ and R¹–NH₃⁺, respectively, while f_a represents the ratio of the deprotonated form of the amine, which is defined by:

$$f_a = [\text{R}^1\text{--NH}_2] / ([\text{R}^1\text{--NH}_2] + [\text{R}^1\text{--NH}_3^+]) \quad (13)$$

When the reaction occurs in a buffered aqueous solution, f_a remains constant during the reaction because the pH of the solution is constant.

4. The reaction progress in a mixture of 20 μmol of R¹–NH₂ in 10 mL of the buffer solution and 200 μmol of R²–CO–NHS in 10 mL of the buffer solution is monitored via the absorption of NHS⁻ in the ultraviolet region. In this case, the concentration of R²–CO–NHS is regarded constant during the reaction, because it is significantly higher than that of R¹–NH₂ (pseudo-first-order reaction).

Reaction S1 proceeds only for the deprotonated amine, R¹–NH₂. The protonated amine, R¹–NH₃⁺, does not react with the active ester.

- 4-1. **Calculate** the time at which half of the added R¹–NH₂ will have reacted when $k' = k[\text{R}^2\text{--CO--NHS}] = 5.0 \times 10^{-2} \text{ s}^{-1}$ and pH = 9.27.

- 4-2. In a differently buffered solution, the time at which one-third of the added R¹–NH₂ has reacted is 500 s when $k' = 5.0 \times 10^{-2} \text{ s}^{-1}$. **Calculate** the pH of the buffer solution in this case.

Then, let us consider reaction S1 in the ionic liquid CM⁺/B⁻. In CM⁺/B⁻, the acid–base equilibrium of R¹–NH₂ is expressed as follows:



$$K_a^A = [\text{R}^1\text{--NH}_2] [\text{HB}] / [\text{R}^1\text{--NH}_3^+] = 10^{-16.40} \quad (15)$$

The reaction rate of S1 is expressed as a second-order reaction:

$$d[-\text{NH--CO-}]/dt = k_l [\text{R}^1\text{--NH}_2][\text{R}^2\text{--CO--NHS}] \quad (16)$$

5. As shown in Q4, to control the reaction rate of S1, the ratio of $[\text{R}^1\text{--NH}_2]$ should be set to the appropriate value by adjusting the proton concentration in the solution. However, the ionic liquid CM⁺/B⁻ does not contain a proton. To solve this problem, let us use the ionic liquid CH⁺/B⁻, which was considered in Q2 and Q3, as a proton source for CM⁺/B⁻. The acid–base equilibrium of CH⁺ in CM⁺/B⁻ can be expressed by:



$$K_a^C = [\text{C}] [\text{HB}] / [\text{CH}^+] = 10^{-14.90} \quad (18)$$

- 5-1. **Calculate** the $[\text{HB}]$ of a $6.00 \times 10^{-3} \text{ mol L}^{-1}$ CH⁺/B⁻ solution dissolved in the ionic liquid CM⁺/B⁻.

- 5-2. A R¹–NH₂ solution is prepared using the solution from Q5-1 as the solvent. The $[\text{HB}]$ of the solution of 100 μmol R¹–NH₂ in 10 mL of the solvent is $5.39 \times 10^{-17} \text{ mol L}^{-1}$. **Calculate** the concentrations of CH⁺, C, R¹–NH₃⁺, and R¹–NH₂.

As shown in Q5-2, most of the protons added as CH^+ are transferred to $\text{R}^1\text{-NH}_2$ and exist in the form of $\text{R}^1\text{-NH}_3^+$. Similarly, the protons produced in reaction S1 also bind to $\text{R}^1\text{-NH}_2$. As the resulting chemical species, $\text{R}^1\text{-NH}_3^+$, does not react with the active ester, the reaction rate decreases as the reaction proceeds.

5-3. Reaction S1 is started once 100 μmol of $\text{R}^2\text{-CO-NHS}$ have been dissolved in the solution from Q5-2. **Calculate** the concentrations of HB, CH^+ , C, $\text{R}^1\text{-NH}_3^+$, and $\text{R}^1\text{-NH}_2$ when the concentration of $\text{R}^2\text{-CO-NHS}$ become $8.00 \times 10^{-3} \text{ mol L}^{-1}$.

5-4. To avoid a decrease in the reaction rate, the concentration of HB should remain constant. When CH^+/B^- and C are dissolved together, the concentration of HB is determined by the ratio of the concentrations of C and CH^+ . **Express** $[\text{HB}]$ in terms of $[\text{C}]$, $[\text{CH}^+]$, and K_a^{C} .

A buffer solution is prepared by adding the appropriate amount of C to 0.10 mol L^{-1} of CH^+/B^- solution using CM^+/B^- as the solvent. The reaction progress of a mixture of 20 μmol $\text{R}^1\text{-NH}_2$ in 10 mL of the buffer solution and 200 μmol of $\text{R}^2\text{-CO-NHS}$ in 10 mL of the buffer solution is monitored. The variation in $[-\text{NH-CO-}]$ over time can be expressed by:

$$[-\text{NH-CO-}] = ([\text{R}^1\text{-NH}_2]_0 + [\text{R}^1\text{-NH}_3^+]_0)(1 - \exp(-k_I' f_a t)) \quad (19)$$

5-5. The time at which one third of the added $\text{R}^1\text{-NH}_2$ will have reacted is 2000 s when $k_I' = k_I[\text{R}^2\text{-CO-NHS}] = 8.0 \times 10^{-4} \text{ s}^{-1}$. **Calculate** the concentration of C in the buffer solution.

[Note] The reaction control technique explained above has already been applied to the condensation of the two polymers shown in Figure 4. As a result, high-strength gels with homogeneous network structures were prepared from both aqueous solutions and ionic liquids (for an example, see: T. Sakai *et al.*, *Macromolecules* **2008**, 41, 5379).

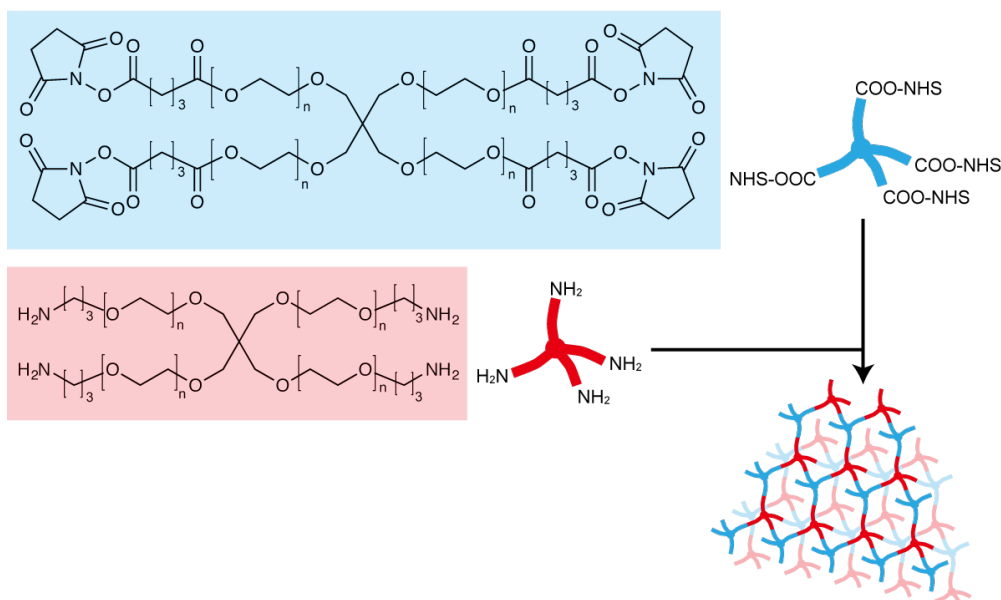


Figure 4. Conceptual illustration of the controlled synthesis of high-strength gels.

Problem 10. The Yamada universal indicator

In this problem, assume that the optical path length of the cell is 1.0 cm. Ignore the absorption of the cell and the solvent.

1. The acid dissociation constant of bromothymol blue (BTB) is $10^{-7.10}$. The absorbance values of $200 \mu\text{mol L}^{-1}$ BTB aqueous solutions with different pH values (2.00, 12.00) were measured, and the results are shown in Table 1.

Table 1. Absorbance values of $200 \mu\text{mol L}^{-1}$ BTB solutions

Wavelength	420 nm	501 nm	520 nm
pH = 2.00	1.74	0.70	0.36
pH = 12.00	0.60	0.70	1.06

- 1-1. **Calculate** the molar absorption coefficients of the protonated/deprotonated forms of BTB at 420 nm, 501 nm, and 520 nm.
- 1-2. At a certain pH value, the absorbance values of an aqueous solution containing a small amount of BTB at 420 nm and 520 nm were 1.13 and 0.52, respectively. **Calculate** the pH of this aqueous solution.
- 1-3. The aqueous solution used in Q1-2 was diluted 5 times using hydrochloric acid with pH = 1. **Calculate** the absorbance value of the diluted solution at 501 nm.
- 1-4. The aqueous solution used in Q1-2 was diluted 5 times using aqueous sodium hydroxide with pH = 12. **Calculate** the absorbance value of the diluted solution at 501 nm.

To estimate the pH of a solution using indicators, appropriate indicators that show a clear color change in the target pH region should be used. Universal indicators have been developed as easy-to-use indicators. Universal indicators can be prepared by mixing several kinds of indicators so that the resulting mixture shows color changes over a wide pH region. As a representative universal indicator, let us consider the Yamada universal indicator, which was developed by a Japanese researcher, Shinobu Yamada, in 1933.

The components of the Yamada universal indicator, its color under various pH conditions, the molar absorption coefficients of each indicator, and the acid dissociation constants of each indicator are summarized in Tables 2, 3, 4, and 5, respectively.

Table 2. Components of the Yamada universal indicator dissolved in 100 mL ethanol

Indicators	Molecular weight	Weight [mg]
Thymol blue (TB)	466.6	5.00
Methyl red (MR)	269.3	12.5
Bromothymol blue (BTB)	624.4	50.0
Phenolphthalein (PP)	318.3	100.0

Table 3. Color of the Yamada universal indicator under various pH conditions

pH	– 3	3 – 6	6 – 8	8 – 11	11 –
Color	Red	Yellow	Green	Blue	Purple

Table 4. Molar absorption coefficients of each indicator (unit: mol⁻¹ L cm⁻¹)

Wavelength [nm]	400	450	500	550	600	650
TB, H ₂ A	5500	2500	6000	18000	1500	0
TB, HA ⁻	6000	7000	3000	500	0	0
TB, A ²⁻	3500	1500	3500	10000	17500	2500
MR, HA ⁻	1000	10000	35000	35000	1500	0
MR, A ²⁻	15500	16000	4000	500	0	0
BTB, HA ⁻	7500	9000	3500	500	0	0
BTB, A ²⁻	5000	1000	3500	10000	20000	10000
PP, HA ⁻	0	0	0	0	0	0
PP, A ²⁻	1000	1000	6000	21000	1000	0

Table 5. Acid dissociation constants of each indicator

(In this problem, ignore all acid dissociation constants except for these.)

Indicator	TB	MR	BTB	PP
pK _a	pK _{a1} = 1.7, pK _{a2} = 8.9	5.1	7.1	9.7

2. The Yamada universal indicator (1.0 mL) was added to aqueous solutions (29.0 mL) with various pH values, and the absorbance of these solutions was measured. The measured absorbance values and the colors of the solutions are shown in Table 6. **Calculate** the pH of solutions (1), (2), and (3) after the addition of the Yamada universal indicator up to one decimal place.

Note that under each pH condition, only one of the four indicators exhibits a drastic change in the ratio of its protonated/deprotonated forms by the slight change of its pH value.

Table 6. Measured absorbance values and colors of the solutions

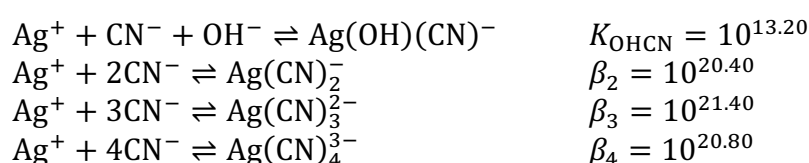
		Wavelength [nm]					
	Color	400	450	500	550	600	650
pH = 1.0	Red	0.236	0.407	0.655	0.609	0.028	0.000
(1)	Yellow	0.323	0.455	0.460	0.352	0.018	0.002
(2)	Green	0.435	0.440	0.176	0.121	0.179	0.089
(3)	Blue	0.466	0.360	0.645	1.979	0.673	0.275
pH = 12.0	Purple	0.490	0.384	0.793	2.498	0.701	0.276

Problem 11. Silver electroplating

Silver electroplating, in which silver is deposited on a metal surface, has been used to decorate objects and to increase their electrical conductivity. In silver electroplating, usually an aqueous alkaline solution containing Ag^+ and CN^- is used. The metal to be plated is used as the cathode, and silver ions are deposited on the metal surface by reductive deposition. Pure silver is used as the anode, from which silver ions are supplied to the solution by oxidative dissolution. The half reaction and standard electrode potential E° of the reductive deposition/oxidative dissolution of Ag^+ are as follows:



In the solution, Ag^+ forms several kinds of complexes with CN^- and OH^- . The complex formation reactions and formation constants are as follows:



where the overall formation constants β_i are defined as $\beta_i = \frac{[\text{Ag(CN)}_i^-]}{([\text{Ag}^+][\text{CN}^-]^i)}$.

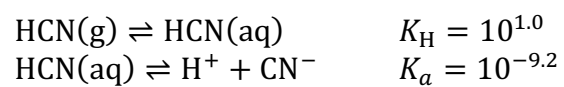
Answer the following questions. Unless otherwise noted, $[\text{CN}^-] = [\text{OH}^-] = 1.00 \text{ M}$, and the total concentration of Ag-related dissolved species is 1.00 mM . Use the absolute temperature $T = 298.2 \text{ K}$.

1. **Write** the five Ag-related dissolved species in this solution in order of concentration. **Calculate** the concentration of the species with the highest concentration.

> > > >

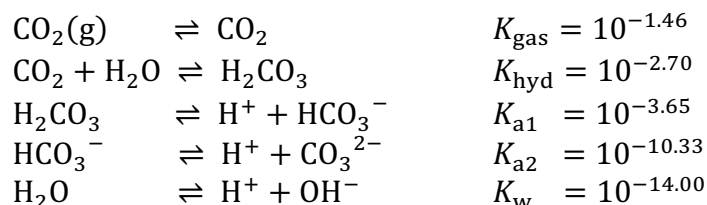
2. **Write** the half reaction in which the Ag-related dissolved species with the highest concentration in Q1 is reduced to Ag(s) . **Calculate** the E° of the half reaction.
3. If $[\text{CN}^-]$ varies from 1.00 M , the relative order of the species in Q1 will also vary. **Calculate** the concentration range of $[\text{CN}^-]$ within which the relative order in Q1 holds.
4. **Calculate** the equilibrium potential of the cathode, assuming that the cathode surface is covered with Ag(s) .
5. The reductive deposition reaction of silver competes with the hydrogen evolution reaction (HER). The potentials at which the HER occurs depend on the pH of the solution; the higher the pH, the more negative the potentials for the HER. By comparing the equilibrium potential calculated in Q4 with that for the HER, **calculate** the lower pH limit above which the reductive deposition reaction of silver is more thermodynamically favorable than the HER.

6. Because HCN(g) is highly toxic, the evolution of this gas should be minimized, even when using a fume hood. **Calculate** the pH requirements for the solution to keep the equilibrium partial pressure of HCN(g) below 10 ppm ($= 10^{-5.0}$ bar). Use the following equilibrium equations for the calculation.



Problem 12. How does CO₂ in the atmosphere affect the pH value of seawater?

Let us consider the chemical equilibrium of carbonic acid in ocean acidification, which is caused by an increase in the concentration of carbon dioxide in the atmosphere. Use the following equilibrium equations and constants:



where (g) denotes a species in the gaseous state, and all species other than CO₂(g) and H₂O are dissolved in an aqueous solution. Let the current value of the molar fraction of carbon dioxide in the atmosphere, x_{CO_2} , be 410 ppm ($= 410 \times 10^{-6}$ bar).

1. When pure water is left exposed to the atmosphere, it absorbs carbon dioxide from the atmosphere, which changes its pH. **Calculate** the pH of water in equilibrium with the atmosphere using the following charge balance equation:

$$[\text{H}^+] = [\text{OH}^-] + [\text{HCO}_3^-] + 2[\text{CO}_3^{2-}]$$

2. To the water in equilibrium with the atmosphere in Q1, a strong base or strong acid was added such that the pH changed by ± 1 ($\Delta\text{pH} = \pm 1$). The solution was then left exposed to the atmosphere again. What is the change in the amount of absorbed carbon dioxide relative to that before the addition? **Choose** the pH change for each scenario from the following Options. Assume that there is no change in the liquid volume due to the acid/base addition.

- (a) Strong base ($\Delta\text{pH} = +1$)
- (b) Strong acid ($\Delta\text{pH} = -1$)

Options

- (1) The amount of absorbed carbon dioxide increases to more than double the initial value.
 - (2) The amount of absorbed carbon dioxide decreases to less than half the initial value.
 - (3) The magnitude of the increase or decrease is less than described in Options (1) and (2).
3. Currently, x_{CO_2} continues to rise. A report has predicted that x_{CO_2} will exceed 800 ppm by 2070 (cf. IPCC RCP 8.5). **Calculate** the pH of water in equilibrium with the atmosphere if x_{CO_2} were twice its current value ($x_{\text{CO}_2} = 2 \times 410 = 820$ ppm) and **evaluate** the pH shift relative to the pH found in Q1 where the current x_{CO_2} value was used.

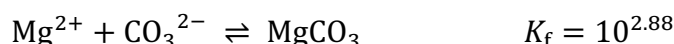
As x_{CO_2} rises, the oceans, like pure water, become more acidic. The current pH of the oceans is 8.05 on average, although it varies spatially and temporally. Compared to the pre-industrialization value in the 18th century, the current pH of the oceans has decreased by 0.1. If the pH decreases a further 0.2 to 7.85 in the future, the decrease in $[\text{CO}_3^{2-}]$ will result in CaCO₃ (aragonite), which is a component of the shells of corals and phytoplankton, being dissolved at low temperatures, causing severe damage to the marine biota. Let us estimate how much a rise in x_{CO_2} would reduce pH.

4. First, let us estimate the ocean acidification due to the rise in x_{CO_2} , ignoring chemical equilibria other than those of carbonic acid. A variety of ions are dissolved in the ocean. The difference in the concentration of the cations and anions originating from strong electrolytes, $C_{\text{C-A}}$, appears as a constant in the charge balance equation.

$$[\text{H}^+] + C_{\text{C-A}} = [\text{OH}^-] + [\text{HCO}_3^-] + 2[\text{CO}_3^{2-}]$$

Calculate the pH shift when x_{CO_2} increases from 410 to 820 ppm, with $C_{\text{C-A}} = 0.72$ mM.

5. In real seawater, chemical equilibria other than those of carbonic acid affect this pH shift. Let us calculate the pH shift taking into account the following ion-pair formation constant for MgCO_3 (dissolved species):



The charge balance equation can be written as:

$$2[\text{Mg}^{2+}] + [\text{H}^+] + C_{\text{C-A}} = [\text{OH}^-] + [\text{HCO}_3^-] + 2[\text{CO}_3^{2-}]$$

where $C_{\text{C-A}} = -105.0$ mM. Use $C_{\text{Mg}} = 53.0$ mM as the total concentration of Mg-related species.

Calculate the pH when x_{CO_2} changes from 410 to 820 ppm. It may be helpful to use an approximation, $(1 - x)^{-1} \sim 1 + x$, for $x \ll 1$. Can corals survive?

Let us consider the meaning of the pH shift evaluated in Q3 and Q4 using a virtual weak acid HA which dissociates as follows:



with the acid dissociation constant $K_a = 10^{-3.00}$ (note that this constant is different from that of carbonic acid). A solution is prepared using a given concentration of HA, C_{HA} , and a given concentration of its conjugate base salt NaA, C_{NaA} . The pH of the solution depends on these concentrations. The dependence of the pH on $\text{p}C_{\text{HA}} (= -\log_{10} C_{\text{HA}})$ and $\text{p}C_{\text{NaA}} (= -\log_{10} C_{\text{NaA}})$ is shown as a contour map below. A doubling in C_{HA} corresponds to a -0.30 shift of $\text{p}C_{\text{HA}}$ to the left in this contour map.

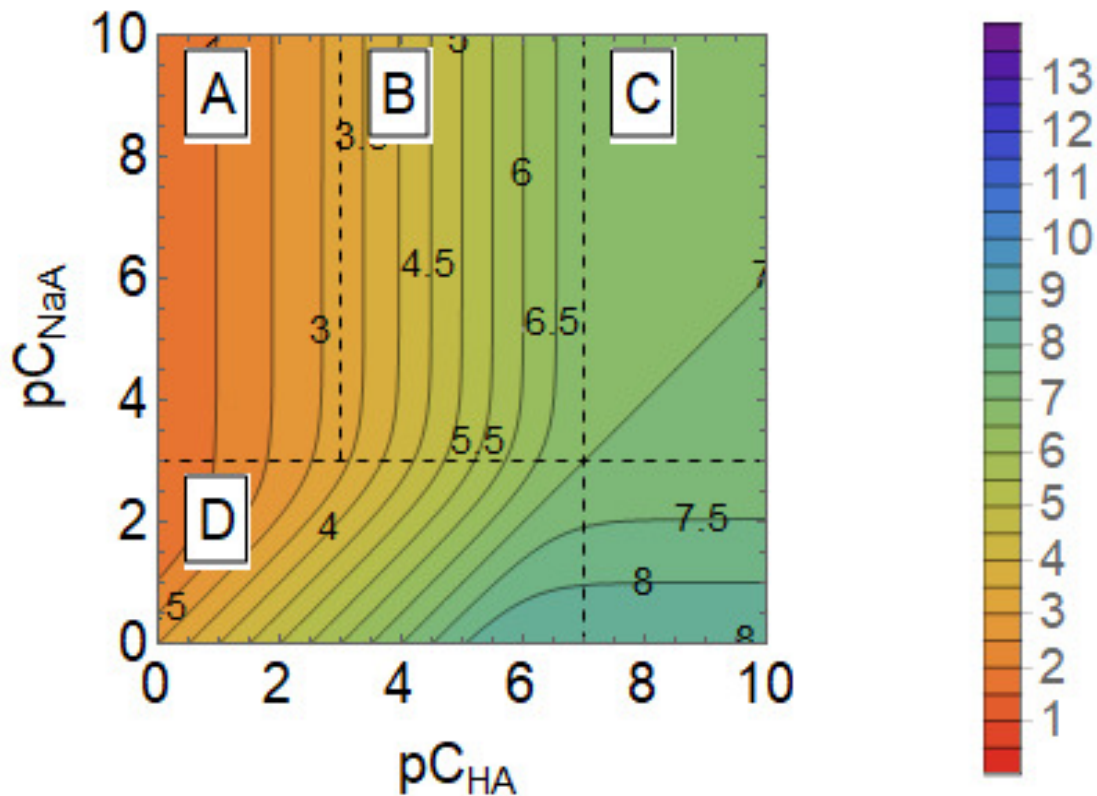


Fig. 1. Contour map of pH for an HA/NaA solution.

6. In the situation described in Q3, *i.e.*, pure water in equilibrium with the atmosphere, C_{NaA} is ideally zero and can be neglected. In the above contour map, this situation corresponds to either Region A, B, or C, where pC_{NaA} is large and the following inequalities for pC_{HA} hold:

$$\begin{aligned} \text{(Region A)} \quad & pC_{\text{HA}} < pK_a \\ \text{(Region B)} \quad & pK_a < pC_{\text{HA}} < \frac{pK_w}{2} \\ \text{(Region C)} \quad & \frac{pK_w}{2} < pC_{\text{HA}} \end{aligned}$$

Derive analytical solutions for the pH as a function of pC_{HA} using the charge balance equation:

$$[\text{H}^+] = [\text{OH}^-] + [\text{A}^-]$$

combined with the above inequalities for each Region. Because doubling C_{HA} corresponds to a -0.30 shift in pC_{HA} as described above, the pH shift can be determined from the derived analytical solutions. **Calculate** the pH shift when C_{HA} is doubled for Regions A, B, and C, respectively. The situation in Q3 corresponds to Region . **Fill** in this blank with either A, B, or C.

7. In the solution with $\text{pH} = 8.05$ in Q4, in which we ignored any chemical equilibria other than that of carbonic acid, HCO_3^- is the main component among the carbonic-acid-related dissolved species. This solution can be regarded as an aqueous solution of NaHCO_3 , which corresponds to Region D with a large C_{NaA} , *i.e.*, a small $\text{p}C_{\text{NaA}}$, in the contour map. In Region D, the Henderson–Hasselbalch equation holds, in which the equilibrium equation $K_a = \frac{[\text{H}^+][\text{A}^-]}{[\text{HA}]}$ is approximated using $[\text{HA}] = C_{\text{HA}}$ and $[\text{A}^-] = C_{\text{NaA}}$. **Calculate** the pH shift using the Henderson–Hasselbalch equation when C_{HA} doubles in Region D.

Problem 13. How to produce sulfuric acid and dilute it without explosion

Japan is a country rich in sulfur resources. Sulfuric acid can be synthesized from sulfide-based mineral resources such as copper sulfide, iron sulfide, and lead sulfide.

1. When a mixture of chalcopryrite (CuFeS_2) and silica sand (SiO_2) is melted at high temperature in the presence of oxygen in a blast furnace, sulfur dioxide is generated along with Cu_2S and FeSiO_3 (Reaction 1). The Cu_2S obtained in Reaction 1 reacts with oxygen at high temperature to form copper and sulfur dioxide (Reaction 2). **Write** the reaction formulae for Reaction 1 and Reaction 2.
2. **Calculate** how many kg of copper and how many liters of sulfur dioxide (at 25 °C, 1.00 bar) will be obtained from 100 kg of pure chalcopryrite by the process described in Q1. Assume that all the reactions proceed completely and that all gases are ideal gases.
3. Sulfur dioxide is oxidized to sulfur trioxide by air using a catalyst such as vanadium(V) oxide. This oxidation proceeds exothermically, and the reaction reaches an equilibrium state as it is a reversible reaction. Which of the following conditions is most appropriate to increase the production ratio of sulfur trioxide? **Choose** one option from (1) to (4).
 - (1) Low temperature / Low pressure
 - (2) Low temperature / High pressure
 - (3) High temperature / Low pressure
 - (4) High temperature / High pressure
4. A mixture of sulfur dioxide (7.00 mol) and oxygen (3.00 mol) is placed in a 50.0 L heat- and pressure-resistant container together with a catalyst. When the container is heated to 350 °C, the pressure increases to 8.60 bar. **Calculate** how many moles of sulfur trioxide are generated in this reaction.
5. The absorption of sulfur trioxide by concentrated sulfuric acid produces fuming sulfuric acid. Subsequent dilution of the fuming sulfuric acid with dilute sulfuric acid can afford the desired concentration of sulfuric acid. **Calculate** how many kg of 60% sulfuric acid are needed to dilute 20.0 kg of 32% fuming sulfuric acid (32% by weight SO_3 , 68% H_2SO_4) to obtain 98% sulfuric acid. Assume that the volatilization of the components during the dilution is negligible.
6. 8.0 kg of 98% sulfuric acid is diluted with water to give 60% sulfuric acid. **Calculate** the heat of dilution Q [J] released by this dilution process. Note that when 1 mol of H_2SO_4 is diluted with n mol of H_2O , the heat of dilution Q_0 [J] is expressed by the following formula:

$$Q_0[\text{J}] = \frac{7.47 \times 10^4 \times n}{n + 1.80}$$

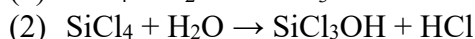
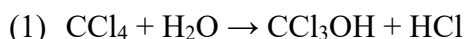
The amount of heat required to raise the temperature of 1 g of water by 1 °C is 4.18 J (1 cal). **Calculate** the increase in temperature that the released heat of dilution Q [J] would cause in 10 kg of water (0 °C).

Problem 14. Hydrolysis of C vs Si and the electronegativity of N vs Cl

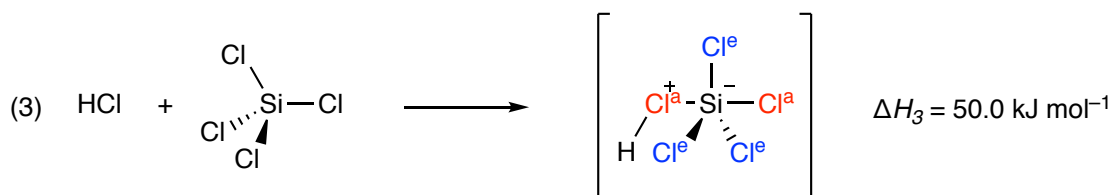
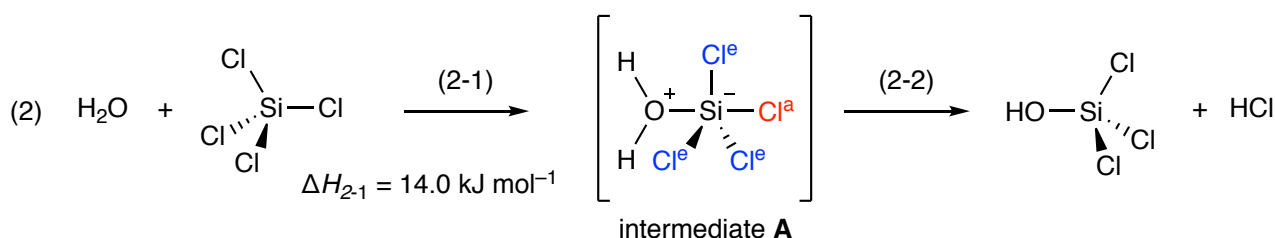
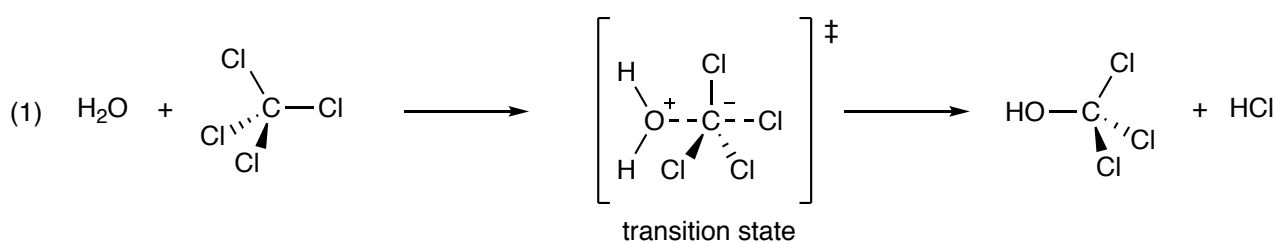
- Answer the following questions based on the following values of bond-dissociation energies [kJ mol^{-1}]. Assume that the reaction-enthalpy change can be estimated by considering only the bond-dissociation energies of the starting materials and the reaction products.

C–Cl: 335, C–O: 392, O–H: 467, H–Cl: 426, Si–Cl: 451, Si–O: 500, C–H: 413, Si–H: 318.

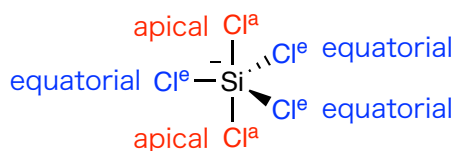
- Carbon tetrachloride is a stable compound in water, while silicon tetrachloride undergoes facile hydrolysis in water. For reactions (1) and (2) below, which are the initial steps of hydrolysis, **calculate** ΔH [kJ mol^{-1}], which can be estimated based on the bond dissociation energies.



In Q1-1, it cannot be anticipated whether the reaction would proceed smoothly based on only the enthalpy change of the bond-dissociation energies between the reaction substrates and the reaction products. The difference in reactivity between carbon tetrachloride and silicon tetrachloride described in Q1-1 can be explained by the one-step reaction in the carbon case and the multi-step reaction in the silicon case.



Equation (1) is a one-step reaction that requires a very large activation energy because its transition state involves a penta-coordinated carbon species. Equation (2) is a two-step reaction through an intermediate, which is a penta-coordinated silicon species. For example, as shown in equation (3), a penta-coordinated silicon compound known as a silicate should be generated by the reaction of silicon tetrachloride with hydrogen chloride. The molecular structure of the penta-coordinated silicon compound exhibits a trigonal bipyramidal geometry with a silicon atom at the center and a bonding atom at each vertex of the trigonal bipyramidal skeleton.

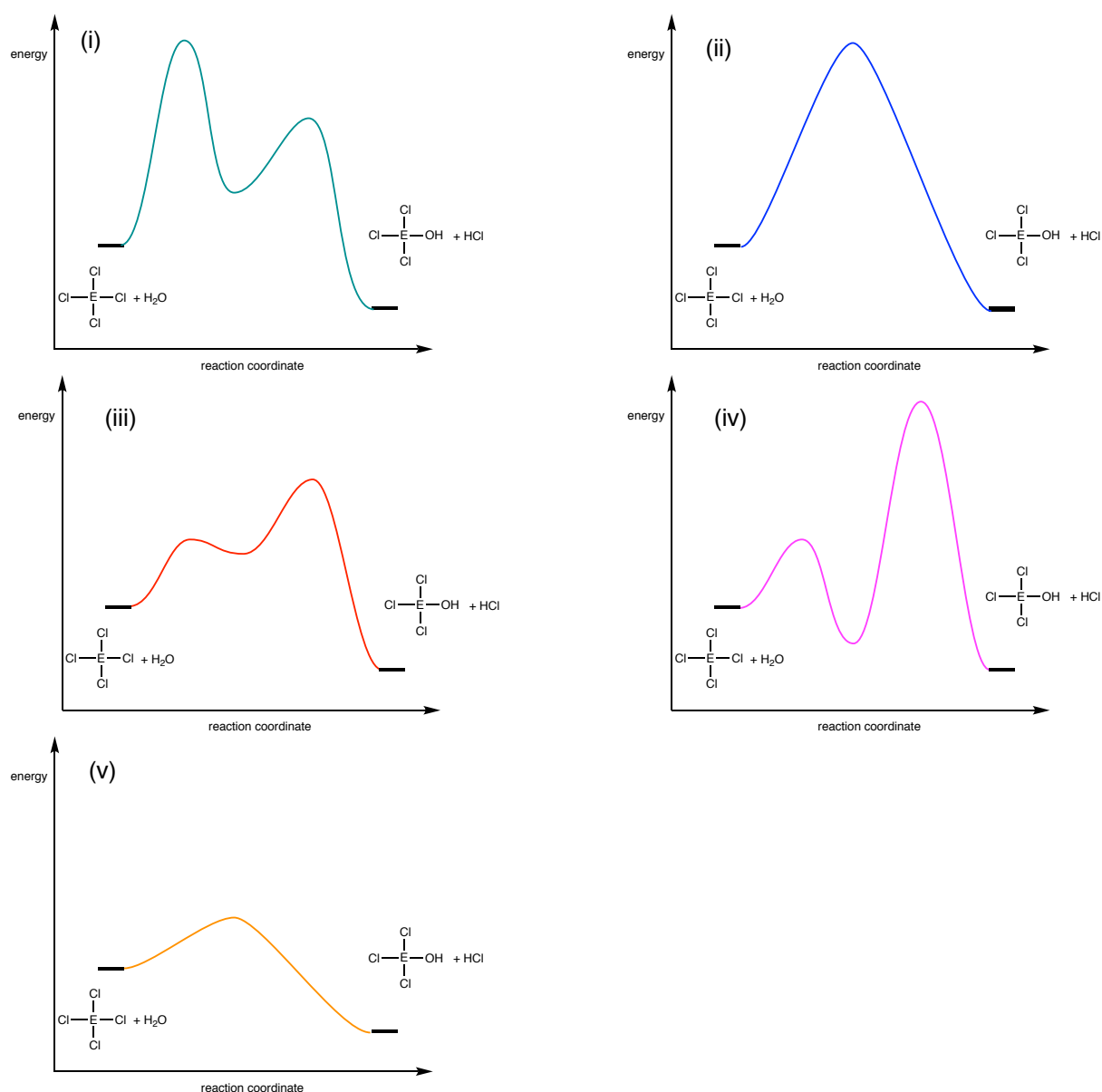


geometry of pentachlorosilicate SiCl_5^- ,
penta-coordinated silicon species

In this intermediate, the bond dissociation energies of the atoms located at the two vertices above and below silicon (apical positions) differ from those of the atoms located at the three vertices that form the triangle centered on silicon (equatorial positions). Assume that the bond-dissociation energies of the equatorial Si–Cl bonds ($\text{BE}(\text{Si}-\text{Cl}^e)$) are all equal, and that the bond-dissociation energies of the apical Si–Cl bonds ($\text{BE}(\text{Si}-\text{Cl}^a)$) are also equal. The bond-dissociation energy between the penta-coordinated silicon and the oxygen atom of the apical H_2O molecule is 400 kJ mol^{-1} , and the changes in the bond-dissociation energies of the O–H and Cl–H bonds upon coordination of the H_2O and HCl molecules to the silicon atom to form the corresponding silicates are negligible.

- 1-2. Provided that ΔH_{2-1} in Eq.(2-1) is 14.0 kJ mol^{-1} and ΔH_3 in Eq.(3) is 50.0 kJ mol^{-1} , **calculate** the bond-dissociation energies $\text{BE}(\text{Si}-\text{Cl}^a)$ and $\text{BE}(\text{Si}-\text{Cl}^e)$ between the silicon atom and chlorine atom at the apical and equatorial positions, respectively.

1-3. As described in Q1-2, it is important that silicon can adopt, in contrast to carbon, a penta-coordinate geometry in a meta-stable intermediate. This is due to the longer bond lengths of silicon relative to those of carbon; accordingly, there is a spatial margin around the central silicon atom, resulting in low repulsion between the five coordinated ligands. As can be found in Q1-2, although the bond-dissociation energy of each bond in the penta-coordinated silicon compound is smaller than that in the tetracoordinated silicon compound, the five weak bonds in the penta-coordinated silicon compounds should collectively yield sufficient stabilizing energy. Thus, the penta-coordinated silicon compound exhibits stability that is comparable to that of the corresponding tetracoordinated silicon compound. Based on the aforementioned considerations, **choose** the graphs that most appropriately represent the energy changes during the progress of reactions of (1) and (2), respectively.



Note that the vertical axes in figures (i)–(v) all have the same scale.

For certain elements A and B, the Pauling electronegativities χ_A and χ_B are defined according to the following equation:

$$(\chi_A - \chi_B)^2 = D_{AB} - (D_{AA} + D_{BB}) / 2$$

D_{AB} : Bond dissociation energy of an A–B bond [eV]

D_{AA} : Bond dissociation energy of an A–A bond [eV]

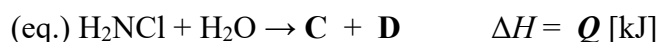
D_{BB} : Bond dissociation energy of a B–B bond [eV]

The Pauling electronegativities of hydrogen, nitrogen, and chlorine are as follows: $\chi_H = 2.10$, $\chi_N = 3.04$, $\chi_{Cl} = 3.16$. The bond-dissociation energies [kJ mol⁻¹] are as follows: N≡N: 945, O=O: 498, N–N: 158, H–H: 436, H–Cl: 426, Cl–O: 206, O–H: 467.

2-1. Based on these values, **calculate** the bond-dissociation energies D_{NH} , D_{NCl} , and D_{ClCl} for the N–H, N–Cl, and Cl–Cl bonds, respectively.

2-2. **Write** the molecular formulae that can apply to blanks **A** to **D** in the following sentence, and **calculate** the numerical value that applies to blank **Q**.

The Pauling electronegativities of nitrogen and chlorine are $\chi_N = 3.04$ and $\chi_{Cl} = 3.16$, respectively, and thus, the polarity of the N–Cl bond can be considered to be N⁺–Cl[–]. For example, in the hydrolysis reaction of monochloroamine (H₂NCl), it would be expected that nitrogen-containing product **A** and chlorine-containing product **B** will be produced based on the N⁺–Cl[–] polarization. In the actual reaction, however, nitrogen-containing product **C** and chlorine-containing product **D** are produced, as shown in the equation below. This result cannot be interpreted in terms of the Pauling electronegativities. The reaction between monochloroamine and water can be written as follows, and the enthalpy change in this reaction can be calculated as $\Delta H = Q$ [kJ] based on the values of the bond-dissociation energies, suggesting that this reaction should proceed endothermically.



Allred and Rochow defined electronegativity using the equation below. The Allred–Rochow electronegativity (χ_{AR}) depends on the values of the effective nuclear charge for the valence electrons ($Z_{\text{eff}}^{\text{VE}}$) and the covalent radius of the atom (r [pm]), based on the idea that electronegativity should be determined by the strength of the electric field on the atomic surface.

$$\chi_{AR} = 3590 \left(\frac{Z_{\text{eff}}^{\text{VE}} - 0.35}{r^2} \right) + 0.744$$

The effective nuclear charge (Z_{eff}) can be estimated according to Slater's rules as follows:

- (i) Write the electron configuration for the atom using the following pattern, in which electrons in the s and p orbitals should be combined into the same group, while those in the d orbitals should be independent from those in the s and p orbitals. For example, [1s], [2s, 2p], [3s, 3p], [3d].
- (ii) Identify the electron of interest and ignore all electrons in higher groups (larger “n” in [ns,np] group.). These do not shield electrons in lower groups.
- (iii) Regarding the shielding experienced by an s- or p- electron, electrons within the same group contribute **0.35** to the shielding, except for 1s electrons, which contribute **0.30** to the shielding.
- (iv) For the electrons in an [ns, np] group, the electrons in the n-1 group contribute **0.85** to the shielding.
- (v) For the electrons in an [ns, np] group, electrons in the n-2 or lower groups contribute **1.00** to the

shielding.

- (vi) For the electrons in an [nd] or [nf] group, electrons within same group contribute **0.35** to the shielding. All electrons in higher groups of [nd] and [nf] orbitals are ignored.
- (vii) For the electrons in an [nd] or [nf] group, the electrons in the lower groups contribute **1.00** to the shielding.

For example, according to Slater's rule, in the case of silicon ($_{14}\text{Si}$), which exhibits an electron configuration of $(1s)^2(2s)^2(2p)^6(3s)^2(3p)^2$, the effective nuclear charge for the valence electrons $Z^{\text{VE}}_{\text{eff}}$ (Si) can be estimated as $4.15 [= 14 - (0.35 \times 3) - (0.85 \times 8) - (1.00 \times 2)]$.

2-3. The covalent radii of nitrogen and chlorine are $r(\text{N}) = 70.0$ [pm] and $r(\text{Cl}) = 99.0$ [pm], respectively. Using the effective nuclear charge $Z^{\text{VE}}_{\text{eff}}$ estimated with Slater's rules, **calculate** the Allred–Rochow electronegativities $\chi_{\text{AR}}(\text{N})$ and $\chi_{\text{AR}}(\text{Cl})$ of nitrogen and chlorine.

The electronegativity values based on the Allred–Rochow definition can explain the products in the hydrolysis reaction of monochloroamine. Thus, 'electronegativity' is a concept that was qualitative in nature and whose numerical values vary depending on the definition.

Problem 15. Sulfur in hot springs and volcanoes

Japan is known as a volcanic country, and the hot springs that are widely distributed throughout the country are deeply beloved. Hot springs exhibit different characteristics regarding *e.g.* temperature, acidity (pH), color, and smell, and are classified according to the chemical components they contain. Interestingly, many hot springs contain sulfur components.

1. Water from a certain hot spring (density: 1.00 g cm^{-3}) contains both thiosulfate ions and hydrogen sulfide. An excess of cadmium acetate is added to 100 mL of this hot spring water, and the resulting precipitate (9.50 mg) is separated by filtration. A small amount of starch is added as an indicator to the filtrate, and an aqueous I_2/KI solution (effective I_2 concentration: $2.50 \times 10^{-2} \text{ mol L}^{-1}$) is slowly added dropwise. After the addition of 7.30 mL of the aqueous I_2/KI solution to the analyte, the coloration due to iodine came to appear. **Calculate** the total sulfur (S) content [mg kg^{-1}] in the initial hot spring water. Assume that sulfur is only derived from the thiosulfate ions and hydrogen sulfide and that no other species are involved in these reactions..
2. Hot springs that contain more than 2 mg of sulfur (S) derived from H_2S , HS^- , S^{2-} , and $\text{S}_2\text{O}_3^{2-}$ in 1.00 kg of hot spring water are known as ‘sulfur springs’. In a water sample from a hot spring, the density is 1.00 g cm^{-3} , the pH is 8.000, $[\text{S}^{2-}]$ is $1.00 \times 10^{-8} \text{ mol L}^{-1}$, and $5.26 \times 10^{-5} \text{ mol}$ of thiosulfate ion is present in 1.00 kg of the water. **Calculate** the total sulfur content [mg kg^{-1}] of this hot spring.
The first and second acid dissociation constants of hydrogen sulfide are $K_1 = 9.50 \times 10^{-8}$ and $K_2 = 1.30 \times 10^{-14}$, respectively.
3. To investigate the content of hydrogen sulfide and sulfur dioxide contained in volcanic gas, 10.0 L of volcanic gas are sampled. The gas is absorbed into 500 mL of an aqueous I_2/KI basic solution (effective I_2 concentration: $2.00 \times 10^{-2} \text{ mol L}^{-1}$) under basic conditions. The generated elemental sulfur is removed by filtration, and the volume of the filtrate is adjusted with water to give a total volume of 1.00 L. Two 100 mL aliquots of this solution are placed in two beakers, which are referred to as beakers **A** and **B**. Barium chloride is added to the solution in beaker **A** until no further precipitate appears, and 41.5 mg of white precipitate is isolated by filtration. The solution in beaker **B** is titrated with $2.00 \times 10^{-2} \text{ mol L}^{-1}$ sodium thiosulfate solution using starch as an indicator. After dropping 73.0 mL of the titrant into the solution, the coloration due to iodine disappears. **Calculate** the concentrations of hydrogen sulfide and sulfur dioxide in the volcanic gas [mol L^{-1}]. Assume that the only sulfur-containing components in this volcanic gas are hydrogen sulfide and sulfur dioxide, and that during the series of experiments described above, the hydrogen sulfide does not react with the sulfur dioxide directly, since they are present under dilute conditions. Additionally, assume that the only substances that react during this series of experiments are hydrogen sulfide, sulfur dioxide, and the related substances generated from them.

Problem 16. Identification of unknown compounds and allotropes

Part 1. Identification of inorganic compounds

[A] is a crystalline solid of a binary compound. It contains a metal ion X^{n+} and is grayish-white in color. [A] slowly reacts with water at room temperature to form [B], which is scarcely soluble in water; the generation of a gas is observed during this reaction. Dehydration reaction occurs upon heating [B] at approximately 350 °C to form the white compound [C], which contains 39.7 weight% of oxygen atoms. Heating [A] generates gas of an amount of 7.6 weight% based on [A], and the elemental metal X is formed. (i) Heating a mass M [g] of X under an N_2 atmosphere provides a yellow-green metal nitride. (ii) This metal nitride reacts with a large amount of water to generate [D]. The amount of [D] corresponds to the gas of volume 120 mL at 1 bar and 25 °C.

1-1. **Write** the chemical formulae of compounds [A], [B], [C], and [D].

1-2. **Write** the chemical reactions corresponding to the underlined parts (i) and (ii).

1-3. **Calculate** the weight M [g].

Part 2. Allotropes

The term “allotrope” refers to one or more physical forms of a chemical element that occur in the same physical state. Allotropes generally exhibit different physical properties and may also differ in their chemical reactivity. For example, graphite and diamond have long been known as allotropes of carbon, and more recently, fullerenes and carbon nanotubes have been discovered as further carbon allotropes. One of the allotropes of phosphorus is a solid composed of P_4 molecules, which is called white phosphorus. It has a low melting point of 44 °C and is highly toxic, so care must be taken in its storage.

2-1. The solution ^{13}C NMR spectrum of fullerene C_{60} (Figure 1) exhibits [E] peak(s). X-ray diffraction measurements have revealed [F] different covalent carbon–carbon bond length(s) in the crystal structure of fullerene C_{60} . **Write** the appropriate integer values for [E] and [F].

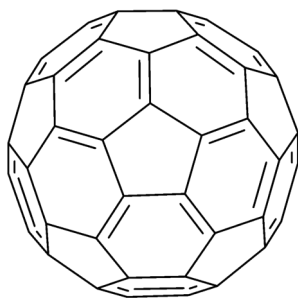


Figure 1. Structure of fullerene C_{60} .

2-2. Fullerene C_{60} forms a crystal via van der Waals forces. The crystal structure of fullerene C_{60} at room temperature is composed of a cubic unit cell with dimensions of 1.41 nm on each side. The molecules are located at all vertices and at the centers of all faces of the cubic unit cell. **Calculate** the density [$g\ cm^{-3}$] of the crystal of fullerene C_{60} .

2-3. The P_4 molecule has high structural symmetry, and all the P–P–P bond angles are 60°. **Draw** the steric structure of P_4 .

Dioxygen and ozone are the allotropes of oxygen. Ozone acts as a strong oxidizing agent. For example, (iii) the oxidation reaction of potassium iodide by ozone in aqueous solution is accompanied with the generation of dioxygen, and the reaction is used for the quantitative determination of ozone. Ozone also exists in the stratosphere and acts as a filter that absorbs harmful ultraviolet light from sunlight. Dioxygen in the stratosphere is irradiated with ultraviolet light of wavelengths < 240 nm, where a dioxygen molecule is split into two oxygen atoms that react with another dioxygen molecule to produce ozone. On the other hand, ozone decomposes into dioxygen molecule and an oxygen atom when exposed to ultraviolet light with a wavelength of 240–315 nm. When these formation and decomposition reactions of ozone are in equilibrium, the concentration of ozone in the stratosphere is maintained at a constant level, blocking short-wave ultraviolet rays that are harmful to humans on the ground. In contrast, (iv) atmospheric nitric oxide reacts with ozone, and (v) nitrogen dioxide reacts with oxygen atoms, resulting in (vi) a reaction that converts ozone into dioxygen. This creates an ozone hole that can allow harmful ultraviolet radiation from the sun to reach the surface on the earth.

2-4. **Write** the reaction formula for the underlined part (iii).

2-5. N [mol] of ozone is bubbled through 15 mL of an aqueous solution of potassium iodide with a concentration of 1.0 mol L^{-1} ; we assume that the ozone reacts completely. The solution is then titrated with an aqueous solution of sodium thiosulfate with a concentration of 0.20 mol L^{-1} ; the titration requires 3.5 mL of the sodium thiosulfate solution. **Calculate** N [mol].

2-6. **Write** the reaction formulae for the underlined parts (iv)–(vi).

Problem 17. Metal oxides

1. In the crystal structures of most metal oxides, the oxide ions (O^{2-}) form a close-packed structure, wherein the metal ions occupy the voids created by O^{2-} . Figure 1(a) shows the cubic close-packed structure created by O^{2-} . Note that the ionic radius of O^{2-} is 0.140 nm. Answer the following questions.

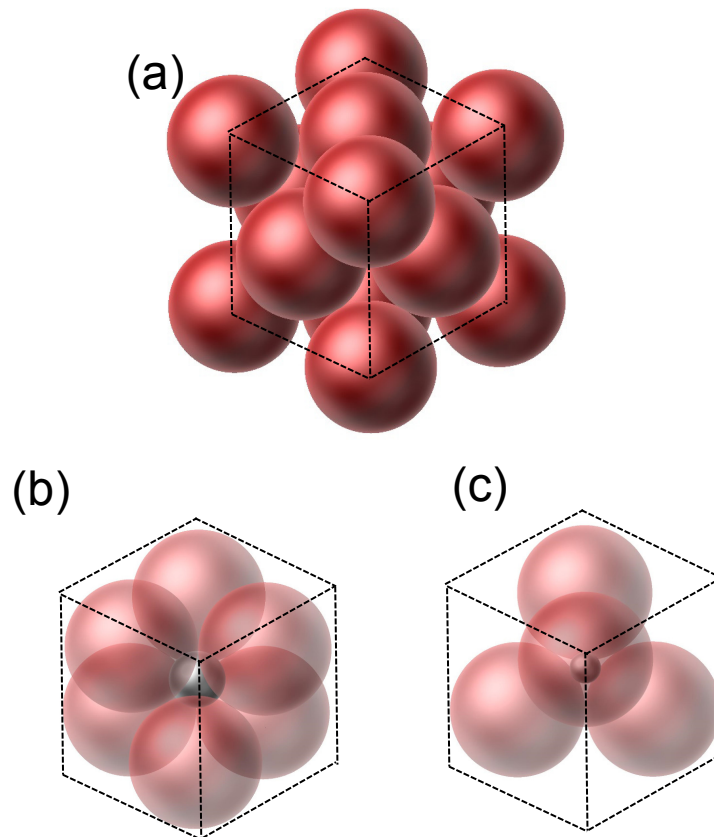


Figure 1. (a) Cubic close-packed structure formed by O^{2-} in metal oxides, (b) octahedral void, (c) tetrahedral void. ● O^{2-} ions, ● voids.

- 1-1. Considering O^{2-} as solid spheres in contact with each other, **calculate** the percentage volume of the voids in a cubic close-packed structure.
- 1-2. With reference to Figure 1(b) and (c), **calculate** the maximum radii of the spheres that can be placed in the octahedral and tetrahedral voids of a cubic close-packed structure composed of O^{2-} , respectively.
- 1-3. **Write** the chemical formula for a ternary metal oxide $A_xB_yO_z$ wherein one metal ion (A) occupies 1/8 of the tetrahedral voids in a cubic close-packed structure composed of O^{2-} , and a second metal ion (B) occupies 1/2 of the octahedral voids.
- 1-4. Regular arrays of atoms, ions, or molecules in solids are represented by a repeating unit known as the unit cell. In $SrTiO_3$, which adopts a perovskite structure, the ionic radii of Sr^{2+} and O^{2-} are comparable, and a cubic close-packed structure is formed by Sr^{2+} and O^{2-} . The Ti^{4+} ions occupy all octahedral voids formed by O^{2-} . Based on this information, **draw** the unit cell of $SrTiO_3$ with reference to Figure 2, assuming Ti^{4+} (●) is located at the center of the cube. Draw Sr^{2+} as ● and O^{2-} as ×.

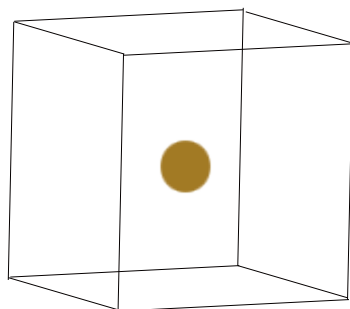


Figure 2. Unit cell of SrTiO₃ showing only Ti⁴⁺ at the center.

Most divalent metal oxides (MO) crystallize in a rock salt structure wherein M²⁺ occupies the octahedral voids created by O²⁻ (Figure 3).

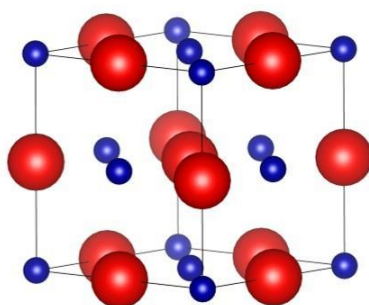


Figure 3. Unit cell of CaO. Blue and red spheres represent Ca²⁺ and O²⁻, respectively. (● Ca²⁺, ● O²⁻)

The thermodynamic properties of metal oxides can be discussed in terms of the standard molar enthalpy change (ΔH_{Lexp}) associated with the formation of gaseous ions from the ionic solid:



ΔH_{Lexp} is known as the lattice enthalpy; although it cannot be measured directly, it can be determined from enthalpy data (Table 1) using a Born–Haber cycle, which is a closed path of steps that includes lattice formation as one stage.

Table 1. Enthalpy changes of reactions involved in the Born–Haber cycle

Steps	Enthalpy change [kJ mol ⁻¹]
Sublimation of Ca(s): Ca(s) → Ca(g)	+193
Ionization of Ca(g) to Ca ⁺ (g): Ca(g) → Ca ⁺ (g) + e ⁻ (g)	+590
Ionization of Ca ⁺ (g) to Ca ²⁺ (g): Ca ⁺ (g) → Ca ²⁺ (g) + e ⁻ (g)	+1010
Dissociation of O ₂ : O ₂ (g) → 2 O(g)	+498
Electron gain by O(g): O(g) + e ⁻ (g) → O ⁻ (g)	-141
Electron gain by O ⁻ (g): O ⁻ (g) + e ⁻ (g) → O ²⁻ (g)	+878
Formation of CaO(s): Ca(s) + ½ O ₂ (g) → CaO(s)	-635

2-1. **Calculate** the ΔH_{Lexp} [kJ mol⁻¹] of CaO using the enthalpy data in Table 1 and the Born–Haber cycle.

The lattice enthalpy of an ionic crystal can be calculated theoretically (ΔH_{Lcalc}) from the sum of the Coulomb energies between the constituent ions as point charges. The Coulomb energy E between ions is expressed by the following equation:

$$E = \frac{1}{4\pi\epsilon_0} \frac{Z_1 Z_2 e^2}{r} \quad (2)$$

where ϵ_0 is the permittivity of the vacuum, e the elementary charge, Z_1 and Z_2 the charge numbers of the ions, and r the distance between the ions. E is attractive (*i.e.*, negative) between an anion and a cation, while E is repulsive (*i.e.*, positive) between two anions or two cations.

Ca^{2+} is surrounded by six O^{2-} in an octahedral arrangement (Figure 4).

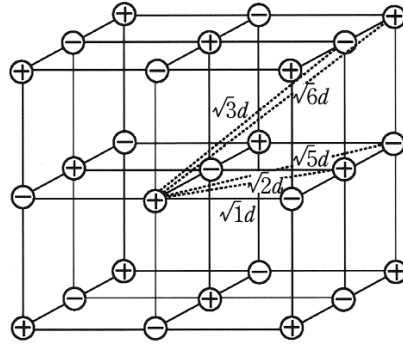


Figure 4. A unit cell of a rock salt structure to calculate the Madelung constant.

For a distance d between Ca^{2+} and O^{2-} in the rock salt structure depicted in Figure 4, the Coulomb energy (E_1) between a Ca^{2+} and six O^{2-} is formulated as follows:

$$\boxed{\phantom{E_1 = \frac{6}{4\pi\epsilon_0} \frac{Z^+ Z^- e^2}{d}}} \quad (3)$$

In the structure depicted in Figure 4, twelve Ca^{2+} are located at a distance of $\sqrt{2}d$ from a given Ca^{2+} . The Coulomb energy (E_2) between the Ca^{2+} and the twelve surrounding Ca^{2+} is formulated as follows:

$$\boxed{\phantom{E_2 = \frac{12}{4\pi\epsilon_0} \frac{Z^+ Z^+ e^2}{\sqrt{2}d}}} \quad (4)$$

Similarly, for any given Ca^{2+} , there are 8 O^{2-} , 6 Ca^{2+} , 24 O^{2-} , and 24 Ca^{2+} at distances of $\sqrt{3}d$, $\sqrt{4}d$, $\sqrt{5}d$, and $\sqrt{6}d$, respectively. The overall Coulomb energy E_{all} , obtained by the summation of E_n converges to the following equation:

$$E_{\text{all}} = \frac{N_A Z^+ Z^- e^2}{4\pi\epsilon_0 d} M \quad (5)$$

where Z^+ and Z^- are the charge numbers of the cation and anion, respectively; N_A is Avogadro's constant, and M is the Madelung constant, which is 1.748 for the rock salt structure. The theoretical lattice enthalpy ΔH_{Lcalc} is calculated using the Born–Mayer equation below, which takes into account the electron–electron and nucleus–nucleus repulsion of nearby ions:

$$\Delta H_{\text{Lcalc}} = \frac{N_{\text{A}}|Z^{+}Z^{-}|e^2}{4\pi\epsilon_0 d} \left(1 - \frac{d^*}{d}\right) M \quad (6)$$

where d^* is a constant (typically: 0.0345 nm).

2-2. **Fill in** the blanks (3) and (4) with the appropriate equations.

2-3. **Calculate** ΔH_{Lcalc} [kJ mol⁻¹] for CaO using equation (6); use $d = 0.240$ nm.

Problem 18. Coordination chemistry and its application to solid-state catalysts

Transition-metal complexes are formed by the coordination of ligands (*e.g.*, H_2O and NH_3) to transition metals or their ions. Most transition-metal complexes exhibit beautiful colors that cannot be explained by the classical theory of chemical bonding. Therefore, crystal-field theory has been developed; the repulsion between the d-electrons and the lone pairs of the ligands as negative point charges splits the energy of the five degenerate d-orbitals. Transition-metal complexes exhibit color because this energy separation and the corresponding transitions coincide with the energy of visible light.

Consider an octahedral transition-metal complex with the metal ion at the origin of a three-dimensional coordinate system and a total of six ligands as negative point charges equidistant from the origin on the x , y , and z axes (Figure 1a). The energies of the five degenerate d-orbitals are split into two groups called the e_g and t_{2g} orbitals, which are oriented along and between the axes, respectively.

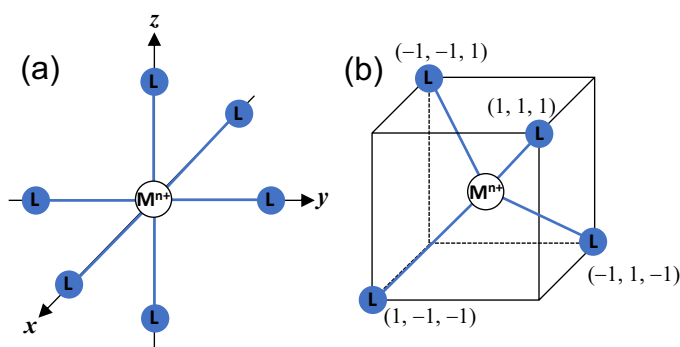


Figure 1. Arrangement of the metal ion (M^{n+}) and ligands (L) in (a) octahedral and (b) tetrahedral complexes. Blue solid lines represent the coordination bonds. The metal ion is located at the origin (0, 0, 0) of the three-dimensional coordinate system. The coordinates of the four ligands in the tetrahedral complex are indicated for clarity.

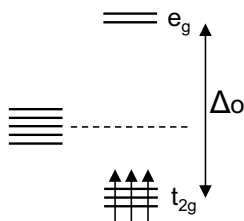
1. **Classify** the five d-orbitals into e_g and t_{2g} orbitals.

Let the energy separation between the e_g and t_{2g} orbitals (*i.e.*, the crystal-field splitting parameter) be Δ_O , where the subscript O signifies an octahedral arrangement. The barycenter of the energies of the e_g and t_{2g} orbitals is equal to the energy of the five degenerate d-orbitals.

2. **Write** the energies of the e_g and t_{2g} orbitals relative to the barycenter in units of Δ_O .

The energetically split d-orbitals, caused by the repulsion between the transition metal ion and the ligands, accommodate electrons according to Hund's rule. For example, Ti^{3+} with one d-electron (d^1) forms an octahedral complex $[\text{Ti}(\text{H}_2\text{O})_6]^{3+}$; this complex is energetically more stable than Ti^{3+} without ligands. This additional stability relative to the barycenter is known as the 'crystal field stabilization energy' (CFSE). The first through third d-electrons (d^1 to d^3) are exclusively accommodated in the t_{2g} orbitals. However, there are two possible ground-state electron configurations for d^4 to d^7 . Namely, Hund's rule applies when the CFSE is small, resulting in a 'high-spin' ground state with a large number of unpaired electrons. On the other hand, Hund's rule does not apply when the CFSE is large, resulting in a 'low-spin' ground state with a smaller number of unpaired electrons. In general, the CFSE depends on the type of ligands (*cf.* spectrochemical series).

3. **Draw** the high-spin electron configurations of octahedral complexes for d^4 - d^7 by referring to the electron configuration of d^3 shown below, and **calculate** each CFSE in units of Δ_O .



While six-coordinate octahedral complexes are the most common among the transition-metal complexes, four-coordinate complexes are also very frequently encountered. There are two types of four-coordinate complexes, tetrahedral and square planar complexes. Of these two, tetrahedral complexes have a lower steric repulsion between the ligands, and similarly to octahedral complexes, the energy splitting of their d-orbitals can be considered using crystal-field theory. In the tetrahedral crystal field (Figure 1b), the energy of the five degenerate d-orbitals is split into two sets of orbitals, e and t_2 orbitals.

4. **Draw** the energy separation between the e and t_2 orbitals with Δ_T as the crystal-field splitting parameter, where the subscript T signifies a tetrahedral arrangement. **Classify** the five d-orbitals into e and t_2 orbitals. **Write** the energies of e and t_2 orbitals relative to the barycenter in units of Δ_T .

When an aqueous solution containing the octahedral complex $[\text{Ti}(\text{H}_2\text{O})_6]^{3+}$ is irradiated with visible light, a d-electron is excited from the t_{2g} to the e_g orbital, which is accompanied by the absorption of green light ($\lambda = 500 \text{ nm}$). Consequently, the aqueous solution takes on a red-purple color, which is the complementary color of green.

5. **Calculate** the energy separation Δ_o (kJ mol^{-1}) between the e_g and t_{2g} orbitals in $[\text{Ti}(\text{H}_2\text{O})_6]^{3+}$.

Transition-metal complexes with carbon monoxide (CO) as a ligand are called metal carbonyls. Representative examples are the octahedral $\text{Cr}(\text{CO})_6$ and tetrahedral $\text{Ni}(\text{CO})_4$ complexes. The total number of electrons provided by the metal and ligands in a transition-metal complex is called the effective atomic number (EAN), and the 18-electron rule states that a complex is stable when the EAN is equal to the atomic number of noble gases. For instance, Cr and the CO ligands in $\text{Cr}(\text{CO})_6$ supply 6 and $2 \times 6 = 12$ electrons, respectively; similarly, Ni and the CO ligands in $\text{Ni}(\text{CO})_4$ supply 10 and $2 \times 4 = 8$ electrons, respectively, satisfying the 18-electron rule for each metal carbonyl. In addition to mononuclear metal carbonyls with one metal atom, there are also multinuclear metal carbonyls with multiple metal atoms and metal–metal bonds.

6. **Draw** the molecular structure of $\text{Mn}_2(\text{CO})_{10}$ and $\text{Ir}_4(\text{CO})_{12}$ and show that the EAN per metal atom is 18.

The coordination bonds formed between carbon monoxide (CO) and metals can be used to estimate the size of metal nanoparticles loaded on catalyst support such as Al_2O_3 . Figure 2a shows a schematic illustration of a platinum catalyst supported on alumina ($\text{Pt}/\text{Al}_2\text{O}_3$), which is used as an automotive catalyst.

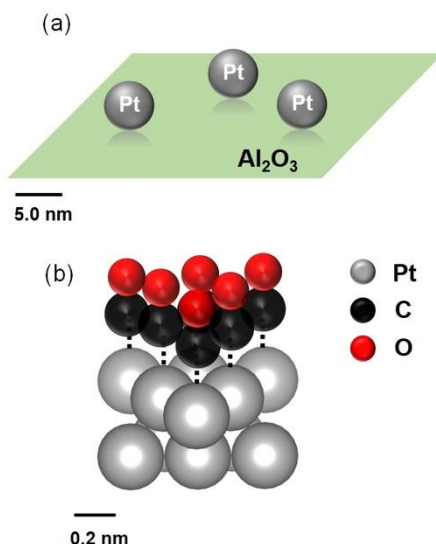


Figure 2. Schematic illustrations of (a) the $\text{Pt}/\text{Al}_2\text{O}_3$ catalyst and (b) the CO molecules adsorbed on the Pt surface. The Pt metal particles in (a) are the same size.

1.0 g of $\text{Pt}/\text{Al}_2\text{O}_3$ catalyst that contains 0.010 g of Pt metal is prepared. Upon exposure to CO gas, 0.55 mL (1.0 bar, 273 K) of CO was adsorbed per 1.0 g of catalyst. The Pt metal particles on Al_2O_3 are spherical, and their surfaces can be regarded as being covered with Pt atoms without gaps. As shown in Figure 2b, one CO molecule coordinates to one Pt atom exposed on the surface. The density of the Pt metal is 21.45 g cm^{-3} , and the area occupied by each Pt atom is $8.0 \times 10^{-2} \text{ nm}^2$.

7. Answer the following questions.

7-1. **Calculate** the ratio [%] of Pt atoms exposed on the surface to the total number of Pt atoms in the spherical Pt metal particles.

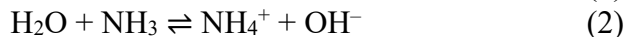
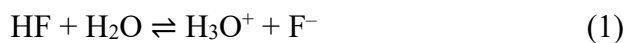
7-2. **Calculate** the number of CO molecules adsorbed per 1.0 g of Pt metal dispersed on the Al_2O_3 support.

7-3. **Calculate** the surface area [m^2] per 1.0 g of Pt metal.

7-4. **Calculate** the diameter of the Pt metal particles.

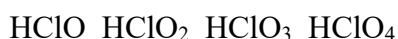
Problem 19. Acids and bases

In 1923, Brønsted and Lowry defined an acid–base reaction as the transfer of a proton (H^+) from the proton donor (acid) to the proton acceptor (base).



Hydrogen fluoride (HF) is an example of a Brønsted acid, ammonia (NH_3) is an example of a Brønsted base, while water (H_2O) is amphoteric, *i.e.*, it can behave as both a Brønsted acid and a Brønsted base. When acid–base reactions are in chemical equilibrium, the reactions are indicated by two one-sided arrows as in (1) and (2). When HF donates a proton to H_2O , F^- and H_3O^+ are formed as the conjugate base and conjugate acid, respectively. Brønsted acidity can be evaluated quantitatively using the acidity constant, or qualitatively using the (a) stability of the conjugated base.

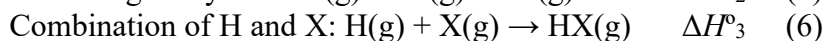
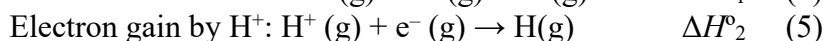
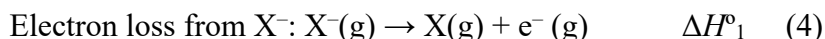
1. **Arrange** the following Brønsted acids in order of increasing acidity by referring to the underlined part (a).



The Brønsted acidity of hydrogen halides (HX , $\text{X} = \text{F}, \text{Cl}, \text{Br}, \text{I}$) can be evaluated by the standard enthalpy change ($\Delta H^\circ_{\text{HX}}$) of the protonation reaction of their conjugate bases (X^-):



This reaction can be divided into three steps:



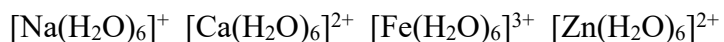
Therefore, $\Delta H^\circ_{\text{HX}}$ is calculated as $\Delta H^\circ_{\text{HX}} = \Delta H^\circ_1 + \Delta H^\circ_2 + \Delta H^\circ_3$.

2. **Calculate** the absolute value of $\Delta H^\circ_{\text{HF}}$ ($|\Delta H^\circ_{\text{HF}}|$ in kJ mol^{-1}) by drawing a thermodynamic cycle for the protonation reaction of F^- . Use the following values if necessary:
H–F bond dissociation enthalpy: 567 kJ mol^{-1} ; ionization enthalpy of hydrogen: 1312 kJ mol^{-1} ; enthalpy of electron gain by fluorine: -328 kJ mol^{-1} .
3. **Calculate** the absolute value of $\Delta H^\circ_{\text{HI}}$ ($|\Delta H^\circ_{\text{HI}}|$ in kJ mol^{-1}) by drawing a thermodynamic cycle for the protonation reaction of I^- . Use the following values if necessary:
H–I bond dissociation enthalpy: 298 kJ mol^{-1} ; enthalpy of electron gain by iodine: -295 kJ mol^{-1} .
4. According to Q2 and Q3, $|\Delta H^\circ_{\text{HI}}|$ (a) $|\Delta H^\circ_{\text{HF}}|$; therefore, the Brønsted acidity of hydrogen halides is arranged in the following order, HF (b) HCl (b) HBr (b) HI. **Choose** which inequality sign, ‘>’ or ‘<’, should be placed in blanks a and b.

Metal ions are hydrated in aqueous solutions, and generally, the first hydration shell of metal ions consists of six water molecules. When the oxygen atom of a water molecule is strongly coordinated to a metal ion, the coordinated water acts as a proton donor as shown in (7).

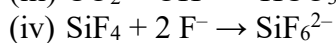
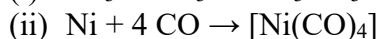


5. **Arrange** the following aqua acids in order of increasing acidity.



Lewis introduced a more general concept of acids and bases, which includes reactions that do not involve protons. Lewis defined an acid–base reaction as the transfer of an electron pair from the electron-pair donor (Lewis base) to the electron-pair acceptor (Lewis acid). Note that the Brønsted acid HA is a complex formed by the Lewis acid H^+ with the Lewis base A^- . All Brønsted acids and Brønsted bases exhibit Lewis acidity and Lewis basicity, respectively.

6. **Identify** the Lewis acids and bases in each of the following reactions.



7. Phosphoric acid (H_3PO_4) and boric acid (H_3BO_3) are both acids with three hydrogens. While phosphoric acid reacts as a triprotic Brønsted acid, boric acid reacts as a monoprotic acid. **Draw** the Lewis structure of the conjugate base of boric acid by considering the reaction with water.

Problem 20. Semiconductors

In molecules that exist as gases or liquids, the molecular orbitals are formed by the overlap between the atomic orbitals of individual atoms. In contrast, in the electronic state of a solid composed of an infinite number of atoms, many atomic orbitals are overlapping; therefore, many molecular orbitals with close energy levels are formed. As the gap between their energy levels is very narrow, these orbitals are for practical reasons represented as an energy band. Insulators have a wide energy gap between the valence band (VB), which is completely filled with electrons, and the conduction band (CB), which does not contain electrons (Figure 1).

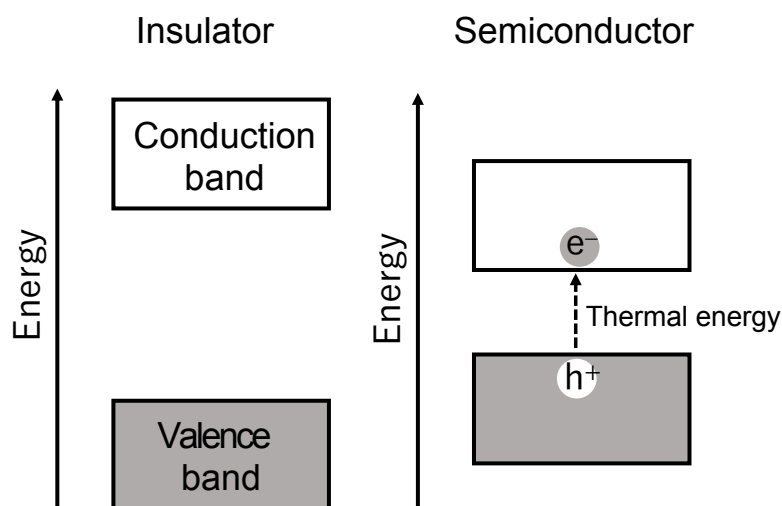


Figure 1. Schematic view of the electronic band structure in solid-state materials.

In insulators, the electrons are bound within the VB. On the other hand, in semiconductors, some electrons (e^-) in the VB can be transferred to the CB by thermal energy, as the energy gap between the VB and CB is relatively small. An electron transition in a semiconductor creates a hole in the VB; this hole behaves like a positively charged particle. The hole is commonly referred to as h^+ . The electrons and holes formed in the semiconductor can move, which results in electrical conductivity.

1. With reference to Figure 1, **illustrate** the band structure of a metallic conductor, which shows electrical conductivity even when the temperature is lowered.

Semiconductors are classified as either intrinsic or extrinsic semiconductors. An intrinsic semiconductor is composed of a pure material, and the same number of electrons and holes are produced by thermal energy and other factors. The electrical conductivity is not very high. On the other hand, there are two types of extrinsic semiconductors, n-type and p-type, whose electrical conductivity is generally higher than that of intrinsic semiconductors. In n-type semiconductors, small amounts of electrons are added to a pure material (electron doping), while in p-type semiconductors, small amounts of holes are added to a pure material (hole doping). For example, adding a small amount of P to pure Si, a typical intrinsic semiconductor, results in the doping of an extra electron (Figure 2). Accordingly, P-doped Si exhibits n-type semiconductor properties.

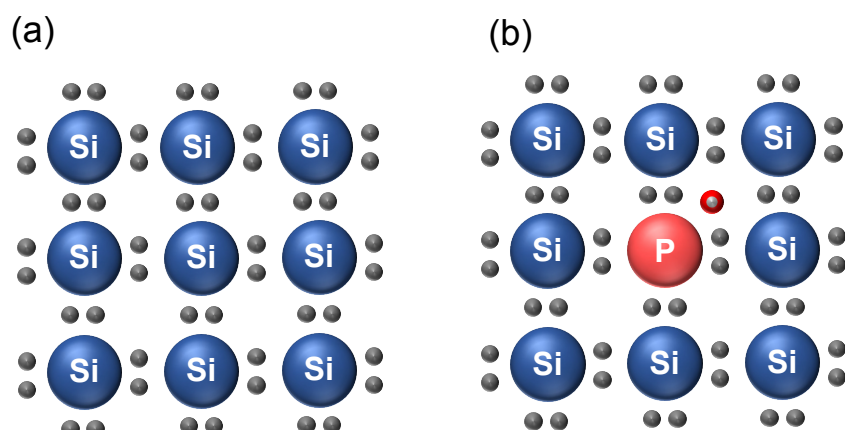


Figure 2. Schematic view for electron states of (a) Si and (b) P-doped Si.

2. **Indicate** which elements in the following list could be used to produce p-type semiconductor properties in Si.

Ga, Ge, As, B

TiO₂, a representative oxide semiconductor, is capable of inducing the water-splitting reaction at room temperature using light energy as a driving force. The water-splitting reaction, which generates hydrogen (H₂) from water, is expected to be a significant source of renewable energy in the near future. The discovery of the following phenomena is one reason for the development of photocatalysts such as TiO₂. (1) The electrolysis of water occurs when a voltage is applied. In contrast, (2) when TiO₂ and platinum electrodes are arranged as shown in Figure 3 and the TiO₂ side is exposed to light irradiation, oxygen and hydrogen are generated from each electrode. This phenomenon is called the Honda–Fujishima effect and was discovered in 1972. Electrons and holes are produced by irradiating TiO₂ with light, which leads to the reduction and oxidation of water, respectively.

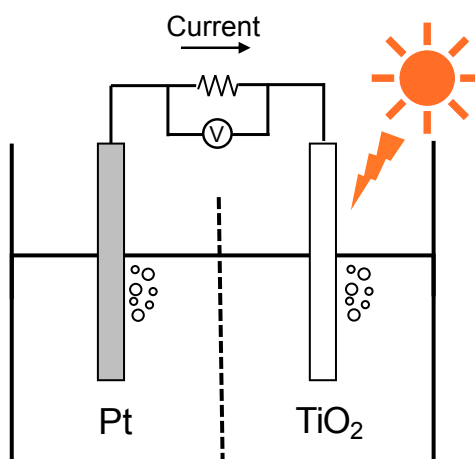


Figure 3. Schematic illustration of the photoelectrochemical water-splitting reaction.

- 3-1. When TiO₂ is subjected to a thermal treatment under an H₂ flow, it exhibits n-type semiconductor properties. **Explain** the reasons for this phenomenon.
- 3-2. Regarding the underlined part in (1), **calculate** the voltage at which water can be thermodynamically electrolyzed. The standard Gibbs energy change for the splitting of 1 mole of water is 237 kJ.

3-3. **Write** the half-reaction equation including the hole (h^+) for the gas-evolution reaction on TiO_2 described in the underlined part in (2). When TiO_2 is exposed to light irradiation, a current is observed in the direction shown in Figure 3.

3-4. **Choose** the option below that best represents the maximum percentage of the photon number in sunlight that is available for water-splitting reactions on TiO_2 . The band gap of TiO_2 between the VB maximum and the CB minimum is 3.0 eV. Figure 4 shows the solar spectrum, and the calculation of the photon number here does not take into account sunlight below 300 nm and above 800 nm.

- (a) <1.0 % (b) 1–10 % (c) 10–20 % (d) 20–30 %

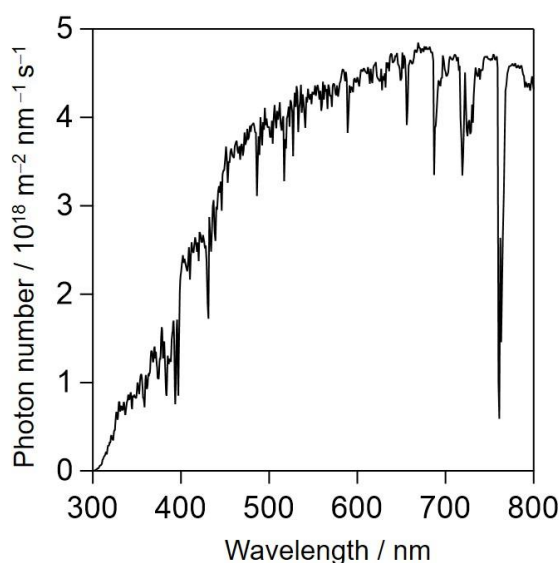
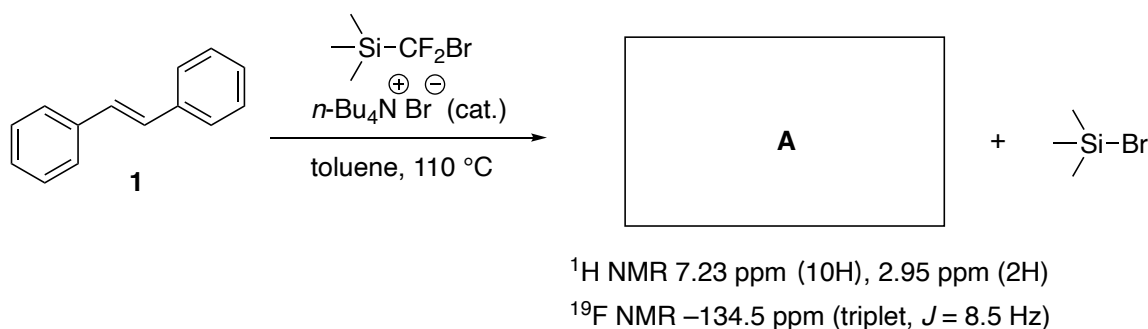


Figure 4. Photon number vs wavelength in sunlight.

3-5. The ratio of the number of carriers (electrons or holes) consumed in the water-splitting reaction to the number of irradiated photons is called quantum efficiency. When TiO_2 is irradiated with 1.00 W of light with a wavelength of 350 nm, 5.00 μmol of hydrogen are produced in 100 seconds. **Calculate** the quantum efficiency [%].

Problem 21. Carbenes and non-benzenoid aromatic compounds

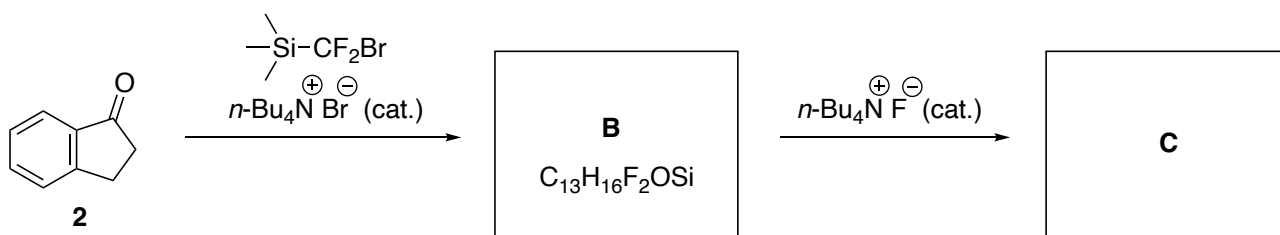
The following problems describe the highly unusual and interesting reactivity of carbenes.



Under the conditions described above, olefin **1** is converted into **A**, which does not contain a double bond.

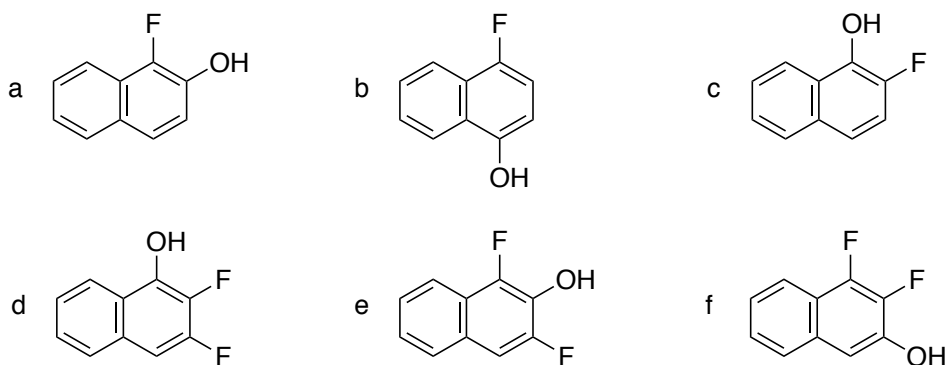
1. **Draw** the structure of **A**.

Under similar reaction conditions, tautomer of ketone **2** is converted into **B**, which is subsequently transformed into **C** in the presence of a fluoride ion.



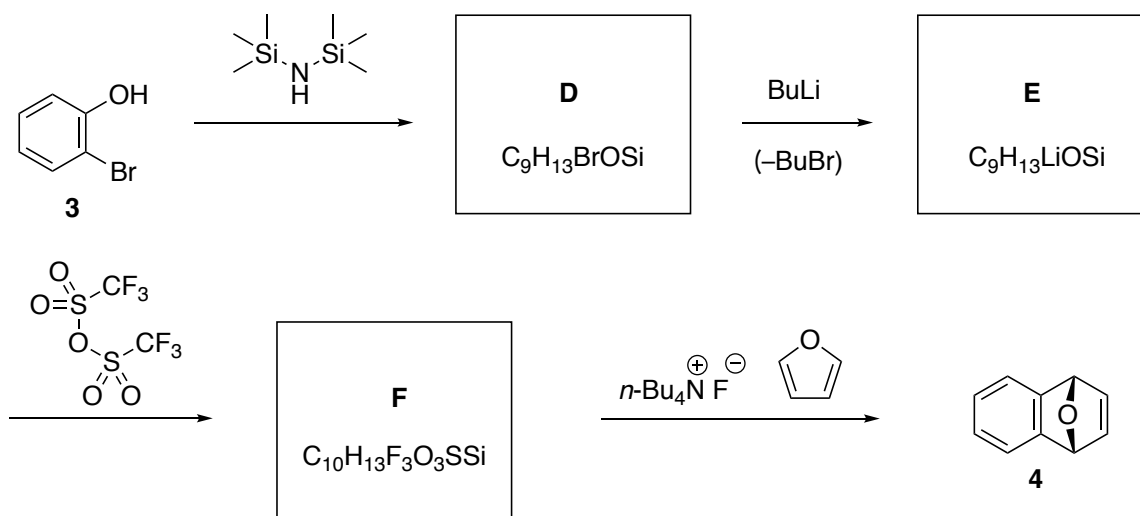
2. **Draw** the structure of **B**.

3. **Choose** all possible structures for **C**.



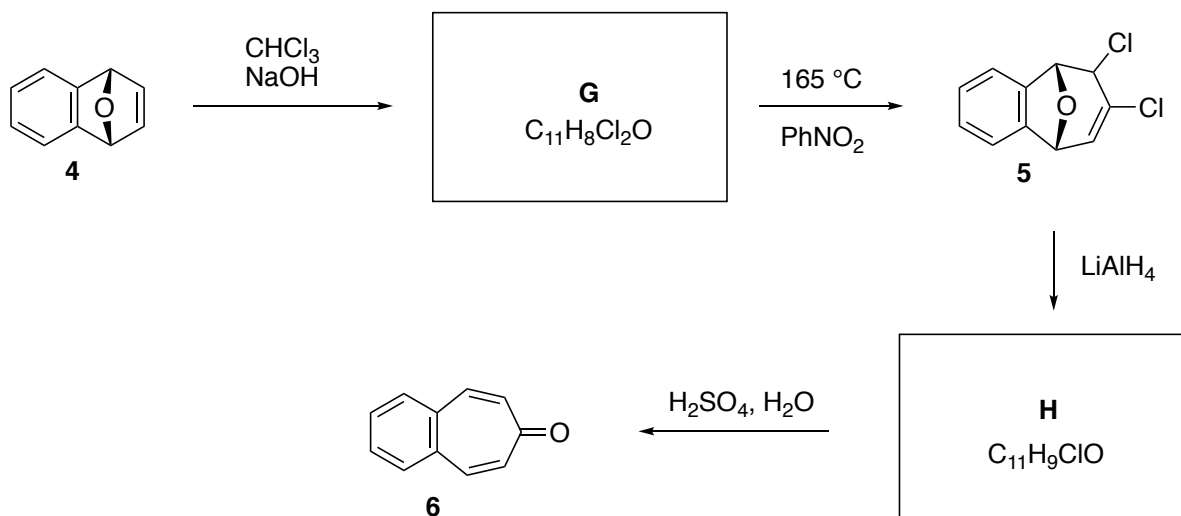
Silicon exhibits an extremely high affinity toward oxygen and especially fluorine. An application that capitalizes on this reactivity is the formation of benzyne species.

4. A four-step transformation converts **3** into **4**. **Draw** the structures of **D–F**.



In another four steps, **4** is converted into **6**, which bears a cycloheptatrienone moiety. The structure of **G** contains one more cyclic moiety than the structure of **4**.

5. **Draw** the structure of **G** (while the stereochemistry is important for the reaction, it is not the focus of this question).



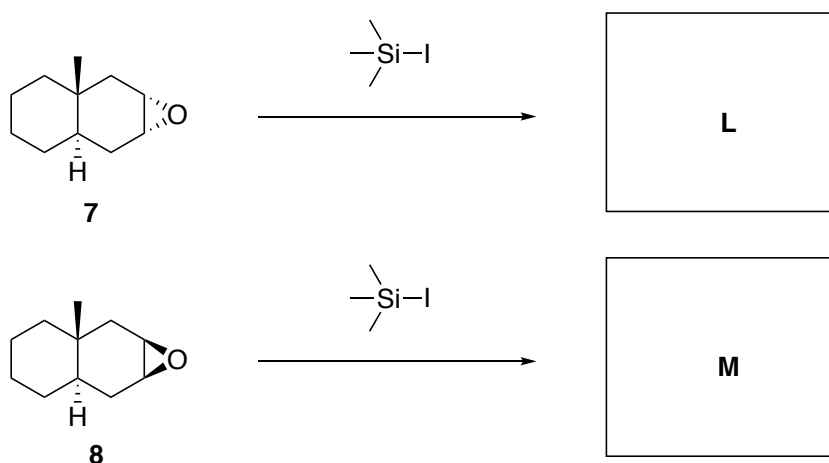
6. **Draw** the structure of **H**.

Subsequently, **6** is converted into **I** by exploiting the unique aromaticity of cycloheptatriene cations. When **I** is treated with the Grignard reagent MeMgI, a mixture of **J** and **K** is obtained. Treating **I** with catalytic amount of HCl in CCl₄ furnishes isomer **I'**, which is again converted into a mixture of **J** and **K** upon treatment with Lewis-acidic Grignard reagents.



7. **Draw** the structures of **I**, **J**, **K**.

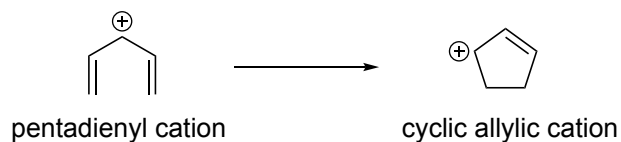
The ring-opening of the epoxide moiety on the six-membered ring occurs so that both the introduced functional group and the hydroxy leaving group adopt axial positions. Epoxides **7** and **8** both react with trimethylsilyl iodide, but afford different products.



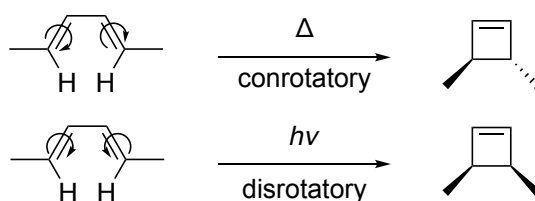
8. **Draw** the structures of **L** and **M**.

Problem 22. Nazarov cyclization

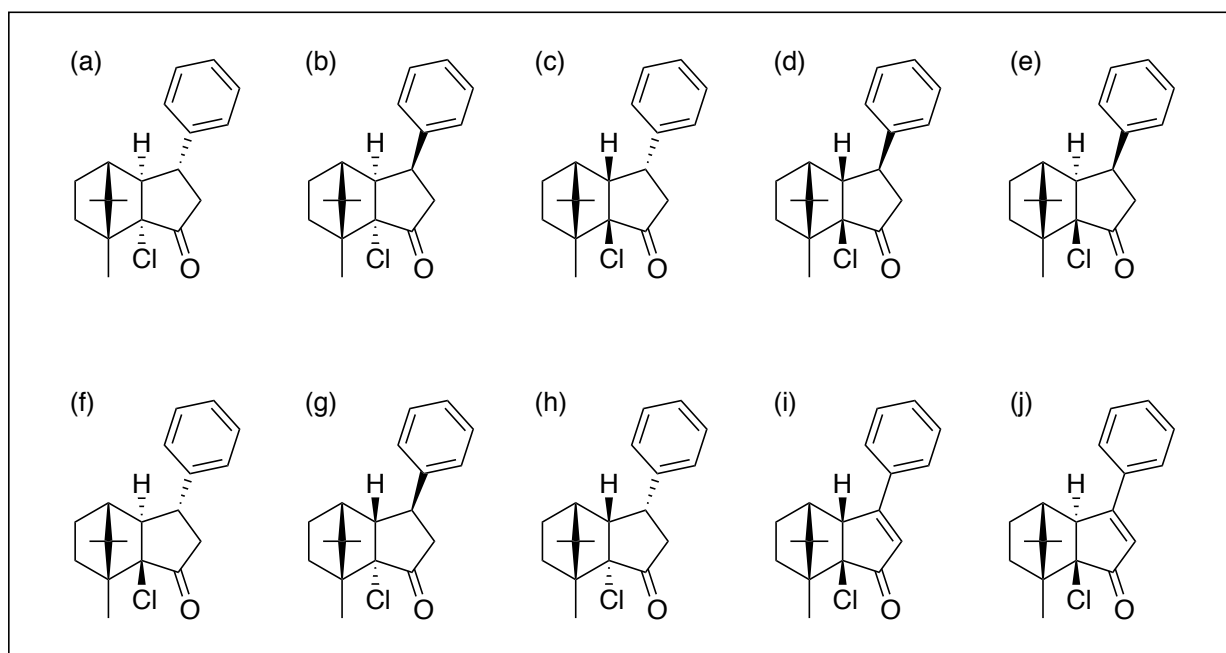
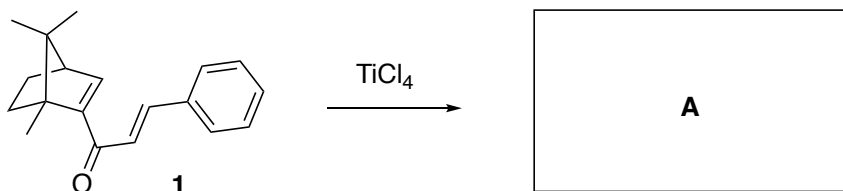
The formation of five-membered rings is a very important class of organic transformations. Answer the following questions regarding one of those interesting reactions, the so-called ‘Nazarov cyclization’.



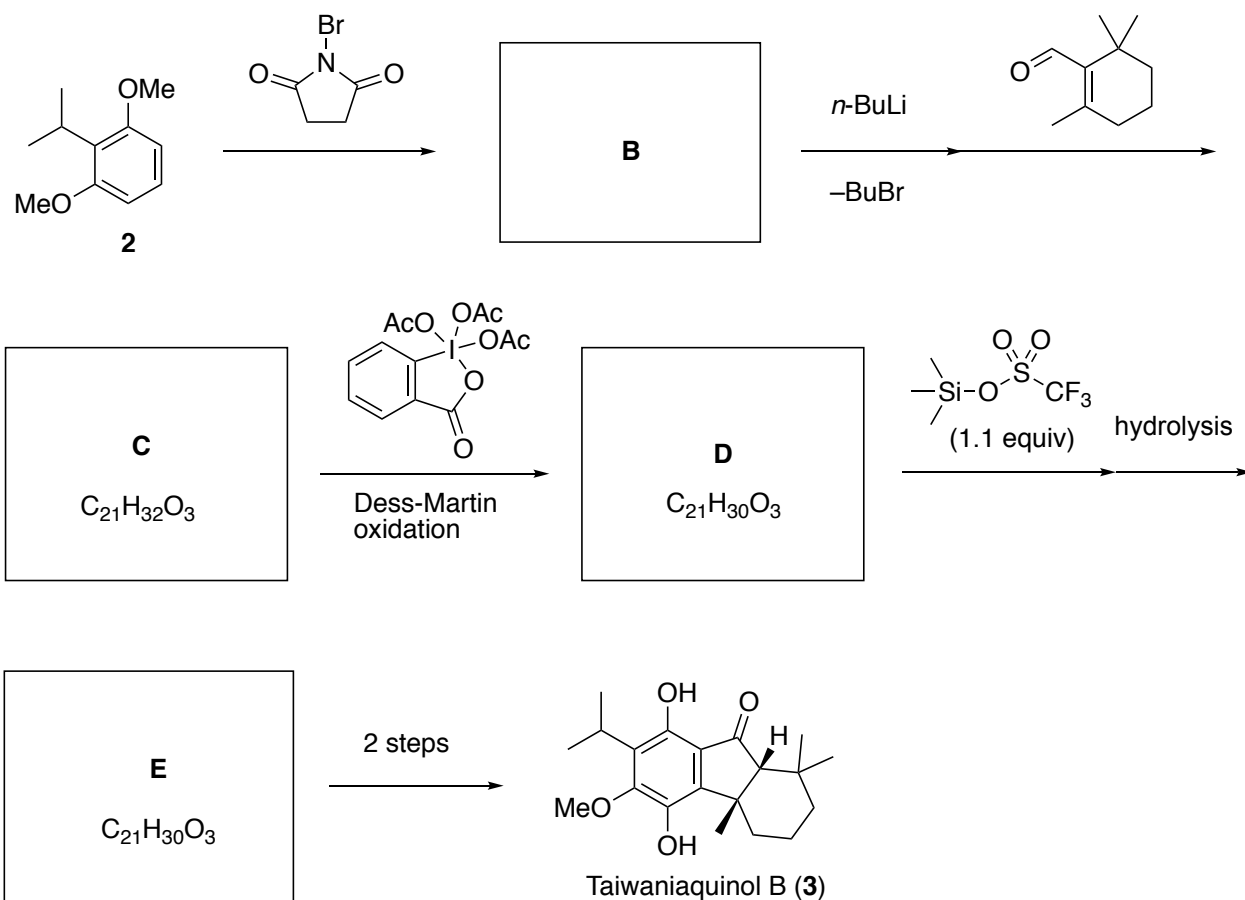
In general, 4π -electrocyclization reactions proceed via one of two cyclization modes. Conrotatory cyclization occurs under thermal transformation conditions, while disrotatory cyclization occurs upon photoirradiating the substrate.



1. Titanium tetrachloride (TiCl_4) is a Lewis acid that can activate the carbonyl group in **1**. The resulting pentadienyl cation intermediate is transformed via a conrotatory Nazarov cyclization. The resulting cation intermediate is then trapped with chloride to give **A**. **Choose** all possible structures of **A**.

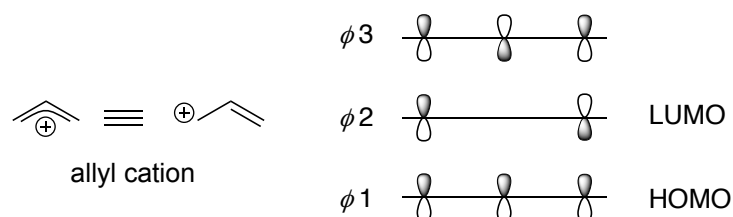


2. Compound **2** is transformed into Taiwanaiquinol (**3**) using a Nazarov cyclization as a key step. **Draw** the structures of **B**, **C**, **D**, **E**.



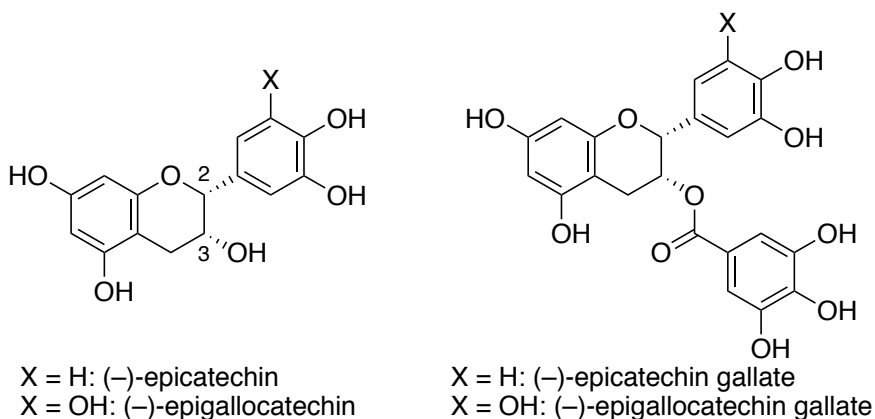
Optional problem:

The frontier molecular orbitals of the allyl cation, which consist of three carbon atoms and one π orbital shown below. The lowest unoccupied molecular orbital (LUMO) and the highest occupied molecular orbital (HOMO) are labeled in this figure. **Draw** the molecular orbitals of the pentadienyl cation using the same style as given in the example and **label** the LUMO and HOMO orbitals.



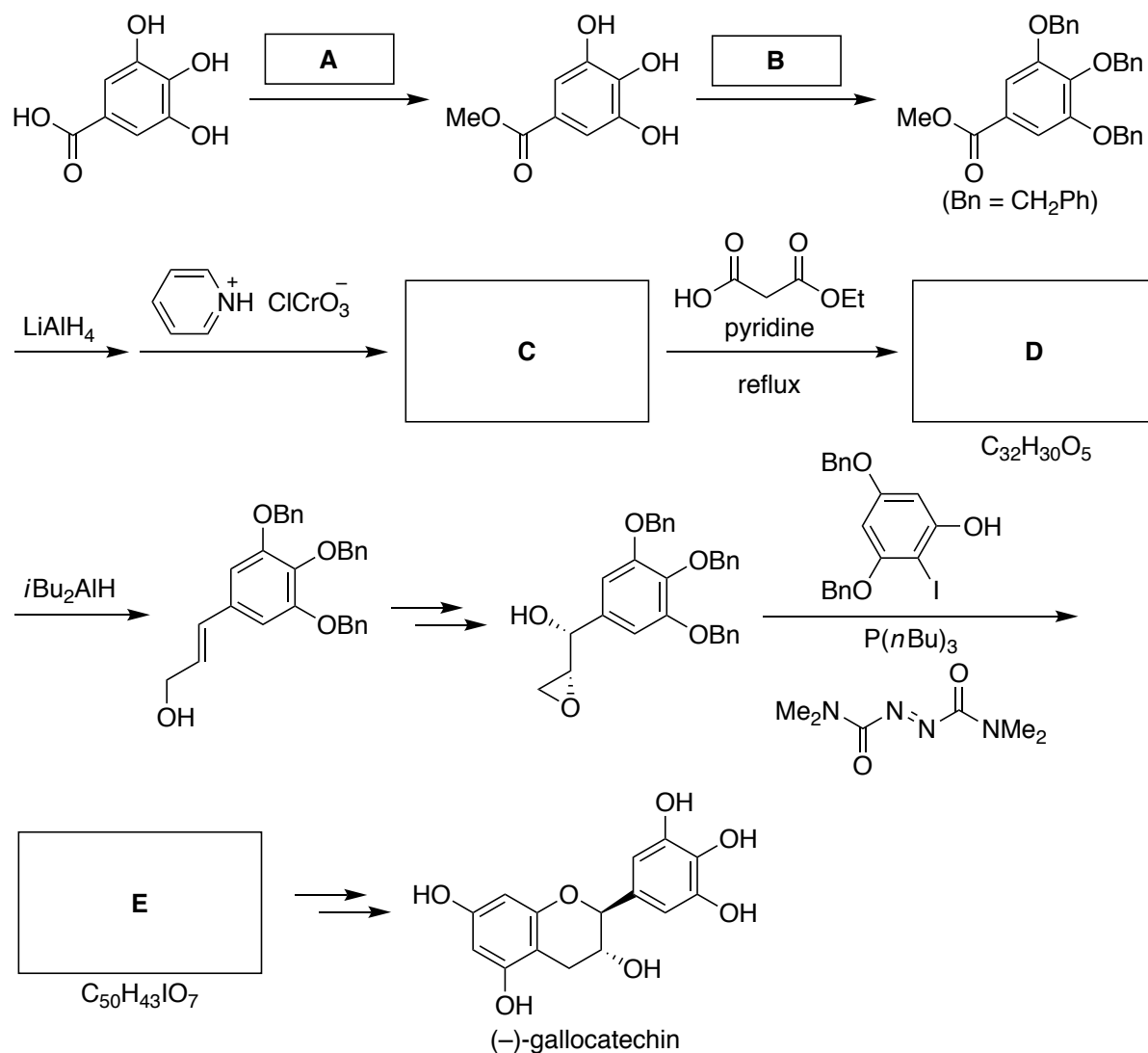
Problem 23. Tea party

In Japan, the cultivation of tea leaves and the green-tea culture started in the early 1200s. This culture has grown and developed ever since into the current form of the traditional ‘tea ceremony’, during which matcha is prepared and drunk. Moreover, regular green tea for daily consumption has become a staple of Japanese diet. Catechins, which are responsible for the characteristic taste of green tea, have been associated with a variety of health benefits. Tea leaves contain several catechins such as epicatechin, epigallocatechin, epicatechin gallate, and epigallocatechin gallate. Green tea also contains caffeine, which is bitter, and theanine, which adds a savory (umami) flavor.



1. **Assign** the absolute configuration of the stereocenters at the 2- and 3-positions of (–)-epicatechin using the *R/S* nomenclature.

The following scheme shows a synthetic route to (–)-gallocatechin, which is an epimer of (–)-epigallocatechin.



2. From the following conditions, **choose** the best for **A**.

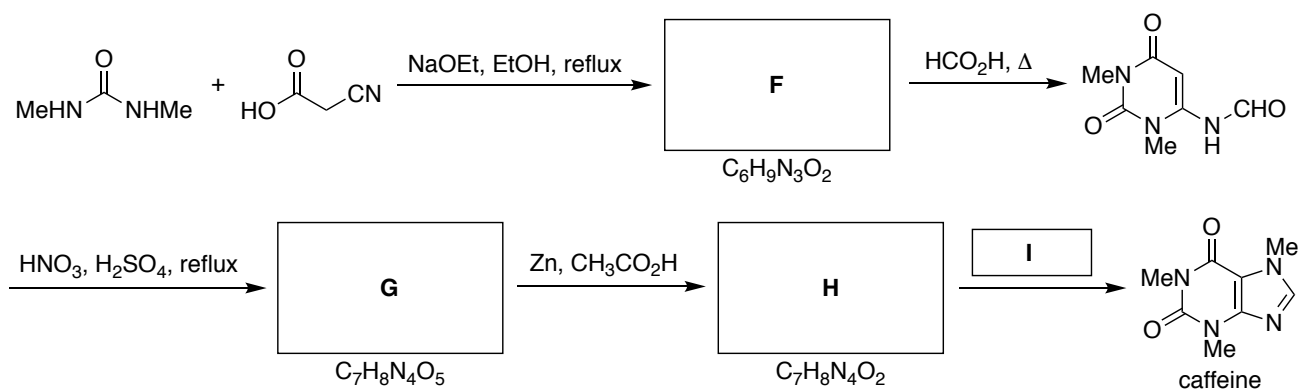
- ☐ MeMgBr , THF
- ☐ NaOMe , THF
- ☐ NaBH_4 , MeOH
- ☐ HCl , MeOH

3. From the following conditions, **choose** the best for **B**.

- ☐ PhCH₂OH, NaH
 - ☐ PhCH₂Cl, NaH
 - ☐ PhCHO, HCl
 - ☐ PhCO₂H, HCl

4. **Draw** the structures of **C–E** and clearly identify the stereochemistry where necessary.

Caffeine, which is responsible for the bitter taste of green tea, can be synthesized as follows.

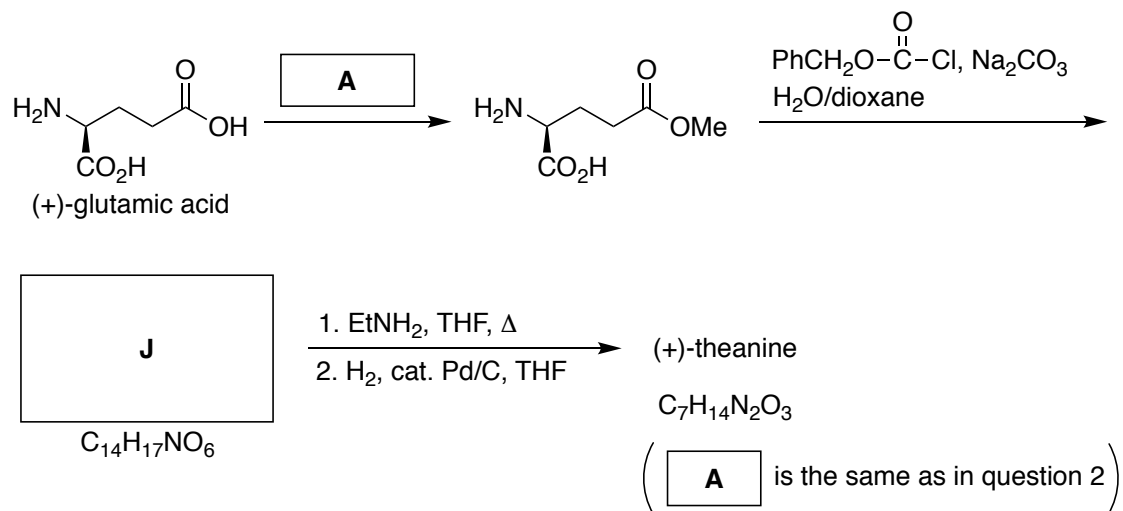


5. **Draw** the structures of **F–H**.

6. From the following conditions, **choose** the best for **I**.

- ☐ 1) NaH, 2) MeI
 - ☐ 1) MeMgBr, 2) H₂O
 - ☐ NaOMe, MeOH
 - ☐ NMe₃, H₂O

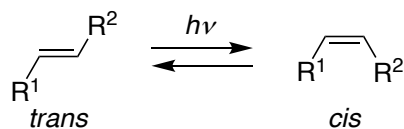
(+)-Theanine, which is responsible for the savory (umami) taste of green tea, can be synthesized from (+)-glutamic acid as follows.



7. **Draw** the structures of **J** and (+)-theanine and clearly identify the stereochemistry where necessary.

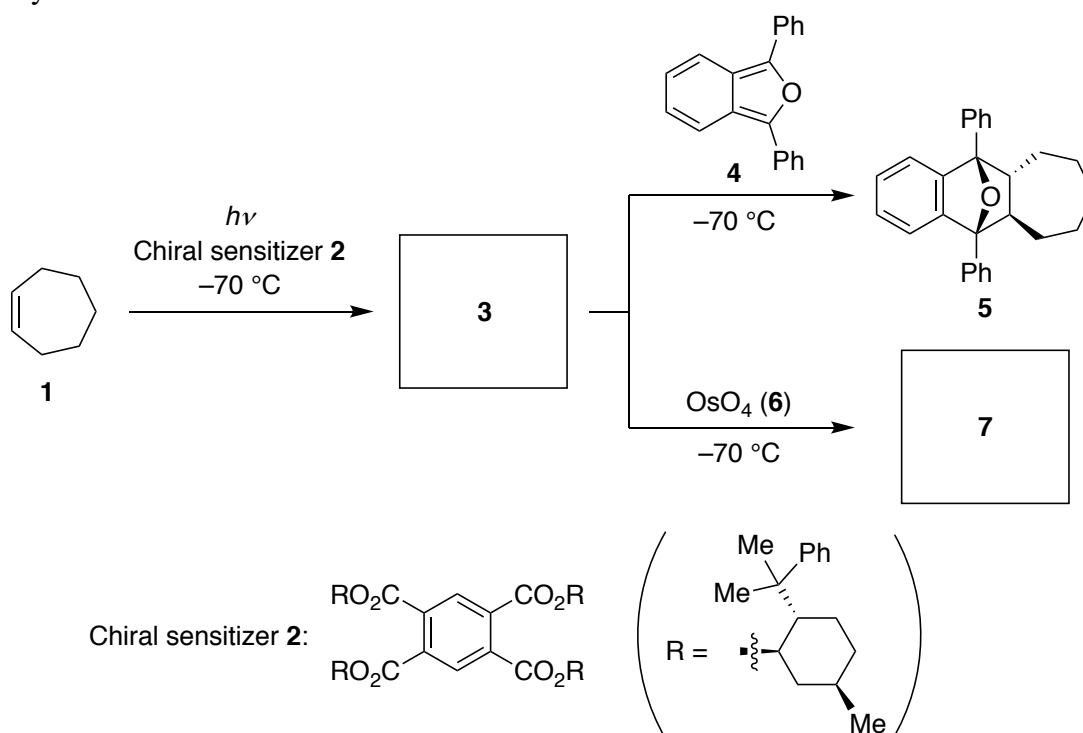
Problem 24. *E-Z* chemistry

Alkenes can undergo *trans/cis* isomerization upon photoirradiation as shown below, and the isomerization process can be accelerated by adding a sensitizer that is excited upon absorption of light and subsequently transfers this energy to the alkenes.



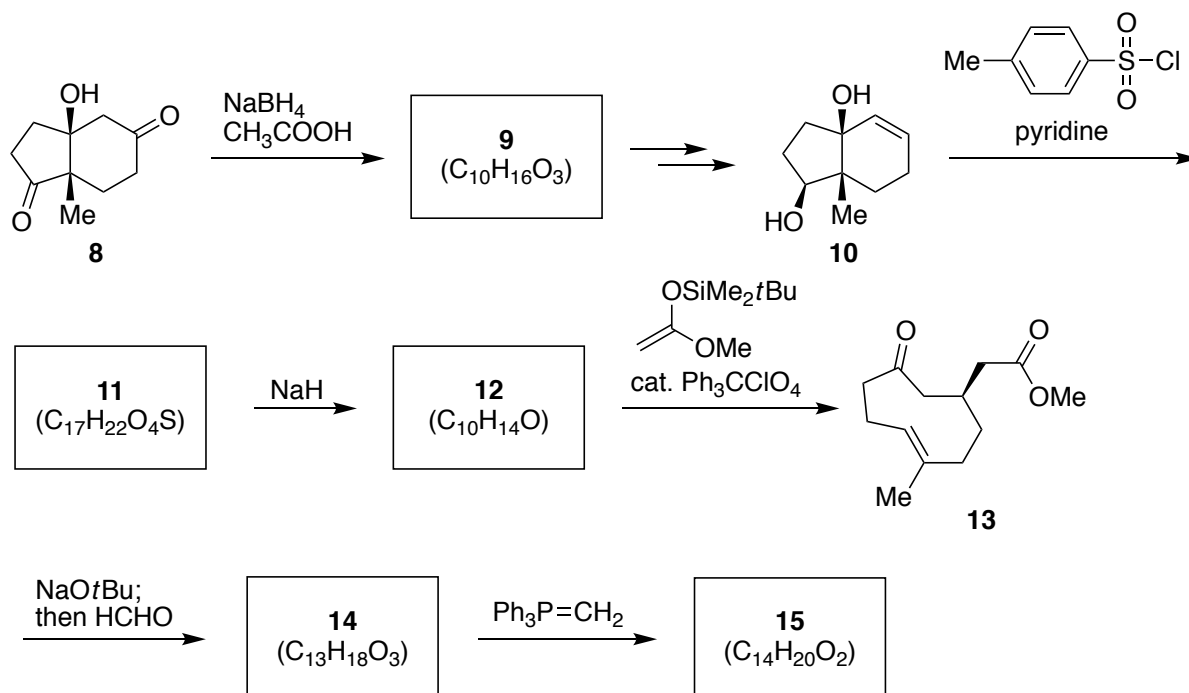
This photo-induced *trans/cis* isomerization also occurs in certain cycloalkenes, which contain connected substituents R^1 and R^2 . In general, *trans*-cycloalkenes that contain a 7- to 9-membered ring are highly reactive due to their intrinsic ring strain. Their two faces of the π -plane can be distinguished by the reactivity, as one face is blocked by the carbon chain within the ring, while the other unblocked face can engage selectively in chemical reactions.

Moreover, asymmetric syntheses can be achieved by exposing cycloalkenes to irradiation in the presence of a chiral sensitizer. For instance, as shown in the scheme below, photoirradiation of cycloheptene (**1**) at low temperature in the presence of chiral sensitizer **2** generates **3**, which undergoes a Diels–Alder reaction with 1,3-diphenylisobenzofuran (**4**) to enantioselectively afford optically active **5**. Under the same photoirradiation conditions, the reaction of **3** with OsO_4 (**6**) results in the formation of optically active **7**.

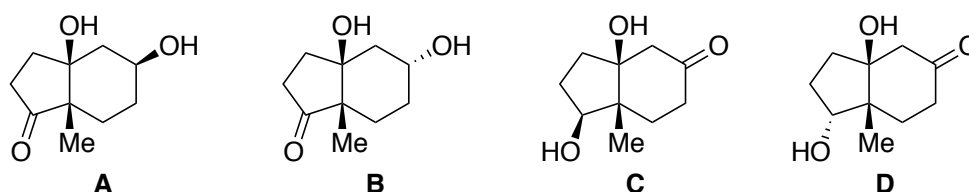


1. **Draw** the structures of **3** and **7** and clearly identify the stereochemistry where necessary.

The naturally occurring compound Coraxeniolide is a bicyclic compound that contains fused 9- and 6-membered rings. A synthetic route to Coraxeniolide precursor **15** is shown below, starting from **8** via cycloalkene derivative **12**.



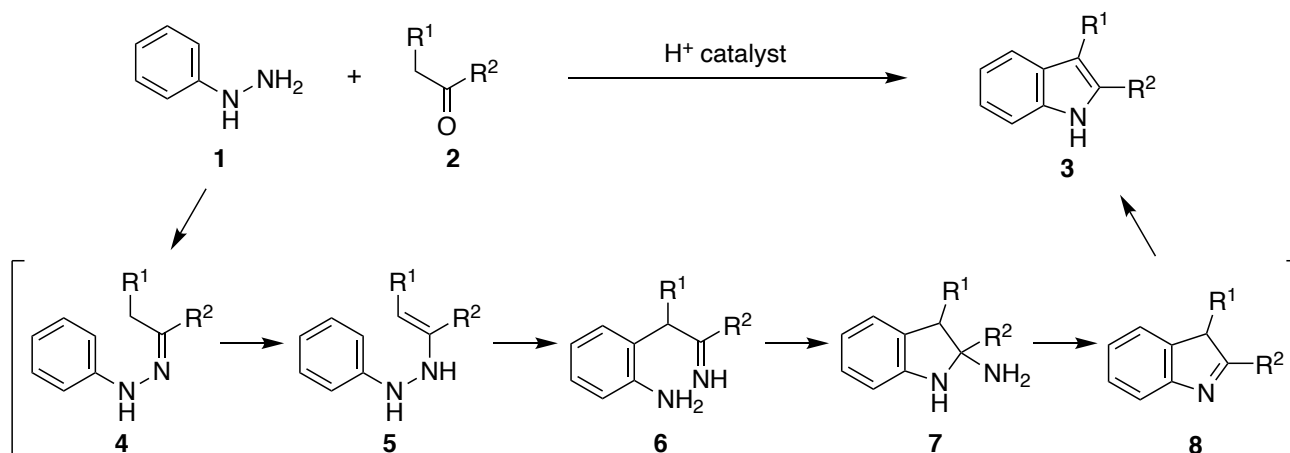
2. A nucleophilic addition to a carbonyl group does not occur easily when the carbonyl group is connected to a bulky substituent. When the two faces of the carbonyl group can be differentiated by the bicyclic structure as in **8**, the addition of the nucleophile usually occurs selectively from the outer face of the core structure. Based on these general considerations, **choose** the most suitable structure for **9** from A–D.



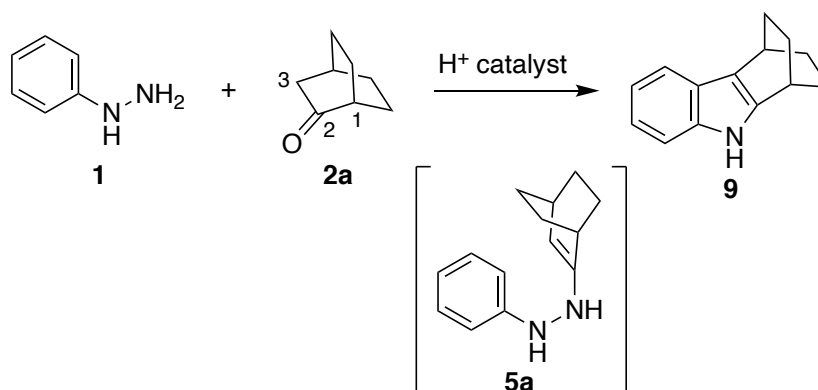
3. The nucleophilicity of the hydroxy group in alcohols generally increases with decreasing size of the associated alkyl group. **Draw** the structure of **11** and clearly identify the stereochemistry where necessary.
4. Compound **12** is a chiral compound although it does not possess a carbon stereocenter. **Draw** the structure of **12** and clearly identify the stereochemistry where necessary.
5. **Draw** the structures of **14** and **15** and clearly identify the stereochemistry where necessary.

Problem 25. Fischer indole synthesis

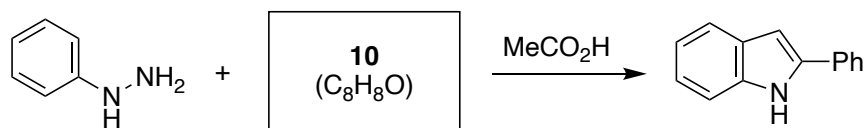
The reaction of phenylhydrazine **1** and carbonyl compound **2** under acid catalysis to give indole **3** via **4–8** is known as the Fischer indole synthesis.



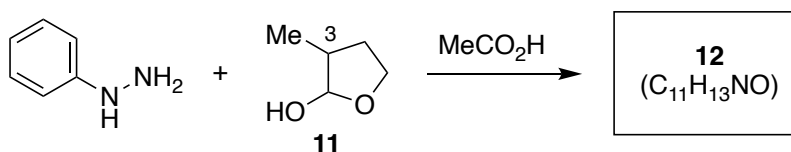
When bicyclic ketone **2a** is used as the carbonyl compound, indole **9** is obtained selectively via intermediate **5a**, wherein a carbon–carbon double bond is formed between C2 and C3 in order to avoid the formation of a highly strained carbon–carbon double bond between bridge-head C1 and C2.



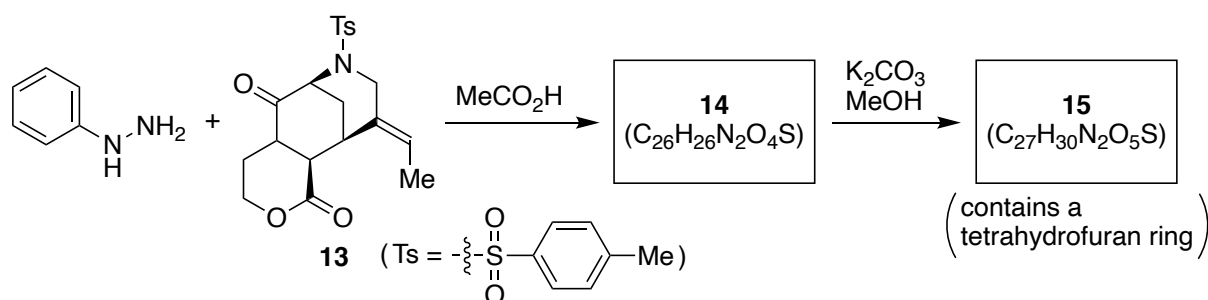
- Draw** the structure of compound **10** in the following reaction.



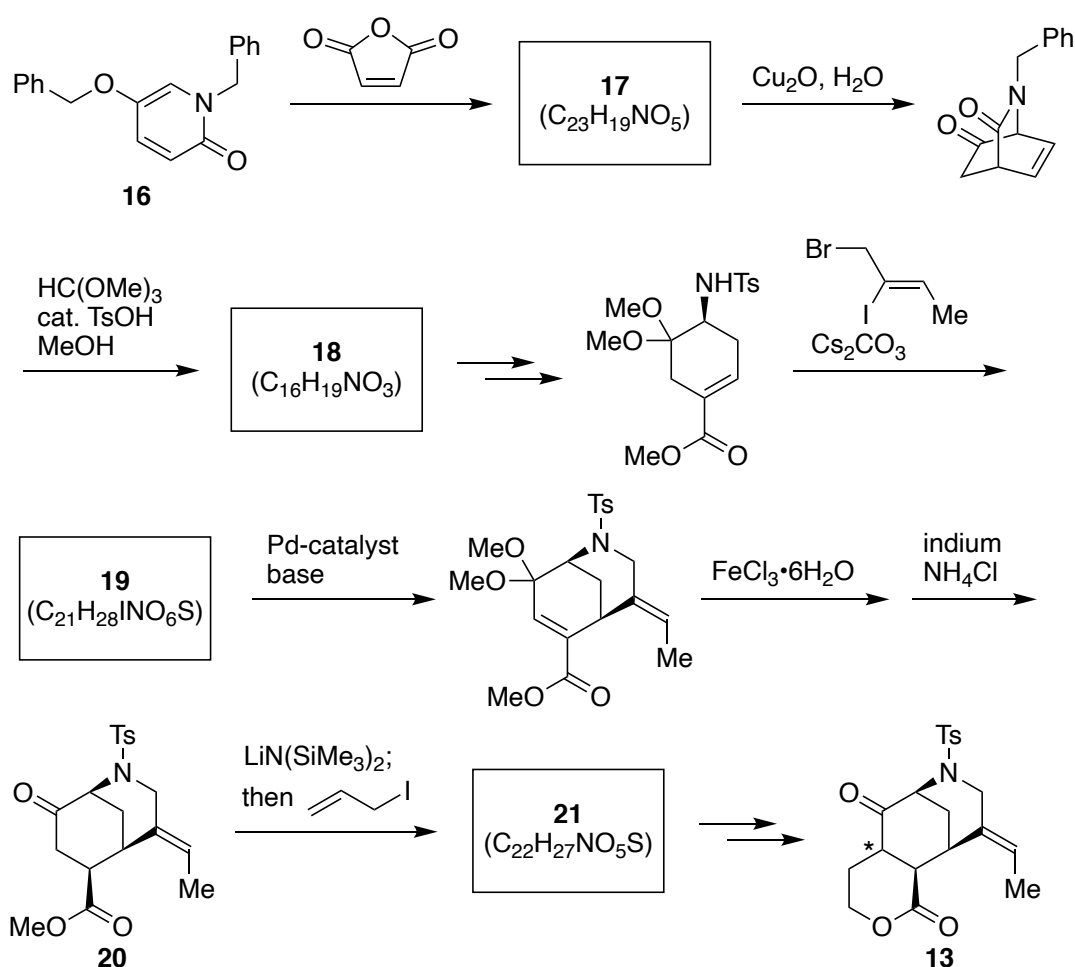
- In the following reaction, tricyclic **12** is produced instead of an indole due to the substituent at the 3-position of **11**. **Draw** the structure of **12**.



3. **Draw** the structures of **14** and **15** in the following scheme and clearly identify the stereochemistry where necessary.



Compound **15** described above is a precursor for the naturally occurring Aspidophylline A, and **13** can be synthesized from **16** as shown below.

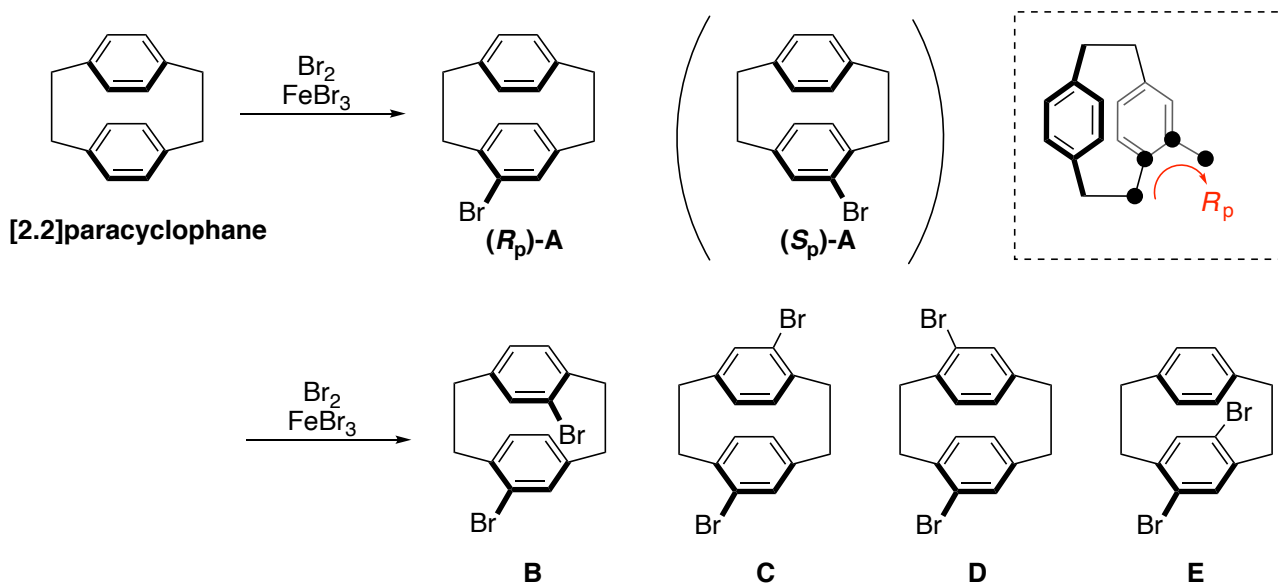


4. **Draw** the structures of **17** and **18** and clearly identify the relative stereochemistry where necessary.
5. **Draw** the structure of **19** and clearly identify the stereochemistry where necessary.
6. In the conversion of **20** to **21**, the reaction occurs selectively at the sterically less hindered side, and the stereochemistry with asterisk (*) of **13** is set in this step. **Draw** the structure of **21** and clearly identify the stereochemistry where necessary.

Problem 26. Planar chirality

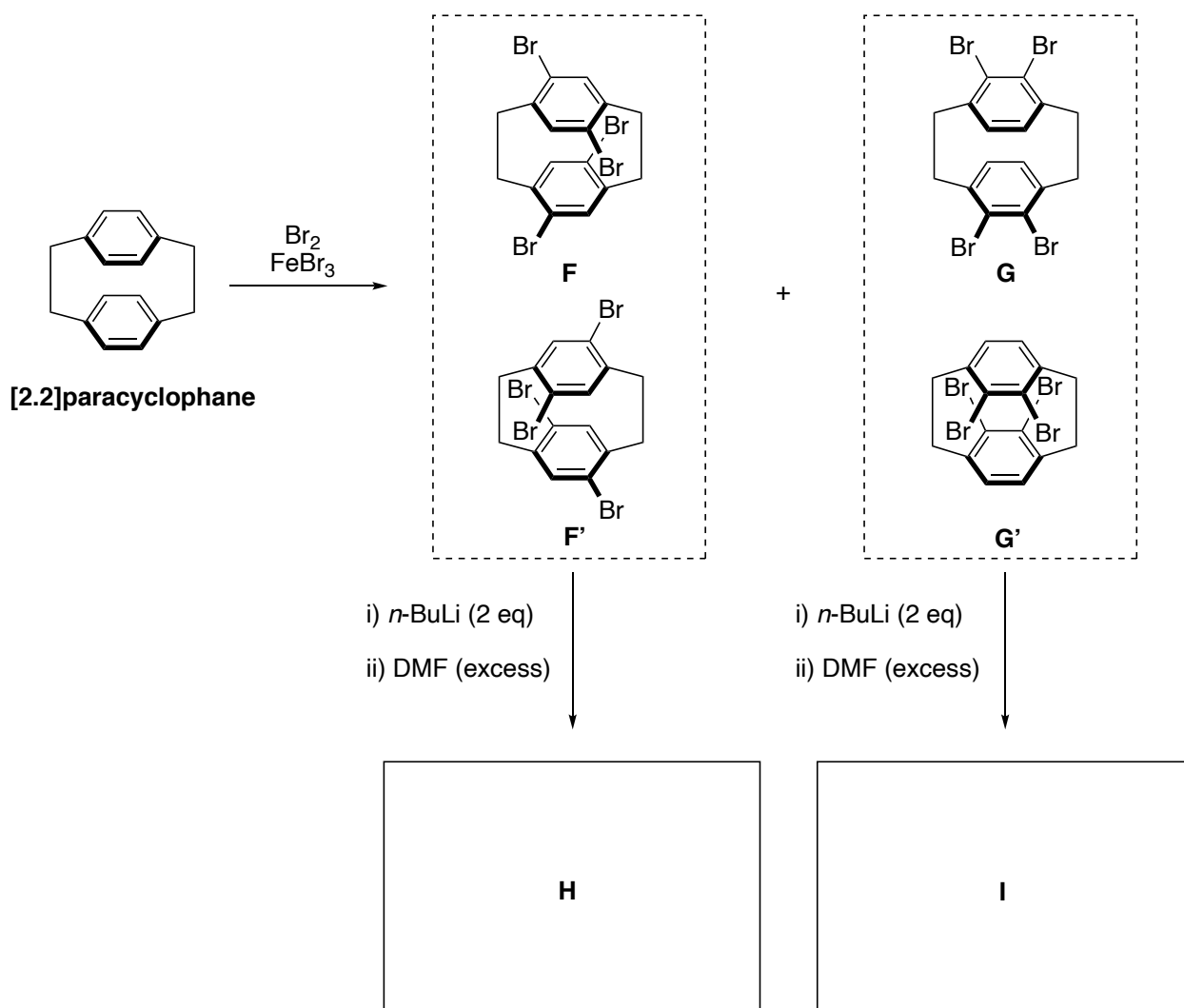
A cyclophane consists of aromatic units (typically benzene rings) and aliphatic chains that form bridges between two non-adjacent positions of the aromatic rings. As shown below, if the bridge is ethylene ($-\text{CH}_2-\text{CH}_2-$) and the substitution pattern is *para*, it is called [2.2]paracyclophane. For some kinds of [2.2]paracyclophanes, enantiomers can be isolated depending on the substituent configurations on the aromatic rings given that these cannot rotate.

Brominating [2.2]paracyclophane affords mono-brominated **A**, which exhibits planar chirality, i.e., (*R_p*)- and (*S_p*)-isomers. Here, as shown in the dotted square, the definition of (*R_p*) is that the *ortho*-substituent is oriented in clockwise direction when traced from the other aromatic unit through the ethylene bridge. Further bromination of **A** furnished dibrominated products **B-E**.



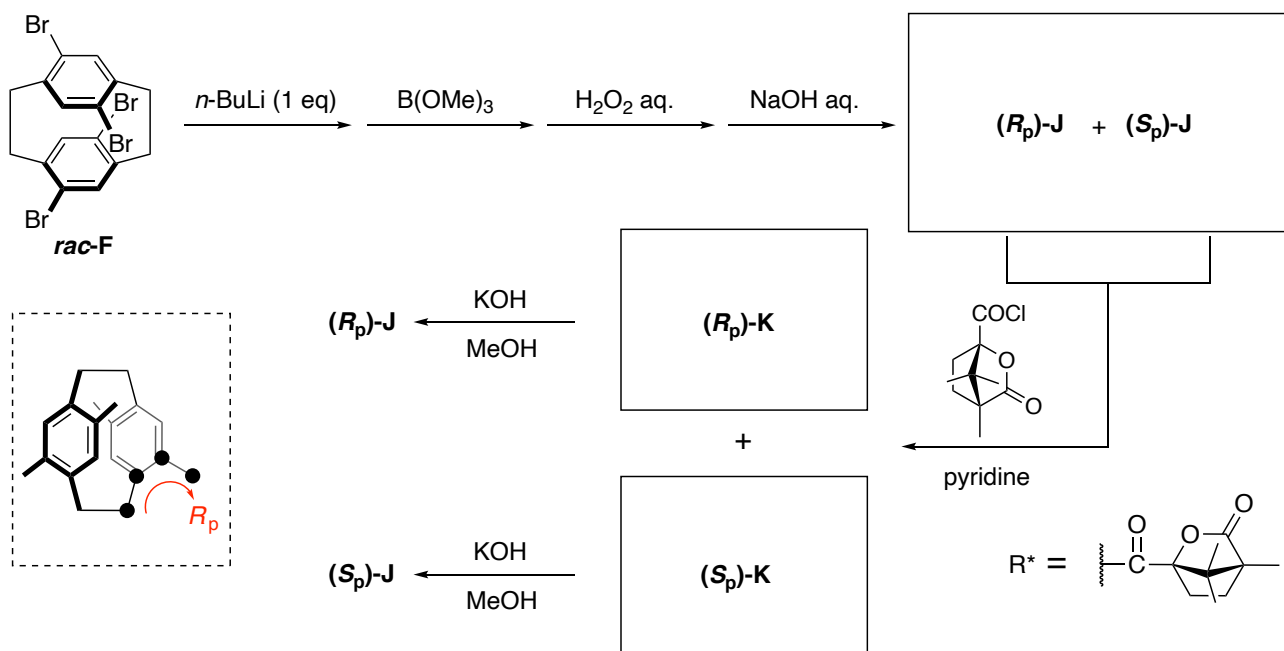
1. **Choose** from **B-E** all products that are optically active.

Bromination of [2.2]paracyclophane with an excess of bromine in the presence of FeBr_3 results in dibromination on each benzene ring to generate tetrabrominated products **F** (**F'**) and **G** (**G'**). Note that **F** and **F'** are a pair of enantiomers, while **G** and **G'** are identical. By adding two equivalents of *n*-BuLi to a solution of **F** or **G** at low temperature, one of two bromo-substituents in each benzene unit is exchanged to lithium, and the subsequent addition of an excess of DMF leads to the formation of several products.



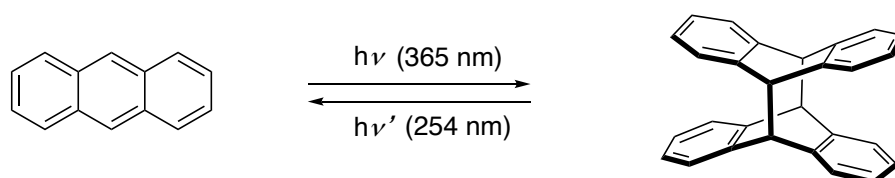
2. Assuming that the reaction proceeds completely, draw all the possible stereoisomers for **H** and **I**.

A racemate of tetrabrominated **F** (*rac*-**F**) is transformed into **J** by applying the reaction conditions shown below. Here **J** is a racemic mixture of (*R_p*)-**J** and (*S_p*)-**J**. The racemic mixture reacts with optically active (-)-camphanic chloride to give a diastereomeric mixture of (*R_p*)-**K** and (*S_p*)-**K**, which can be separated by column chromatography. (*R_p*)-**K** and (*S_p*)-**K** can be hydrolyzed to give optically pure (*R_p*)-**J** and (*S_p*)-**J**. Here, the definition of (*R_p*) is the same as in Q1. When there are several kinds of substituents on the benzene ring, the definition obeys the Cahn-Ingold-Prelog priority rule.

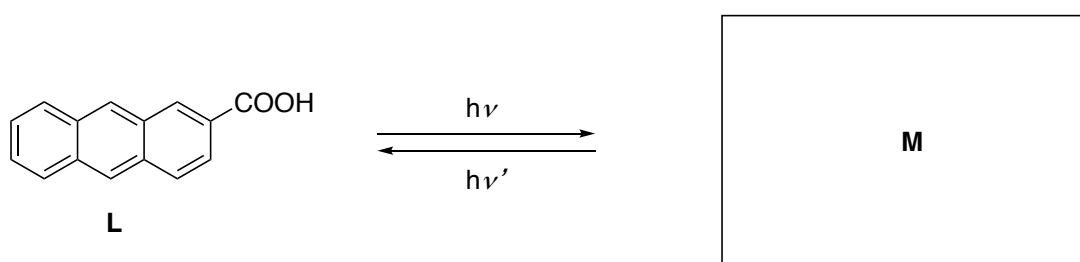


3. **Draw** the structures of (*R_p*)-**J**, (*S_p*)-**J**, (*R_p*)-**K**, and (*S_p*)-**K**. You can abbreviate the acyl moiety derived from (-)-camphanic chloride as R*.

The photodimerization of anthracene affords product whose planar chirality is similar to that of cyclophanes. As shown below, anthracene undergoes photodimerization under irradiation with ultraviolet light.

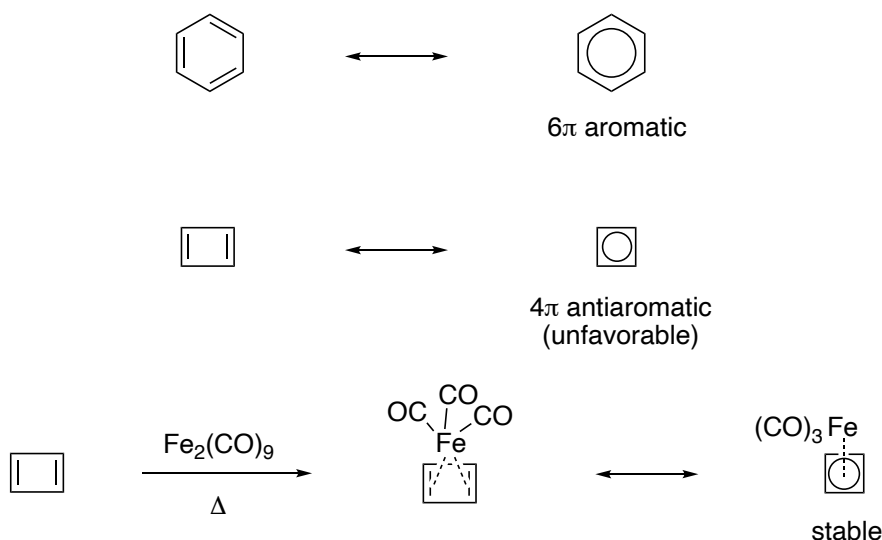


4. **Draw** all the stereoisomers of photodimerized products of 2-substituted anthracene **L**. Among these, **draw** lines between each pair of enantiomers.

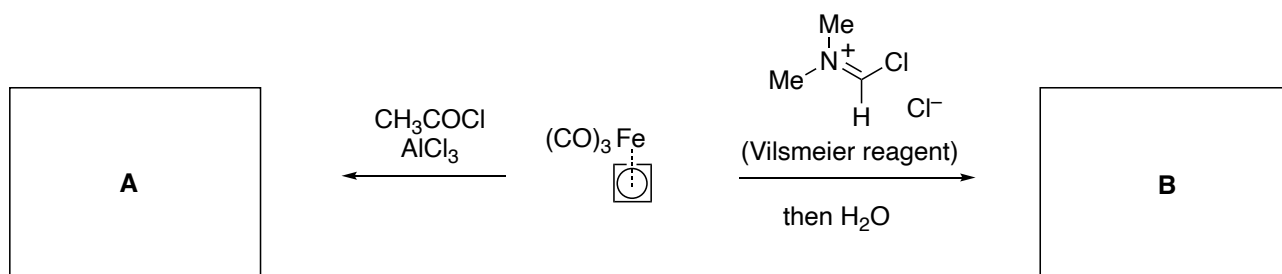


Problem 27. Cyclobutadiene

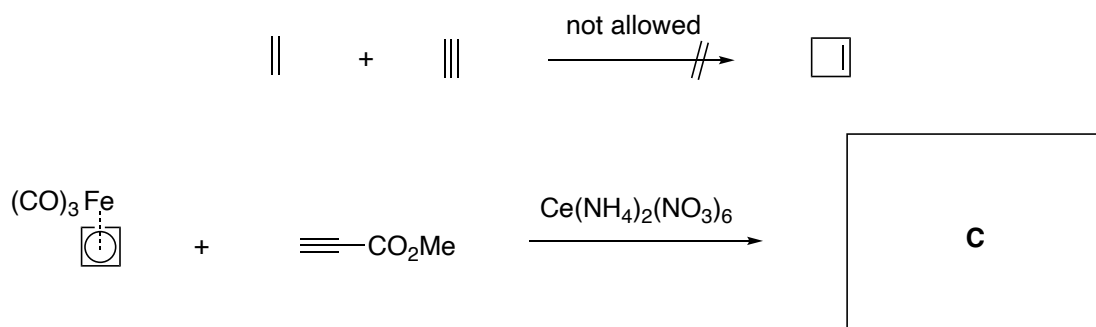
In contrast to benzene, cyclobutadiene adopts a rectangular conformation in order to avoid 4π antiaromaticity by bond alternation. Even though it is difficult to isolate pristine cyclobutadiene under ambient conditions, its tricarbonyliron complex is isolable and relatively stable toward acids and bases. Moreover, this complex readily engages in electrophilic substitutions, *i.e.*, it exhibits reactivity that is similar to that of benzene.



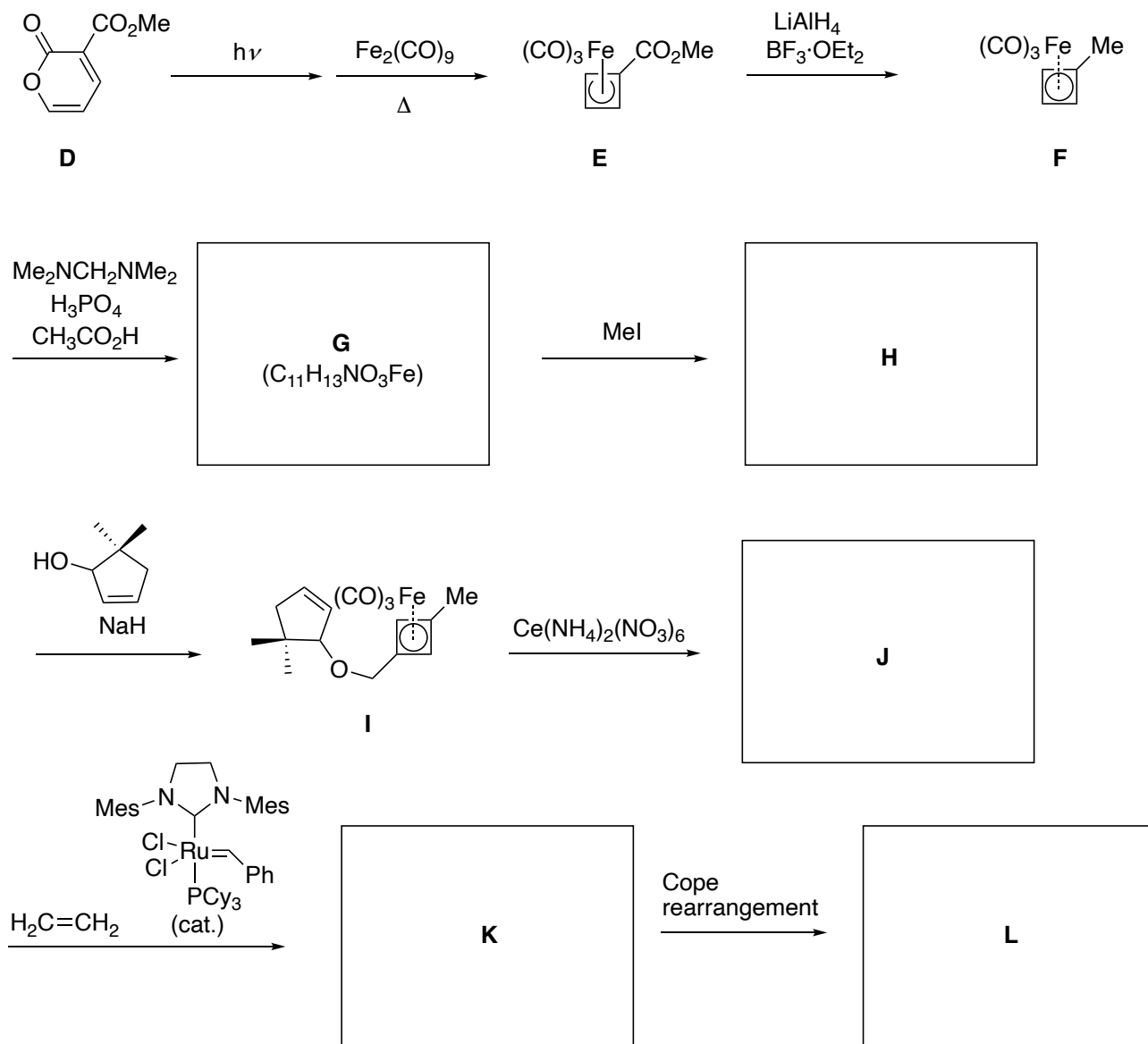
1. **Draw** the structures of **A** and **B**, which are obtained from cyclobutadiene under the conditions shown below. The description of the iron complex is allowed to be the same as that of substrate.



2. The iron moiety can be removed by treatment with cerium ammonium nitrate, $\text{Ce}(\text{NH}_4)_2(\text{NO}_3)_6$. Although $[2+2]$ -cycloaddition reactions are generally not allowed, the thus generated cyclobutadiene is so reactive that it can undergo $[2+2]$ -cycloaddition-like reactions with alkenes and alkynes. **Draw** the structure of **C** shown below. Its stereochemistry is not required.



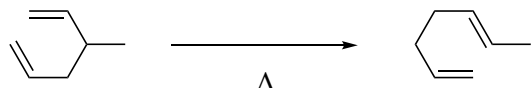
3. A part of a synthetic route toward natural product asteriscanolide is shown below.



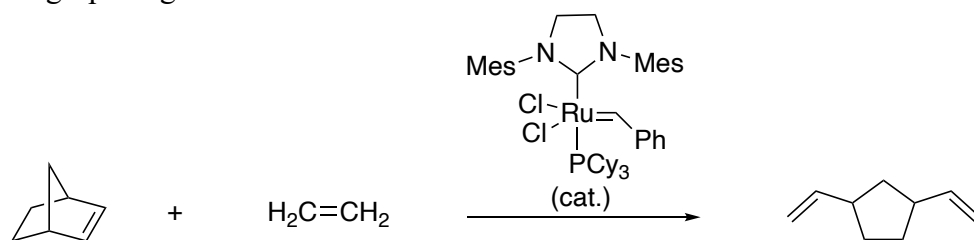
- 3-1. **Draw** the structure of the aromatic compound obtained by heating a mixture of **D** and dimethyl acetylenedicarboxylate.
- 3-2. **Draw** the structures of **G** and salt **H**. The latter is an intermediate of the reaction from **G** to **I**.
- 3-3. **Draw** the structure of tetracyclic compound **J** (its stereochemistry is not required).

3-4. The ring opening metathesis of **J** furnishes **K**, and the subsequent Cope rearrangement leads to the formation of **L**. **Draw** the structures of tricyclic compounds **K** and **L** (their stereochemistry is not required). Examples of Cope rearrangement and ring-opening metathesis are shown below.

Cope rearrangement:

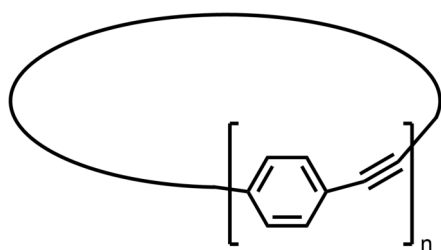


Ring-opening metathesis :

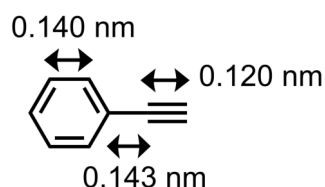


Problem 28. Onion-like complexes

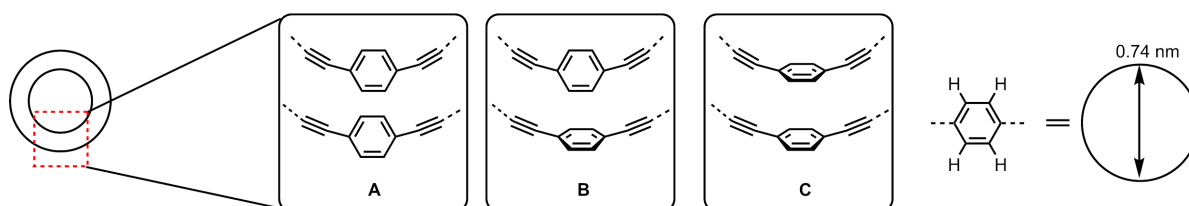
As shown below, cyclic molecules composed of alternating benzene and alkyne moieties can form an onion-like concentric complex if a suitable pair of ring-sizes is chosen.



- For $n = 6$, **calculate** the length of the outer perimeter of the ring-shaped molecule. A list of relevant bond-length values is shown below. Consider the benzene ring as a regular hexagon. In addition, **calculate** the diameter under the assumption that the ring is a true circle.

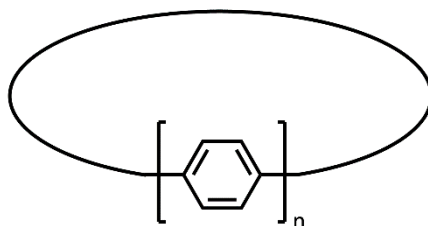


- For $n = 9$, **calculate** the length of the outer perimeter and the diameter under the same assumptions as in Q1.
- Ring **1** ($n = 6$) and ring **2** ($n = 9$) can form a concentric complex in chloroform. **Calculate** the width of the interspace between the two rings (ignore the volume of the atoms).
- From **A-C** shown below, **choose** all the possible configurations of the benzene rings in the complex of **1** and **2** when viewed vertically relative to the ring plane. Here, a benzene ring is regarded as a circle with a diameter of 0.74 nm.

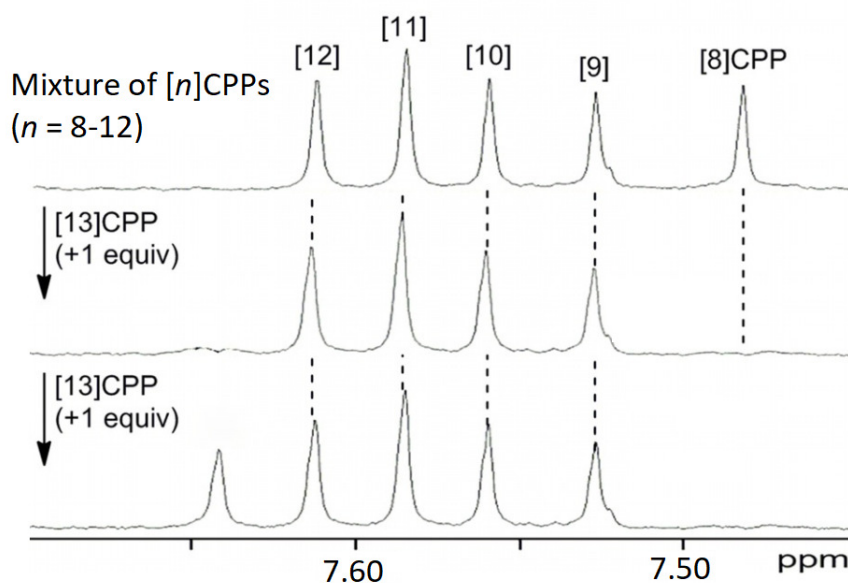


- Similar to the case of the encapsulation of **1** by **2**, C_{60} can be encapsulated by ring **1**. **Estimate** the diameter of C_{60} under the same assumptions for **1** and **2** regarding the interspace.

Cycloparaphenylenes (CPPs) are ring-shaped molecules that consist exclusively of benzene moieties that are connected in a *para* fashion. Depending on the number of constituent benzene rings (n), CPPs are usually denominated $[n]$ CPP. There are combinations of $[n]$ CPPs that can form onion-like concentric complexes.



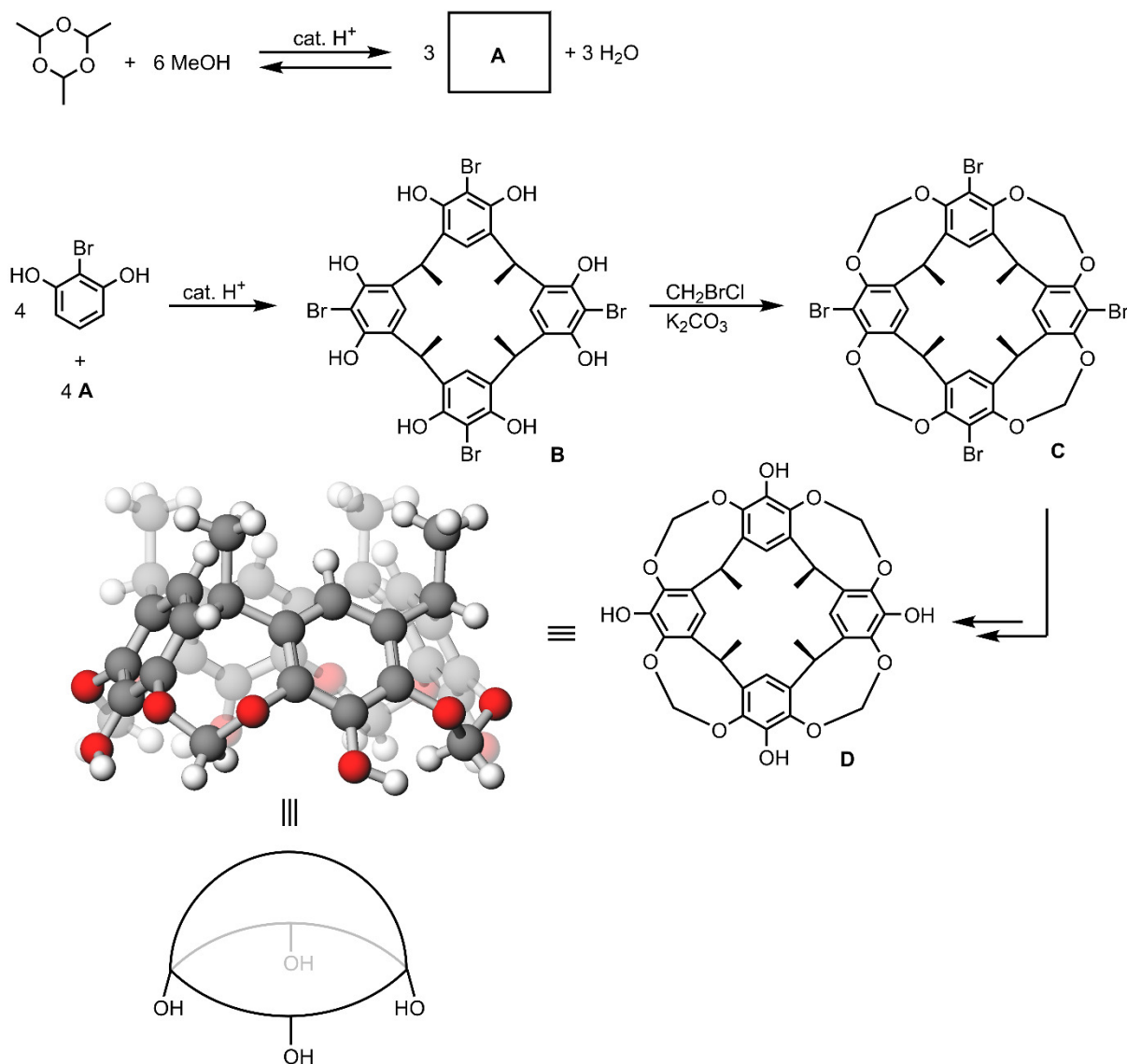
6. A free-energy change of $-18.00 \text{ kJ mol}^{-1}$ was estimated for the encapsulation of $[6]$ CPP by $[11]$ CPP in deuterated dichloroethane at 323.15 K. **Calculate** the concentration of free $[6]$ CPP (which does not form any complexes) when the same volume of solutions of $[6]$ CPP and $[11]$ CPP in deuterated dichloroethane ($0.800 \text{ mmol L}^{-1}$ each) is mixed at 323.15 K. In this case, the resulting mixture is homogenous.
7. Two equivalents of $[13]$ CPP in solution were added in two portions to a solution containing an equimolar amount of five kinds of $[n]$ CPPs ($n = 8 - 12$). Shown below is the ^1H NMR spectral change. No signals derived from CPPs were observed outside the region shown. Upon adding the first equivalent of $[13]$ CPP, the formation of a precipitate was observed. Based on the information given, **choose** all correct statements among (a) – (e).



- (a) $[13]$ CPP encapsulates $[8]$ CPP to form a precipitate.
- (b) $[13]$ CPP quantitatively forms complexes with all other $[n]$ CPPs ($n = 8 - 12$) and generates a precipitate.
- (c) The new peak that emerges at approximately 7.64 ppm can be ascribed to the complex of $[13]$ CPP and $[8]$ CPP.
- (d) The new peak that emerges at approximately 7.64 ppm can be ascribed to $[13]$ CPP.
- (e) In the presence of $[13]$ CPP, the peak associated with $[8]$ CPP is substantially downfield shifted.

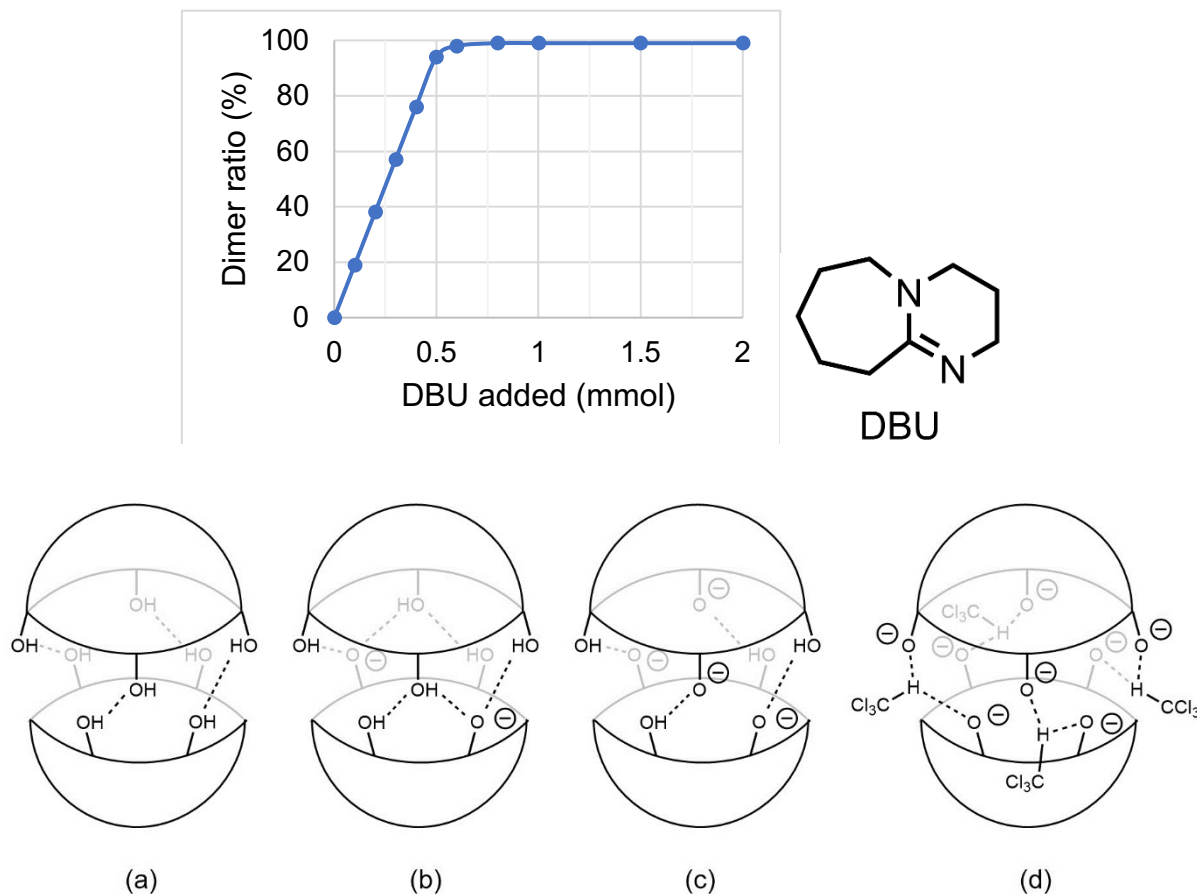
Problem 29. Hydrogen-bonded capsules

Calix[4]arene is a bowl-shaped molecule that is synthesized as shown below.



1. **Draw** the structure of intermediate **A**.
2. **Choose** the most suitable conditions for the transformation from **C** to **D**.
 - (a) *t*BuLi, then B(OMe)₃, then AcOH
 - (b) *t*BuLi, then B(OMe)₃, then H₂O₂/NaOH aq.
 - (c) BBr₃, then H₂O₂/NaOH aq.
 - (d) PMe₃, then H₂SO₄
 - (e) PMe₃, then H₂O₂ aq.

3. Two molecules of **D** form an aggregate via hydrogen-bonds upon addition of DBU (a kind of weakly nucleophilic but strong organic base; see the structure below) to a chloroform solution of **D**. Among (a) – (d), choose the most probable structure for the dominant hydrogen-bond network of dimers of **D**. Refer to the graph showing the ratio of dimer (%) as a function of the amount of DBU added to a solution of **D** (0.25 mmol) in chloroform.



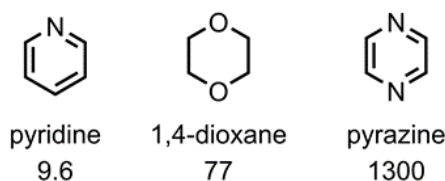
The dimeric capsule of **D** (host) described in Q3 can encapsulate other molecules (guests). In solution, the encapsulation and release of the guest(s) are reversible. The association constant K for this process is given by

$$K = \frac{[\text{solvent}][\text{guest@host}]}{[\text{solvent@host}][\text{guest}]}$$

Here, the encapsulation of guest **A** by host **B** is expressed as **A@B**. The relative association constant K_{rel} can be calculated by measuring the ratio of free and encapsulated guests in the coexisting state. Thus, K_{rel} is given by

$$K_{\text{rel}} = \frac{K_2}{K_1} = \frac{[\text{solvent}][\text{guest2@host}]}{[\text{solvent@host}][\text{guest2}]} \bigg/ \frac{[\text{solvent}][\text{guest1@host}]}{[\text{solvent@host}][\text{guest1}]} = \frac{[\text{guest2@host}][\text{guest1}]}{[\text{guest1@host}][\text{guest2}]}$$

Below, the K_{rel} values of several guest molecules in chloroform relative to benzene (guest1) are shown.

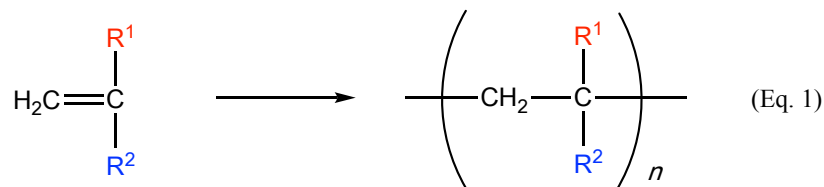


In the presence of a sufficient amount of DBU, **D** dimerizes almost quantitatively. In the following questions, free **D** can be ignored.

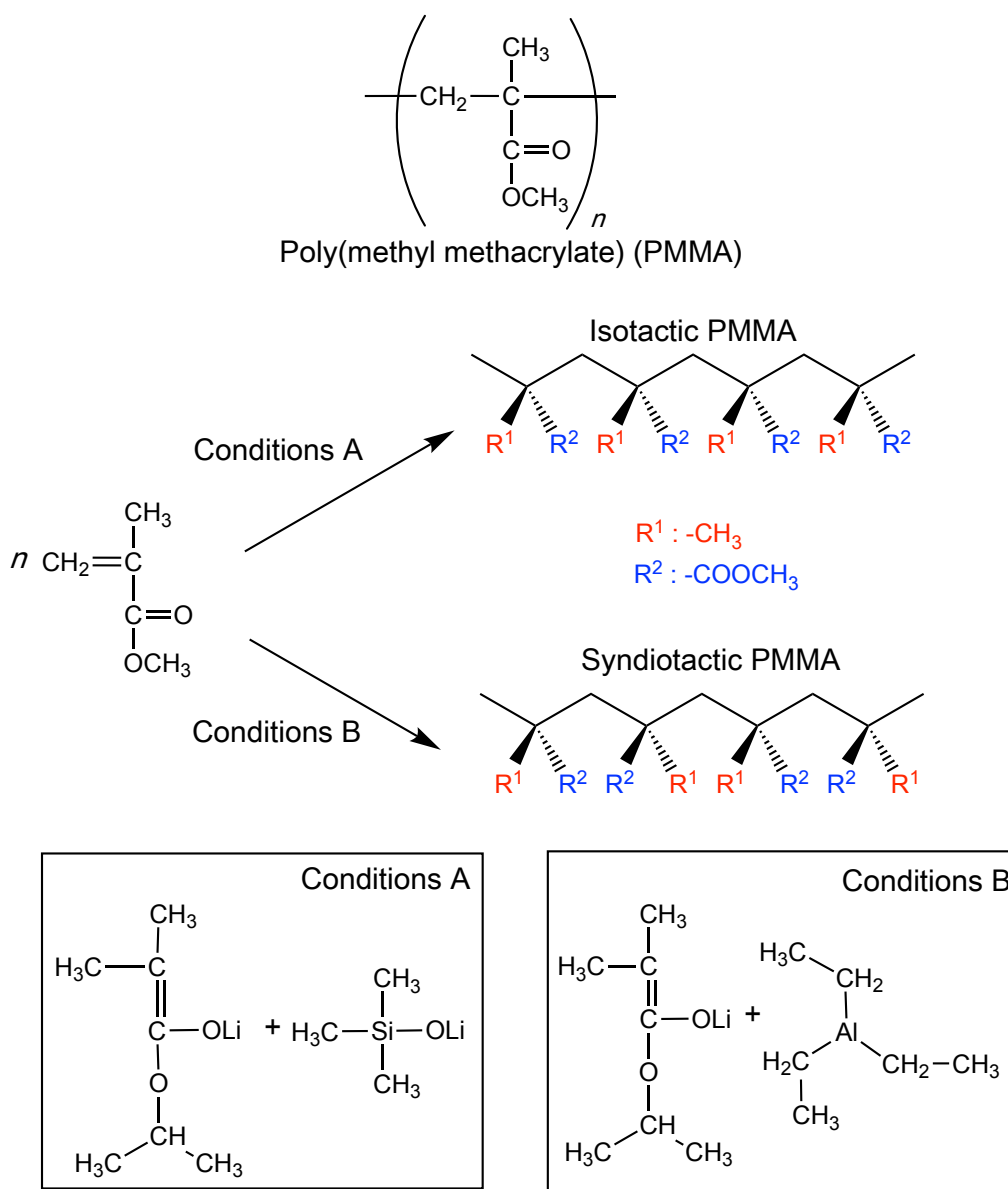
- Equimolar amounts of pyrazine and 1,4-dioxane are added to a chloroform solution of **D** in the presence of excess DBU. After the system reaches the equilibrium state, a 75:25 ratio of free to encapsulated 1,4-dioxane was found. **Estimate** the ratio of pyrazine encapsulated by **D**.
- A chloroform solution of dimers of **D** encapsulating benzene is exposed to the following conditions (a) and (b). For each set of conditions, **choose** from (1) – (3) what happens to the capsule structure and the benzene molecule.
 - Addition of acetyl chloride and pyridine.
 - Dilution with chloroform.
 - The capsule dissociates and benzene is released.
 - Both capsule and benzene remain intact.
 - The capsule remains intact, but benzene is released.
- The same solution used in Q5 is treated with K_2CO_3 and CH_2BrCl (*cf.* the reaction **B**→**C** in the scheme on the first page of this problem). Subsequently, pyrazine, which is more prone to be encapsulated than benzene, is added. However, an exchange between the encapsulated benzene and pyrazine is not observed. **Explain** this observation.

Problem 30. Synthesis and structural analysis of polymers

Polymers that contain carbon-carbon based main chains are often synthesized by chain polymerization of vinyl monomers (Eq. 1).



When the main chain of a polymer adopts a zigzag shape, polymers in which all substituents R^1 (or R^2) are located on the same side are called 'isotactic', while those in which the substituents are located on alternating sides of the main chain are called 'syndiotactic'. Polymers that contain $\text{R}^1 = -\text{CH}_3$ and $\text{R}^2 = -\text{COOCH}_3$ are called poly methyl methacrylate (PMMA). Isotactic PMMA is obtained under conditions A in the scheme below, while syndiotactic PMMA is obtained under conditions B.



The ^1H NMR spectra of isotactic and syndiotactic PMMA are shown in Figure 1.

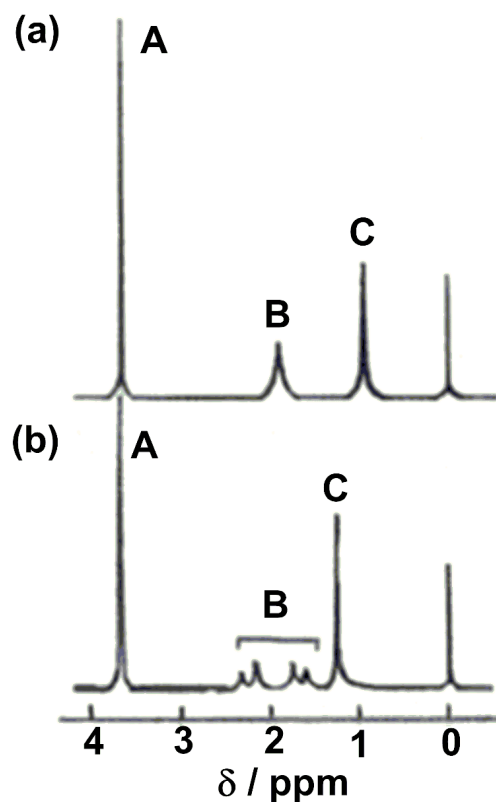
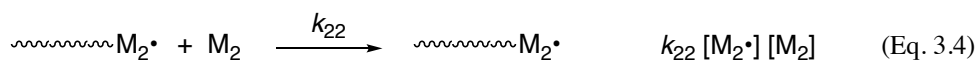
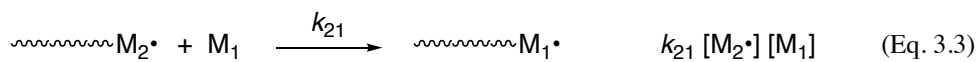
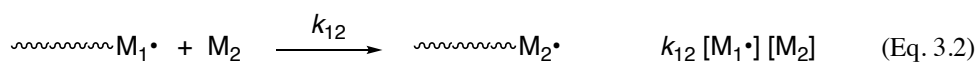


Figure 1. 100 MHz ^1H NMR spectra of two types of PMMA in CD_3NO_2 at 100°C

1. In Figure 1, the intensity ratio of the peaks A, B, and C is 3:2:3. **Assign** the protons in PMMA to the corresponding peaks.
2. In Figure 1, which ^1H NMR spectrum belongs to isotactic PMMA? **Choose** (a) or (b).

Among the copolymers that consist of two types of monomers (M_1 and M_2), those in which the sequences of M_1 and M_2 are not ordered are called ‘random copolymers’, while those in which the two types of monomers are arranged alternately are called ‘alternating copolymers’. When the monomers M_1 and M_2 are copolymerized, the composition and arrangement of the polymer are determined by the (relative) reactivity of M_1 and M_2 . When the polymerization proceeds via a radical reaction, two active species at the growth end of the polymer chain and two monomer species reacting with the active species can be considered. There are four types of monomer-addition reactions to the growth end of the polymer as shown in Eqs. 3.1 – 3.4. Here, it is assumed that the reaction between the growth end of polymer and the monomers M_1 and M_2 depends on the radical species ($M_1\cdot$ and $M_2\cdot$) at the growth end of the polymer. When the concentrations of the radically active species of M_1 or M_2 at the polymer growth end and monomers M_1 and M_2 are expressed by $[M_1\cdot]$, $[M_2\cdot]$, $[M_1]$, and $[M_2]$, respectively, the reaction rates of reactions 3.1 – 3.4 are expressed as follows:



These reactions take place at the reactive chain end terminating in either monomer ($M_1\cdot$ and $M_2\cdot$) with their reaction rate constants k . The consumption rates of M_1 and M_2 are expressed according to Eqs. 4.1 and 4.2:

$$-\frac{d[M_1]}{dt} = k_{11} [M_1\cdot] [M_1] + k_{21} [M_2\cdot] [M_1] \quad (\text{Eq. 4.1})$$

$$-\frac{d[M_2]}{dt} = k_{12} [M_1\cdot] [M_2] + k_{22} [M_2\cdot] [M_2] \quad (\text{Eq. 4.2})$$

In a steady state, where the radical concentration is constant during polymerization, the rate at which the active species $M_1\cdot$ at the polymer growth end changes to $M_2\cdot$ and the rate at which $M_2\cdot$ changes to $M_1\cdot$ are equal. The ratio of the consumption rates of M_1 and M_2 under such conditions are shown in Eq. 5 when $k_{11} / k_{12} = r_1$ and $k_{22} / k_{21} = r_2$. The reactivity ratio (r_1 or r_2) for each propagating chain end is defined as the ratio of the rate constant for addition of a monomer of the species already at the chain end to the rate constant for addition of the other monomer. These ratios are a measure of the tendency for one of the two monomers to show a preference for insertion into a growing chain in which the last inserted unit was the same, rather than the other monomer.

$$\frac{d[M_1]}{d[M_2]} = \frac{[M_1]}{[M_2]} \cdot \frac{r_1 [M_1] + [M_2]}{[M_1] + r_2 [M_2]} \quad (\text{Eq. 5})$$

3. What kind of polymers can be obtained when r_1 and r_2 adopt the values shown in (1), (2), and (3)? Among (a – g), **select** those that most appropriately depict the sequence and the ratio of the monomer-unit content in the polymer synthesized by mixing two different monomers in a 1:1 ratio. When the values of fraction of M_1 unit in the polymer (0 – 1.0) and the initial concentration ratio of M_1 to M_2 ($[M_1] / ([M_1] + [M_2])$; 0 – 1.0) are plotted on the vertical and horizontal axes, respectively, **select** among (A – F) those sequences that most accurately reflect the characteristics of the polymer obtained in each system.

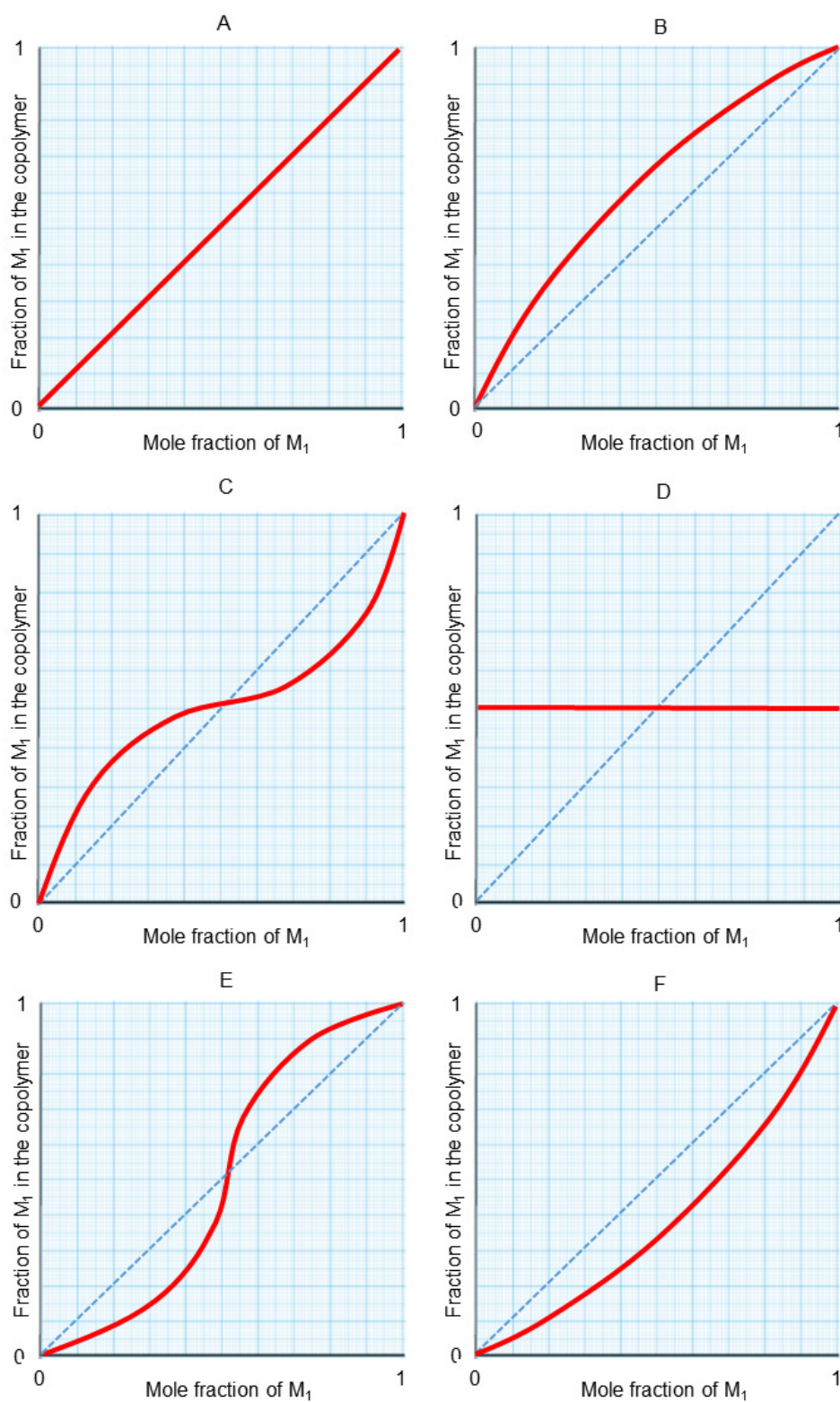
- | | | |
|-----|--------------|--------------|
| (1) | $r_1 = 1.0,$ | $r_2 = 1.0$ |
| (2) | $r_1 = 2.0,$ | $r_2 = 0.50$ |
| (3) | $r_1 = 0,$ | $r_2 = 0$ |

Sequence and ratio of the monomer-unit content in the polymer:

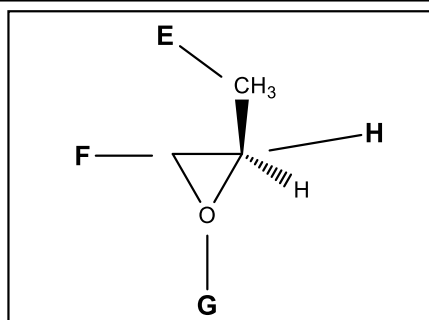
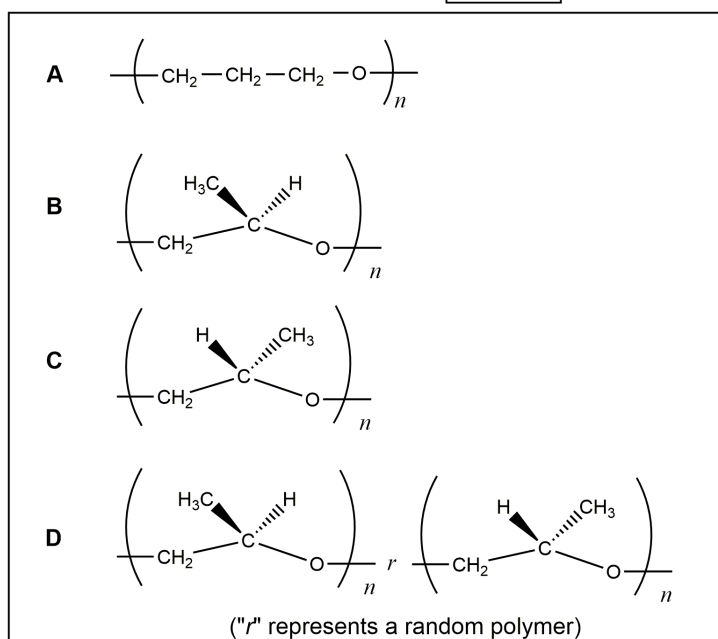
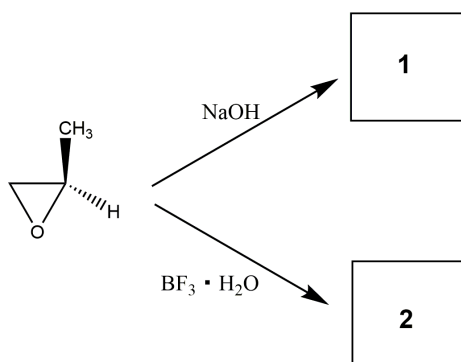
- a ----- $M_1-M_2-M_1-M_2-M_1-M_2-M_1-M_2-M_1-M_2$ -----
- b ----- $M_1-M_1-M_1-M_1-M_1-M_1-M_1-M_1-M_1-M_1$ -----
- c ----- $M_2-M_2-M_2-M_2-M_2-M_2-M_2-M_2-M_2-M_2$ -----
- d ----- $M_1-M_1-M_2-M_1-M_2-M_1-M_1-M_1-M_2-M_1$ -----
- e ----- $M_2-M_2-M_1-M_2-M_1-M_2-M_2-M_2-M_1-M_1$ -----
- f ----- $M_1-M_1-M_1-M_1-M_1-M_2-M_2-M_2-M_2-M_2$ -----
- g ----- $M_1-M_2-M_2-M_1-M_1-M_2-M_1-M_2-M_2-M_1$ -----

4. What kind of polymer can be obtained when $r_1 = 0.50$ and $r_2 = 0.50$? When the vertical axis is the fraction of M_1 in the polymer (0 to 1) and the horizontal axis is the initial concentration ratio of M_1 to M_2 (0 to 1), **select** a suitable graph showing the characteristics of the obtained polymer.

Graphs for Q3 and Q4



5. A copolymer that contains two types of monomers (M_1 and M_2) with a monomer reactivity ratio of $r_1 = 0.40$ and $r_2 = 0.10$ is synthesized using a radical polymerization initiator. In order to synthesize a copolymer with an M_1 content of 50 mol% at the initial stage of polymerization, **how much** M_1 must be mixed with M_2 ? Your answer should be expressed in terms of mol% of M_1 relative to the two monomers.
6. The configuration of the obtained polymer is different when a) NaOH (anionic polymerization) or b) BF_3 in the presence of a small amount of water (cationic polymerization) is added as an initiator to optically active propylene oxide. Among (A – D), **select** the appropriate polymer structure for **1** and **2**. In addition, **select** among (E – H) the site where the initiator reacts during the synthesis of **1** and **2**.

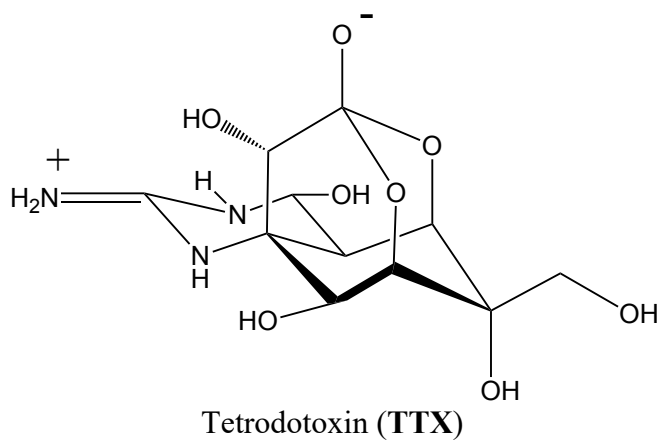


Problem 31. Total synthesis of tetrodotoxin

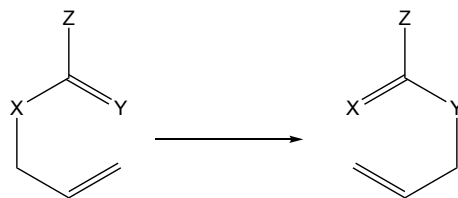
The 'Fugu' fish, which inflates and threatens when angry, has a delicious taste and is marketed as a delicacy in Japan.



However, fugu fish are also very dangerous as they contain highly toxic substances such as tetrodotoxin (TTX). The structure of TTX has been determined, and its asymmetric total synthesis has been accomplished.

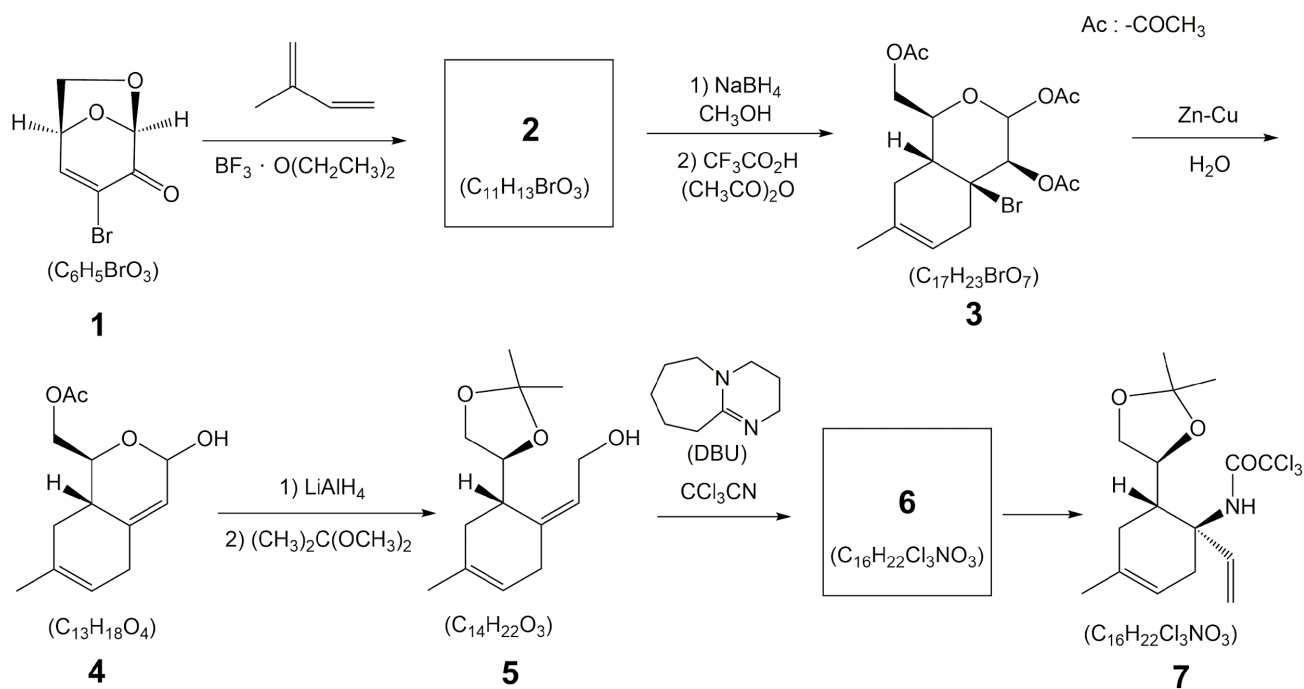


1. Compound **7** was synthesized from **1** via the synthetic route shown below. **Draw** the structures of **2** and **6** and clearly identify the stereochemistry where necessary. Compound **7** is the product of [3,3]-sigmatropic rearrangement from a compound with 3-hetero-atomic-1,5-diene structure as shown in the following scheme.

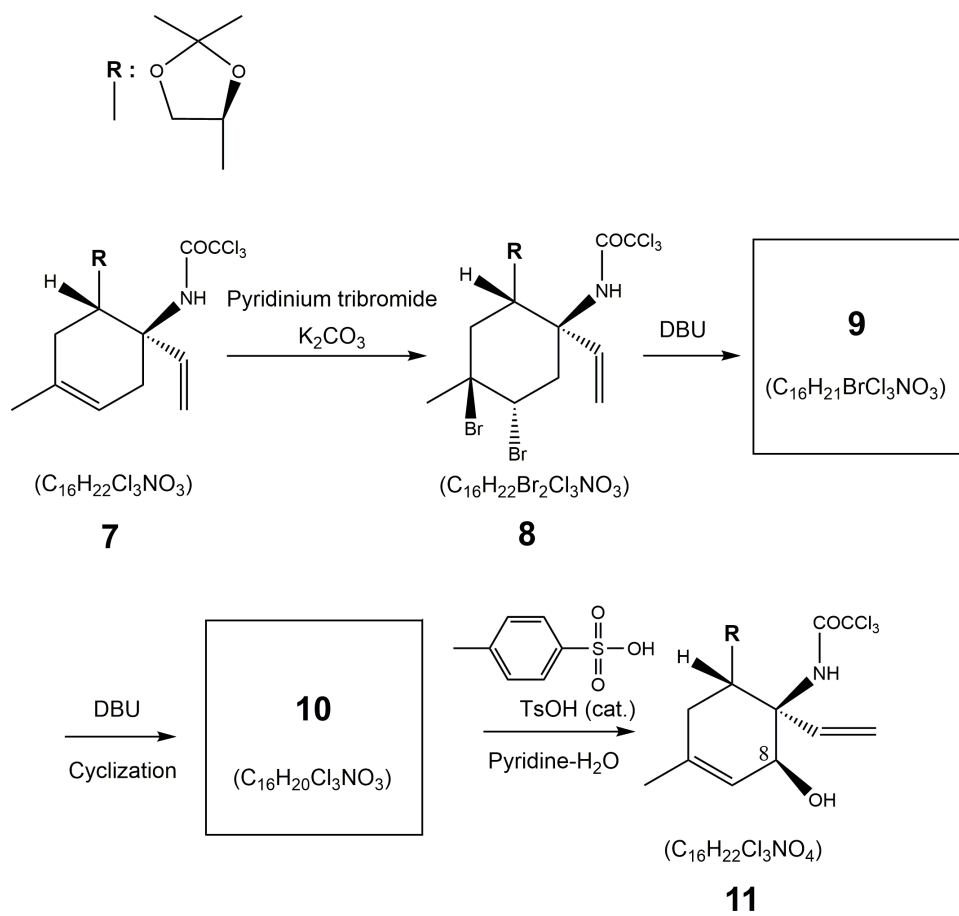


X = O, Y = NH

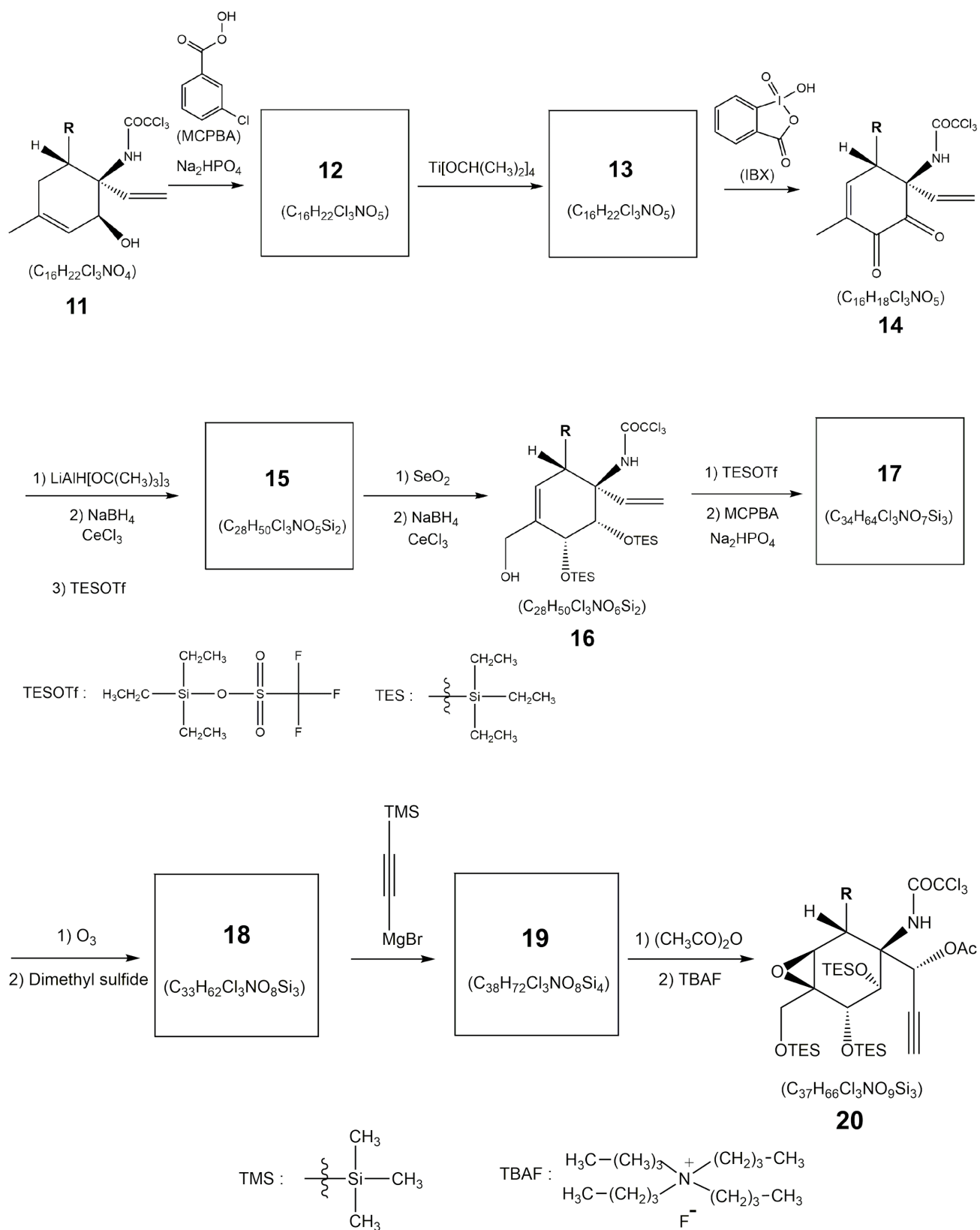
Scheme. [3,3]-Sigmatropic rearrangement reaction



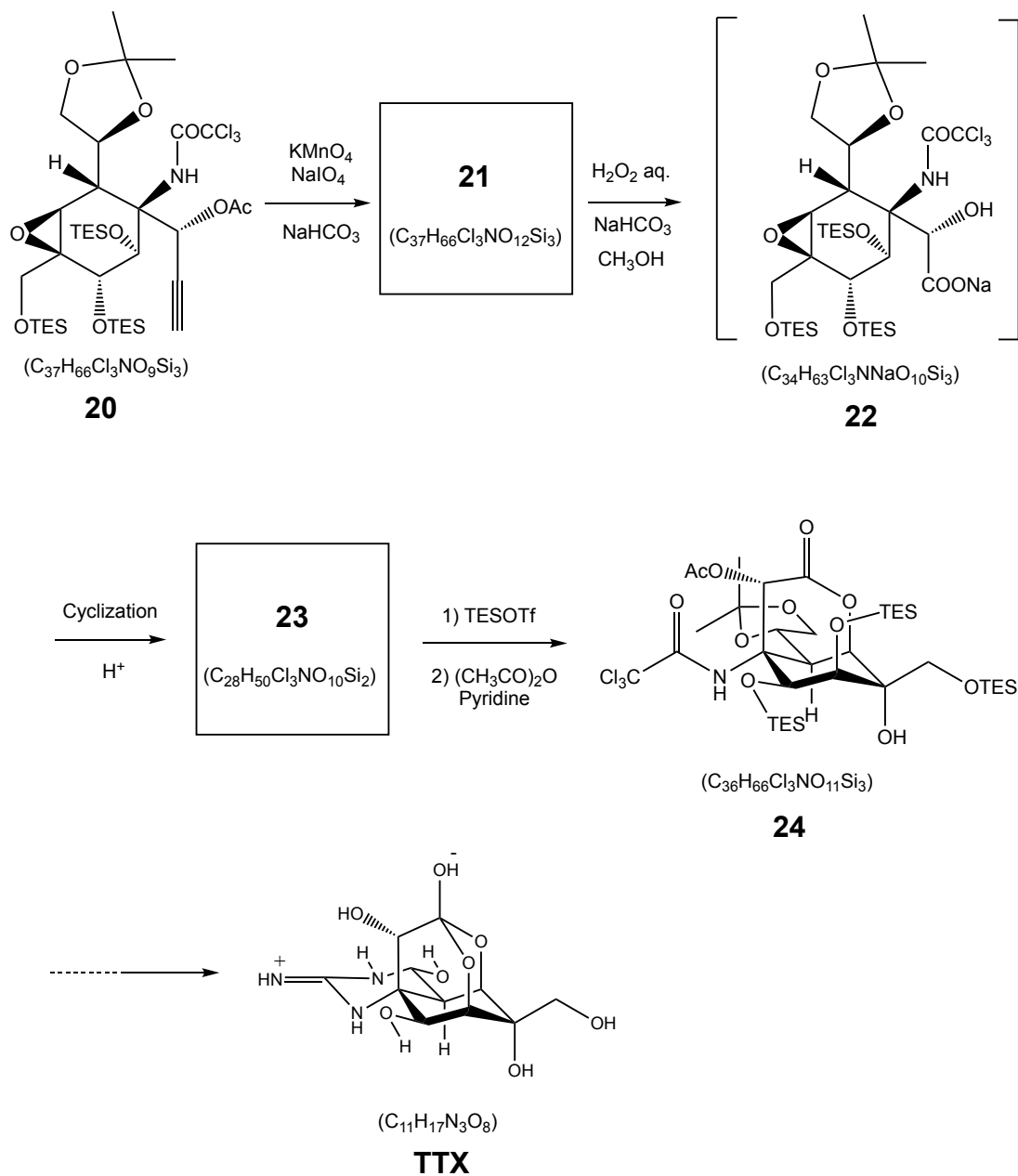
2. To synthesize **11**, a hydroxy group is introduced into **7** in a site-specific and stereoselective manner. **Draw** the structures of **9** and **10** and clearly identify the stereochemistry where necessary.



3. More hydroxy groups and oxygen-based functional groups required for the synthesis of **TTX** are introduced by epoxidation of the ring olefin, isomerization to an allyl alcohol, oxidation of the allylic position with SeO_2 , and another epoxidation. Draw the structures of **12**, **13**, **15**, **17-19** in the reaction scheme below and clearly identify the stereochemistry where necessary.



4. During the synthesis of **24** from **20**, a regioselective ring opening of epoxide is carried out in the conversion from **22** to **23**. The total synthesis of **TTX** was achieved by hydrolyzing all protecting groups under acidic conditions after the introduction of guanidine. **Draw** the structures of α -keto acid derivative **21** and cyclization product **23** and clearly identify the stereochemistry where necessary.



Appendix

Practical Tasks

Task 1. Analysis of the saponification rate using a pH meter

Purpose

Although the hydrolysis of esters is very slow in itself, it is significantly accelerated by the presence of acids or bases, which act as catalysts. A typical ester hydrolysis reaction is the saponification of fats and oils, which produces soap. In the saponification reaction using sodium hydroxide, hydroxide ions are consumed because the organic acids produced react with sodium hydroxide. In the saponification of ethyl acetate using sodium hydroxide, the reaction rate, v , is proportional to the product of the concentration of ethyl acetate, $[\text{CH}_3\text{COOC}_2\text{H}_5]$, and the concentration of hydroxide ions, $[\text{OH}^-]$, according to:

$$v = k_2[\text{CH}_3\text{COOC}_2\text{H}_5][\text{OH}^-]$$

where k_2 is the rate constant of the second-order reaction.

When ethyl acetate is present in excess relative to sodium hydroxide, the concentration of ethyl acetate can be considered constant during the reaction. The reaction under such conditions is known as a pseudo-first-order reaction. By defining the reaction rate constant k'_1 as:

$$k'_1 = k_2[\text{CH}_3\text{COOC}_2\text{H}_5],$$

the reaction rate, v , can be expressed as:

$$v = k'_1[\text{OH}^-]$$

Therefore, the reaction rate constants k'_1 and k_2 can be obtained by examining the change in the hydroxide ion concentration over time. In this experiment, the concentration of the hydroxide ion during the saponification of ethyl acetate is monitored using a pH meter, and the reaction rate constant is determined by analyzing the results.

Chemicals

Substance	Name	State	GHS Codes
$\text{C}_4\text{H}_8\text{O}_2$	Ethyl acetate	liquid	H225, H320, H332, H335, H336
NaOH	Sodium hydroxide aqueous solution	liquid	H315, H318, H371
$\text{C}_6\text{H}_4(\text{COOH})(\text{COOK})$	Potassium hydrogen phthalate aqueous solution (pH = 4 standard solution)	liquid	Not applicable
KH_2PO_4	Potassium dihydrogen phosphate aqueous solution (pH = 7 standard solution)	liquid	H320
Na_2HPO_4	Disodium hydrogen phosphate aqueous solution (pH = 7 standard solution)	liquid	H320
$\text{Na}_2\text{B}_4\text{O}_7 \cdot 10\text{H}_2\text{O}^*$	Sodium tetraborate aqueous solution (pH = 9 standard solution)	liquid	H360
NaHCO_3	Sodium hydrogen carbonate aqueous solution (pH = 10 standard solution)	liquid	Not applicable
Na_2CO_3	Sodium carbonate aqueous solution (pH = 10 standard solution)	liquid	H318, H332, H335, H336

*If students use the pH = 9 standard solution, it should be prepared by the mentor. Otherwise, a pH = 10 standard solution should be used.

Glassware and equipment

Volumetric flasks (2 pcs; 100 mL), Erlenmeyer flask with stopper (2 pcs), volumetric pipette (2 pcs; 25 mL), volumetric pipette (1 pc; 2 mL), pipette (1 pc), stir bar (1 pc), stopwatch (1 unit), pH meter (1 unit), water bath (1 unit), thermometer (1 unit), stirrer (1 unit), precision electronic balance (1 unit) [measurement accuracy: 0.1 mg].

Experimental procedure

Preparation of an aqueous solution of ethyl acetate

1. **Add** ion-exchanged water (ca. 50 mL) to a volumetric flask (100 mL) and weigh it on the precision electronic balance.
2. **Add** approximately 90 mg of ethyl acetate to the ion-exchanged water in the volumetric flask, and immediately close the flask with a stopper.
3. **Record** the mass of ethyl acetate based on the mass increase.
4. **Add** ion-exchanged water to the marked line to increase the volume to 100 mL and mix it.
5. Using a volumetric pipette, **transfer** 25 mL of the aqueous solution of ethyl acetate into an Erlenmeyer flask. **Place** the stir bar, **close** the flask with a stopper, and **place** it in a water bath at 30 °C to keep the temperature of the liquid constant.

Preparation of an aqueous solution of NaOH

1. **Add** ion-exchanged water (ca. 50 mL) to a volumetric flask (100 mL).
2. Using a volumetric pipette, **transfer** 2 mL of a 0.05 mol L⁻¹ aqueous solution of NaOH to the volumetric flask, and then **add** ion-exchanged water to the marked line to increase the volume to 100 mL.
3. Using a volumetric pipette, **transfer** 25 mL of the aqueous solution of NaOH into an Erlenmeyer flask, **close** it with a stopper, and **place** the flask in a water bath at 30 °C to keep the temperature of the liquid constant.

Calibration of the pH meter

Calibrate the pH meter using three different pH standard solutions.

Saponification

1. **Begin** stirring the aqueous solution of ethyl acetate in the Erlenmeyer flask in the water bath.
2. Quickly **add** the aqueous solution of NaOH (25 mL), close the flask with a stopper and **start** timing with a stopwatch.
3. After 3 minutes, **insert** the thermometer and the electrodes of the pH meter.
4. **Measure** the temperature and the pH value of the solution every 5 minutes for 60 minutes.

Discussion

Relationship between the pH value and the reaction rate

The transformation and definite integration of $v = -\frac{d[\text{OH}^-]}{dt} = k'_1[\text{OH}^-]$ from $t = 0$ to $t = t$ gives:

$$-\ln \frac{[\text{OH}^-]}{[\text{OH}^-]_0} = k'_1 t$$

where $[\text{OH}^-]_0$ is the initial concentration of sodium hydroxide, and $[\text{OH}^-]$ is the concentration of sodium hydroxide at time t . Using the common logarithm, the equation will be:

$$-\log \frac{[\text{OH}^-]}{[\text{OH}^-]_0} = \frac{1}{2.303} \times k'_1 t.$$

Furthermore, this equation can be transformed to give:

$$-\log[\text{OH}^-] + \log[\text{OH}^-]_0 = \frac{1}{2.303} \times k'_1 t \quad (\text{a})$$

Since $[\text{OH}^-] = \text{pH} - 13.833$ at 30°C , equation (a) can be rewritten as:

$$(\text{pH})_0 - \text{pH} = \frac{k'_1}{2.303} \times t$$

or:

$$\text{pH} = -\frac{k'_1}{2.303} \times t + (\text{pH})_0.$$

Here, $(\text{pH})_0$ and pH are the pH value of the solution before the reaction and at time t , respectively.

Analysis

1. **Calculate** the concentration of the prepared aqueous solution of ethyl acetate (C_1) and the concentration of the diluted aqueous solution of NaOH (C_2).

C_1 [mol L ⁻¹]	C_2 [mol L ⁻¹]

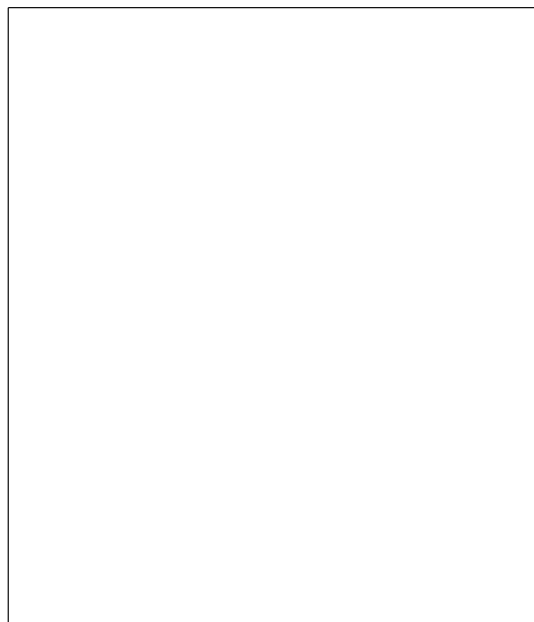
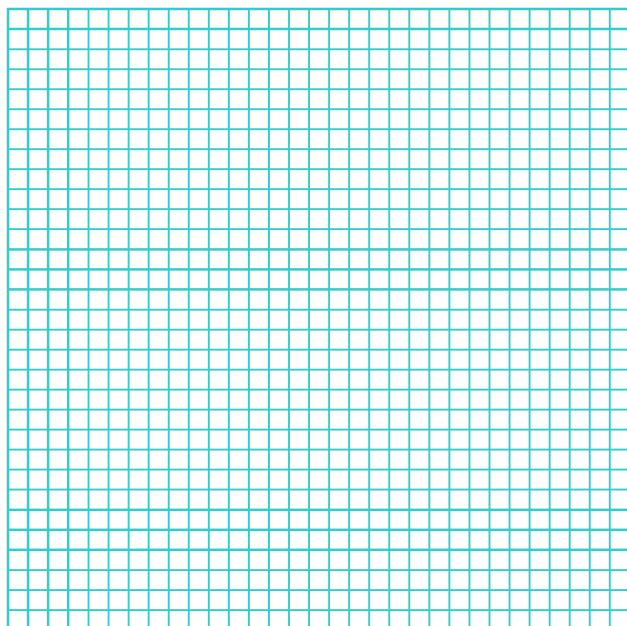
2. **Write** the equation for the saponification of ethyl acetate with NaOH.

--

3. **Record** the temperature and the pH value of the solution.

Time (minutes)	Temperature (°C)	pH	Time (minutes)	Temperature (°C)	pH

4. **Plot** the time on the horizontal axis, the pH value on the vertical axis, and **determine** k'_1 from the slope. Indicate the units.



5. **Determine** k_2 . Given that the concentrations of the two aqueous solutions are low, it can be assumed that the volume after mixing is equal to the sum of the volumes of the two solutions.

6. The time when the concentration of the substrate is half of its initial concentration is called the half-life (time of half decay), which is represented using the symbol $t_{\frac{1}{2}}$. **Determine** $t_{\frac{1}{2}}$.

Task 2. Simultaneous acid–base titration

Introduction

Sodium carbonate, which is a raw material for glass, is produced by absorbing ammonia into an aqueous solution of sodium chloride and subsequent thermal decomposition of the sodium hydrogen carbonate obtained after passing carbon dioxide. Sodium carbonate can also be obtained by reacting carbon dioxide with an aqueous solution of sodium hydroxide, which is an important chemical for the production of soap, paper, and fibers.

In this experiment, a differential titration (Warder method) is used to simultaneously determine the concentrations of two electrolytes with different basicity. Specifically, the mass of the electrolytes in a mixed aqueous solution containing sodium hydroxide ($pK_a > 13$) and sodium carbonate ($pK_{a1} = 6.35$, $pK_{a2} = 10.33$) will be determined using two pH indicators.

Chemicals

Substance	Name	State	GHS Codes
HCl	Hydrochloric acid	Aqueous solution	H301, H314, H318, H330, H331, H334, H370, H372, H400
C ₂₀ H ₁₄ O ₄	Phenolphthalein	Ethanol solution	H225, H320, H335, H336, H341, H351, H372, H373
C ₁₄ H ₁₄ N ₃ NaO ₃ S	Methyl orange	Aqueous solution	-
NaOH	Sodium hydroxide	Aqueous solution	H314, H318, H370, H402
Na ₂ CO ₃	Sodium carbonate	Aqueous solution	H332, H318, H335, H336

Glassware and Equipment

- 1 Volumetric pipette, 20 mL with pipette filler
- 1 Burette, 25 mL
- 2 Erlenmeyer flasks with stopper (HCl standard solution, unknown alkali solution), 300 mL
- 1 Plastic container (for solution-state chemical waste), 1 L
- 2 Pipettes and pipetting bulbs (for indicators **a** and **b**)
- 5 Titration flasks, 100 mL
- 1 Erlenmeyer flask (for transferring the HCl standard solution to the burette), 50 mL
- 1 Transfer funnel
- 1 Laboratory stand with burette clamp

Chemicals

- 0.1 mol L⁻¹ HCl standard aqueous solution
- Unknown alkali solution containing NaOH and Na₂CO₃
- Indicator **a**: Phenolphthalein ethanolic solution
- Indicator **b**: Methyl orange aqueous solution
- Deionized water

Experimental procedure

- (1) **Transfer** 20.00 mL of the unknown alkali aqueous solution into a 100 mL titration flask using a 20 mL volumetric pipette. **Add** indicator *a*, which will turn the solution reddish purple. **Titrate** the unknown alkali solution by adding the HCl standard solution in the burette. When the alkali solution turns pale pink, you have reached the first equivalence point. **Record** the volume (V_a) in your notebook.
- (2) **Add** indicator *b* to the now pale-pink aqueous solution. The color of the solution will turn yellow. **Continue** the titration using the HCl standard solution until the aqueous solution turns light orange, where you have reached the second equivalence point. **Record** the volume (V_b ; volume from the first equivalence point to the second equivalence point).

Repeat procedures (1) and (2) if necessary.

Results

Titration Step (1)

No.	V_{final} (mL)	V_{initial} (mL)	V (mL)
1			
2			
3			
4			
5			
Accepted volume V_a			

Titration Step (2)

No.	V_{final} (mL)	V_{initial} (mL)	V (mL)
1			
2			
3			
4			
5			
Accepted volume V_b			

Questions

1. **Write** the two chemical equations for the neutralization reactions during titration step (1).
2. **Write** the chemical equation for the neutralization reaction during titration step (2).

3. From the results of the above titration operation, **calculate** the weights (g) of NaOH and Na₂CO₃ contained in 1 L of the unknown alkali aqueous solution.

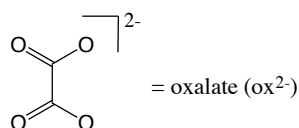
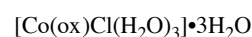
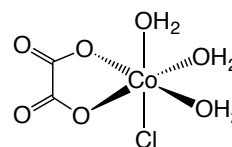
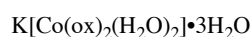
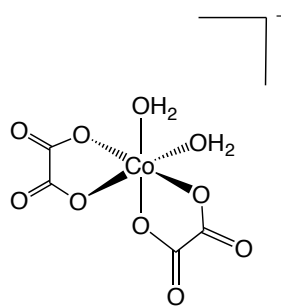
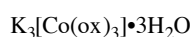
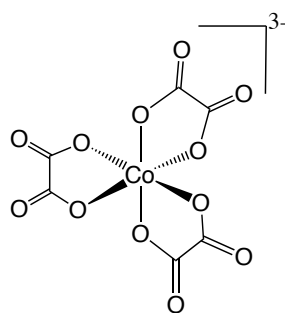
	Weight (g)
NaOH	
Na ₂ CO ₃	

Calculation:

4. **Sketch** the pH titration curve expected for the unknown alkali solution.

Task 3. Synthesis and analysis of a cobalt(III) oxalate complex

Cobalt is a silver-white ferromagnetic metal that belongs to the elements of the iron group. As it is less easily oxidized than iron as well as less corroded by acids and bases, alloys of cobalt with nickel, chromium, molybdenum, and other metals are used in equipment that requires wear resistance, such as cutting tools and high-grade materials such as scissors. Cobalt is also one of the trace biological essential elements because it is the central metal ion of vitamin B12. The most common oxidation states of cobalt are +2 and +3; cobalt ions in these oxidation states form metal complexes with a hexa-coordinated octahedral structure. In this problem, a cobalt(III) oxalate complex in which oxalate ions are coordinated to a cobalt ion is synthesized. Cobalt(II) chloride is oxidized with hydrogen peroxide and then treated with oxalic acid to obtain a green cobalt(III) oxalate complex. Below, three possible formulae for this complex are shown:



The number of oxalate ligands coordinated to the cobalt(III) oxalate complex synthesized in this experiment can be determined by titration with an aqueous potassium permanganate solution after decomposing the metal complex with an acid. The cobalt(III) oxalate complex is photosensitive and gradually decomposes from a green to a yellowish-brown product when exposed to visible or ultraviolet light. Thus, care must be taken when handling the sample in solution. In this experiment, this effect can be ignored if the measurement is performed immediately after the solution is prepared.

Chemicals

Substance	Name	State	GHS Codes
[CoCl ₂] $\cdot$ 6H ₂ O	Cobalt(II) chloride hexahydrate	Solid	H315, H319, H301, H334, H341, H351, H361, H335, H317
H ₂ SO ₄ (aq), 6 M	Sulfuric acid	Aqueous solution	H314, H318, H330, H402, H370, H372
K ₂ C ₂ O ₄ $\cdot$ H ₂ O	Potassium oxalate monohydrate	Solid	H301, H312
Na ₂ C ₂ O ₄	Sodium oxalate	Solid	H319
H ₂ O ₂ (aq), 30 %	Hydrogen peroxide solution	Aqueous solution	H272, H314, H318, H302, H312, H331, H351, H401, H370, H372
C ₂ H ₅ OH	Ethanol	Liquid	H225, H320
KMnO ₄ (aq), ca. 0.02 M	Potassium permanganate	Aqueous solution	H272, H314, H318, H302, H341, H361, H335, H400, H410, H372
C	Activated carbon	Powder	NA

Glassware and equipment

- Erlenmeyer flask, 100 mL (2), 50 mL (1), 25 mL (3)
- Valves for Pasteur pipettes and rubber pipettes
- Hot plate
- Graduated cylinder, 25 mL
- Bath
- Ice bath
- Conical funnel and filter paper
- Glass filter for vacuum filtration
- Vacuum filtration set (Stand, flask-fixing clamp, aspirator, filtration flask or bottle, rubber adapter used for filtration)
- Burette (25 mL) and stand
- Small funnel to transfer the solution to the burette

Procedure

A. Synthesis of the cobalt(III) oxalate complex

1. **Add** 2.4 g of potassium oxalate monohydrate and 5 mL of water to a 100 mL Erlenmeyer flask, and **heat** the mixture to 70 °C in order to dissolve the solid.
2. In another 100 mL Erlenmeyer flask, **add** 1 g of cobalt(II) chloride hexahydrate followed by 3 mL of water to dissolve it. Then, **add** ca. 0.02 g of activated carbon powder followed by 1.0 mL of the 30% hydrogen peroxide solution.
3. **Add** the solution from step 1 to the solution from step 2 and **heat** the mixture while stirring in a water bath at 70 °C; the mixture will begin to foam. After further heating and stirring for about 15 minutes, the foaming will subside, and the red color of the solution will gradually turn to a dark green.
4. **Remove** the activated carbon via vacuum filtration and **wash** it with a small amount of water to obtain a dark green solution. **Transfer** the filtrate to a 50 mL Erlenmeyer flask.
5. **Add** 10 mL of ethanol to the filtrate. A green precipitate will form. To aid the precipitation, **cool** the flask in an ice bath for 0.5 h.
6. **Separate** the precipitate using vacuum filtration and **wash** it with a small amount of a water–ethanol (50/50, v/v) solution.
7. **Allow** the crystals to **air-dry** or **dry** them between two sheets of filter paper.
8. **Weigh** a clean empty vial (sample container) and **place** the dry crystals in the container to determine the weight of the resulting cobalt oxalate complex crystals.

B. Analysis of the cobalt oxalate complex

B-1. Standardization of the potassium permanganate aqueous solution (ca. 0.02 M)

Transfer the aqueous potassium permanganate solution (ca. 0.02 M) to a 25 mL burette. Accurately **weigh out** ca. 50 mg of sodium oxalate into a 100 mL Erlenmeyer flask, and then **add** 20 mL of water and 5 mL of 6 M sulfuric acid. **Warm** the flask in a hot water bath to approximately 80 °C. **Titrate** this oxalate solution with the aqueous potassium permanganate solution. When the mixture turns light pink and the color is maintained for about 1 minute, the end point of the titration has been reached. **Record** the amount of potassium permanganate aqueous solution required for the titration and **determine** its molar concentration.

B-2. Analysis of the cobalt oxalate complex

1. Accurately **weigh out** ca. 20 mg of the cobalt oxalate complex synthesized in A and **place** it in a 100 mL Erlenmeyer flask. To this Erlenmeyer flask, **add** 20 mL of water and 5 mL of 6 M sulfuric acid. **Warm** the mixed solution in the Erlenmeyer flask in a hot water bath maintained at ca. 80 °C.
2. **Titrate** the solution in the warm Erlenmeyer flask with the aqueous solution of potassium permanganate standardized in B-1. The end point is determined in the same way as above. **Record** the amount of the aqueous potassium permanganate solution required for the titration.

Questions

1. **Write** the values of the following data obtained in the experiment.

1-1. Weight of the crystals of the complex obtained in A. _____ g

1-2 Weight of sodium oxalate used in B-1. _____ g

1-3 Volume of the aqueous potassium permanganate solution (accepted) used in the titration in B-1.
_____ mL

1-4 Concentration of the aqueous potassium permanganate solution in B-1.
_____ mol L⁻¹

1-5 Weight of cobalt oxalate complex analyzed in B-2. _____ g

1-6 Volume of the potassium permanganate aqueous solution (accepted) used in the titration in B-2.
_____ mL

2. **Write** the chemical equation of the reaction used in B-1.

3. **Find** the ratio (% by weight) of the oxalate ion relative to the cobalt oxalate complex. Then, assuming that the synthesized cobalt oxalate complex has one of the following compositions, **determine** the composition ratio of the cobalt ion to the oxalate ligand.

- tris complex: $K_3[Co(C_2O_4)_3] \cdot 3H_2O$

- bis complex: $K[Co(C_2O_4)_2(H_2O)_2] \cdot 3H_2O$

- mono complex: $[Co(C_2O_4)Cl(H_2O)_3] \cdot 3H_2O$

Weight% of oxalate ion _____ %

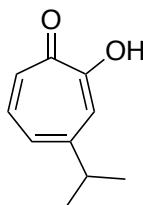
Cobalt ion to oxalate ligand composition ratio _____ :

4. **Calculate** the yield of the complex based on the raw cobalt material.

Yield of complex _____ %

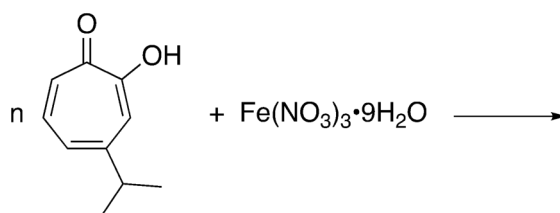
Task 4. Hinokitine: synthesis of a deep-red-colored natural product

Non-benzenoid aromatic compounds based on seven-membered ring systems have been widely investigated for many years both with respect to fundamental and applied chemistry. One such compound, 4-isopropyltropolone, is known as ‘hinokitiol’, as it had originally been isolated from an essential oil of the *Chamaecyparis obtuse* var. *formosana* (*Taiwan Hinoki*) tree. Hinokitiol is used in e.g. cosmetics, sunscreens, and oral care products. Recently, it has also been reported that hinokitiol can restore iron transport into, within, and/or out of cells, and thus may have potential in treating some genetic diseases.



Hinokitiol

The iron complex of hinokitiol, which is known as ‘hinokitine’, is found in the heartwood of *Taiwan Hinoki*, *Thuja dolabrata*, and *Thujopsis dolabrata*. In this task, you will synthesize hinokitine starting from hinokitiol and iron(III) nitrate nonahydrate.



Chemicals

Substance	Name	State	GHS Codes
C ₁₀ H ₁₂ O ₂	Hinokitiol	Solid	H302, H361
Fe(NO ₃) ₃ ·9H ₂ O	Iron(III) nitrate nonahydrate	Solid	H272, H315, H319, H402, H412
C ₂ H ₅ OH	Ethanol	Liquid	H225, H320
CH ₃ COOC ₂ H ₅	Ethyl acetate	Liquid	H225, H320, H332, H335, H336
SiO ₂	Silica gel	Solid	H351, H402
	Sea sand	Solid	

Glassware and equipment

- 2 Vials (20 mL)
- 1 Spatula
- 1 Weighing balance (0.001 g)
- 2 Weighing papers
- 1 Magnetic stirrer
- 1 Magnetic stir bar (small)
- 4 Pasteur pipettes
- 1 Filter funnel (small)
- 1 Filter paper
- 1 Filtering flask
- 1 Aspirator
- 1 Laboratory stand
- 1 Bosshead and clamp
- 1 Column tube with stopcock (inner diameter: 12 mm)
- 1 Beaker (100 mL)
- 2 Erlenmeyer flasks (100 mL)
- 2 Funnels
- Absorbent cotton
- 1 Glass rod
- 1 Eggplant flask
- 1 Rotary evaporator

Procedure

Synthesis of hinokitine

1. **Charge** a 20 mL vial (vial A) with hinokitiol (50 mg), iron(III) nitrate nonahydrate (25 mg), ethanol (0.8 mL), and a small magnetic stir bar.
2. Vigorously **stir** the reaction mixture at room temperature for 50 minutes.
3. **Collect** the product by vacuum filtration using a small filter funnel. **Transfer** all the contents of vial A to the filter funnel.
4. **Wash** the product with a small amount of ethanol using a Pasteur pipette.
5. **Let** the product **dry** on the filter funnel by continuing suction for more than 10 minutes.
6. **Transfer** the product to a 20 mL vial (vial B).

Purification of hinokitine by column chromatography on silica gel

Packing the silica gel column

1. Loosely **pack** a small plug of cotton at the bottom of the column tube using a glass rod.
2. **Clamp** the column tube to a laboratory stand. **Add** sea sand to fill the curved part of the column tube.
3. **Add** silica gel (5 g) and ethyl acetate (30 mL) as the eluent to a 100 mL beaker.
4. Carefully **pour** the silica gel slurry into the column tube using a funnel.
5. **Rinse** off any silica gel adhered to the side of the column tube with a small amount of the eluent.
6. **Tap** on the side of the column tube to help the silica gel to settle uniformly.

Loading the sample onto the column

7. **Dissolve** the product in vial B by adding a small amount of ethyl acetate.
8. **Open** the stopcock of the column tube and **reduce** the eluent level to the top of the silica gel. Be sure that the silica gel is always covered with the eluent.
9. **Close** the stopcock and **load** the solution in vial B onto the top of the silica gel using a Pasteur pipette.
10. **Open** the stopcock and **reduce** the solution level to the top of the silica gel.
11. **Close** the stopcock, **rinse** vial B with a small amount of the eluent and **load** the washings onto the top of silica gel using the Pasteur pipette.
12. **Open** the stopcock and **reduce** the solution level to the top of the silica gel.
13. **Repeat** steps 11 and 12 one or two more times.
14. **Close** the stopcock and **add** a small amount of the eluent to the column using a Pasteur pipette. **Open** the stopcock and **add** more eluent to the column.

Eluting and collecting the sample

15. **Collect** the colored fraction in a 100 mL Erlenmeyer flask. **Add** more eluent to the column if necessary.
16. **Weigh** a 100 mL eggplant flask and **record** the value.
17. **Transfer** the solution in the Erlenmeyer flask to the eggplant flask using a funnel.
18. **Evaporate** the solvent in the flask using a rotary evaporator.
19. **Submit** the flask for the evaluation.

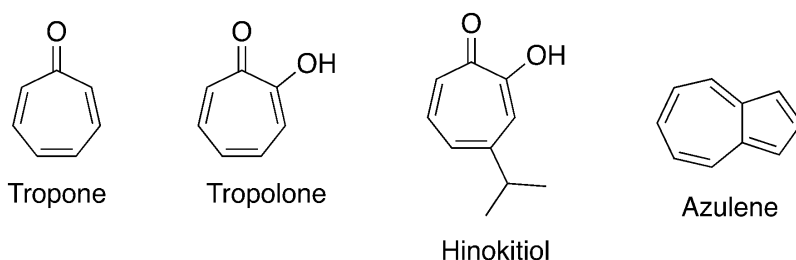
Using the above procedures, hinokitine should be obtained as a deep red solid in more than 80% yield.

Questions

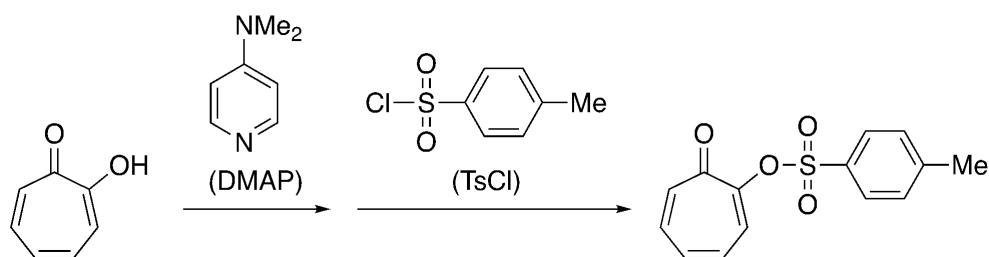
1. **Calculate** the theoretical yield of hinokitine.
2. **Write** the side product other than hinokitine.
3. **Draw** the structures of hinokitine. **Explain** how many isomers, including enantiomers, are possible for hinokitine.

Task 5. Functionalization of a seven-membered ring: synthesis of tropolone tosylate

Tropolone is a derivative of tropone (cyclohepta-2,4,6-trienone) wherein a hydroxy group is bound to the carbon atom adjacent to the ketone group on the conjugated seven-membered ring. Tropone, tropolone, and their derivatives constitute an important class of organic cyclic compounds that have aromatic character due to the contribution of the tropylium ion structure with six π -electrons. The natural product hinokitiol (4-isopropyltropolone) is a typical tropolone-type compound derived from an essential oil of the *Hinoki* tree family, and shows effective antibacterial and antimicrobial properties.



In this task, you will synthesize tropolone tosylate by the reaction of tropolone with 4-dimethylaminopyridine (DMAP) followed by tosyl chloride (TsCl). Tropolone tosylate is commercially available and useful for the construction of fused ring systems such as ‘azulene’ compounds.



Chemicals

Substance	Name	State	GHS Codes
C ₇ H ₆ O ₂	Tropolone	Solid	
(CH ₃) ₂ NC ₅ H ₄ N	4-Dimethylamino-pyridine (DMAP)	Solid	H315, H319, H301, H371
C ₂ H ₅ OH	Ethanol	Liquid	H225, H320
CH ₃ C ₆ H ₄ SO ₂ Cl	Tosyl Chloride (TsCl)	Solid	H314, H315, H318

Glassware and equipment

- 2 Vials (20 mL)
- 1 Spatula
- 1 Weighing balance (0.001 g)
- 2 Weighing papers
- 1 Magnetic stirrer
- 1 Magnetic stir bar (small)
- 2 Pasteur pipettes
- 1 Filter funnel (small)
- 1 Filter paper
- 1 Filtering flask
- 1 Aspirator

Procedure: Synthesis of tropolone tosylate

1. **Charge** a 20 mL vial (vial A) with tropolone (125 mg), ethanol (1.0 mL), and a small magnetic stir bar.
2. Slowly **add** 4-dimethylaminopyridine (DMAP; 126 mg) to vial A while stirring the reaction mixture.
3. After the addition of DMAP, **stir** the reaction mixture at room temperature for another 10 minutes.
4. Slowly **add** tosyl chloride (TsCl; 196 mg) while stirring the reaction mixture.
5. After the addition of TsCl, **stir** the reaction mixture at room temperature for another 50 minutes.
6. **Collect** the product by vacuum filtration using a small filter funnel. **Transfer** all the contents of vial A to the filter funnel.
7. **Wash** the product with a small amount of ethanol using a Pasteur pipette.
8. **Let** the product **dry** on the filter funnel by continuing suction for more than 10 minutes.
9. **Weigh** a 20 mL vial (vial B) and **record** the value.
10. **Transfer** the product to vial B for submission.

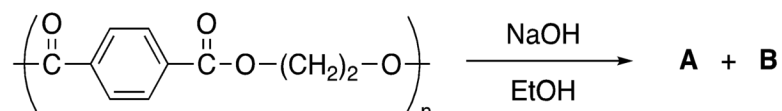
Using the above procedures, almost pure tropolone tosylate should be obtained as a light-brown solid in about 30% yield, which can be confirmed by ^1H NMR spectroscopy.

Questions

1. **Draw** the structure of the reaction intermediate resulting from the reaction between tropolone and 4-dimethylaminopyridine (DMAP). **Explain** the role of DMAP in this reaction.
2. **Describe** a procedure for the recovery of DMAP after the tosylation of tropolone.
3. What tosylation product(s) would be obtained from the above reaction if hinokitiol was used instead of tropolone? **Draw** the structure(s) of the tosylation product(s) of hinokitiol.

Task 6. Hydrolysis of poly(ethylene terephthalate): A small experiment for us, but a giant leap toward a more sustainable society

Poly(ethylene terephthalate) (PET), the raw material for PET bottles, is one of the most common plastics. In recent years, growing concern about the environmental impact of plastic waste has prompted the development of efficient technologies to recycle plastics. Chemical recycling, which is based on decomposing plastic into its raw monomer materials and reusing the recycled monomers for the production of new plastics, is an important technology because it allows the production of recycled plastics with high purity. This task explores the chemical recycling of plastics through an experiment involving the hydrolysis of PET.



Materials

- A strip of PET cut from a PET bottle, 1.00 g
- Sodium hydroxide, 3.0 g
- Ethanol, 50 mL

Substance	Name	State	GHS Codes
$(\text{C}_{10}\text{H}_8\text{O}_4)_n$	Poly(ethylene terephthalate)	Solid	-
NaOH	Sodium Hydroxide	Solid	H314, H318, H370
$\text{C}_2\text{H}_6\text{O}$	Ethanol	Liquid	H225, H320

Glassware and equipment

- Laboratory stand with clamps
- Magnetic stirrer and a stir bar
- Oil bath with a temperature controller
- Round-bottom flask (100 mL): A wide-mouthed flask is preferred.
- Round-bottom flask (20 mL)
- Reflux condenser and rubber tubes for supplying water as the coolant
- Graduated cylinder (100 mL)
- Beaker (100 mL)
- Buchner funnel and filter paper
- Vacuum flask (100 mL) and rubber adapter to connect the Buchner funnel
- Aspirator for vacuum filtration. An alternative such as a dry pump can be used.
- Pipette (10 mL)
- Petri dish
- Tweezers to handle the PET strip
- Weighing balance

Experimental procedure

Hydrolysis of PET

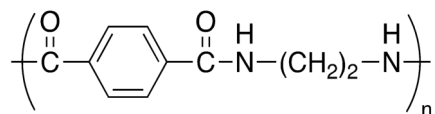
1. **Heat** the oil bath to 100 °C.
2. **Add** 5.0 g of sodium hydroxide and 30 mL of ethanolic to a 100 mL round-bottom flask in order to prepare an ethanol solution of sodium hydroxide.
3. **Weigh** a strip of PET and **place** it in the flask.
4. **Connect** the reflux condenser to the flask and run water. **Immerse** the bottom of the flask in the oil bath to start heating and refluxing. After 30 minutes, **lift** the flask from the oil bath.
5. **Remove** the residual PET from the flask using tweezers and **wash** it with a small amount of ethanol. **Place** the PET strip on a filter paper, **dry** it under air, and then **weigh** it.
6. **Filter** the suspension remaining in the flask using vacuum filtration. **Wash** the solid on the filter paper with a small amount of ethanol and **dry** it by continuing suction to obtain crude crystals of compound **A** shown in the reaction scheme.
7. **Transfer** the crude crystals of **A** on the filter paper to a petri dish and **weigh** them.

Recrystallization of A

1. **Place** the crude crystals of **A** in a 20 mL round-bottom flask and **add** 2 mL of water. **Dissolve** the crude crystals by heating the mixture to 100 °C using an oil bath. If necessary, **add** 0.5 mL of water to dissolve all the crude crystals.
2. **Allow** the solution **to cool** to room temperature. **Collect** the precipitated crystals of **A** via vacuum filtration, **wash** them with a small amount of ethanol and **dry** them with continuing suction.
3. **Transfer** the crystals of **A** to a petri dish and **weigh** them.

Questions

1. **Draw** the structural formulas of **A** and **B**.
2. **Calculate** the yield of **A** based on the amount of PET used.
3. **Calculate** the yield of **A** based on the amount of PET reacted.
4. **Draw** a reaction mechanism for the cleavage of ester bonds in the reaction of PET and NaOH.
5. This reaction is irreversible. **Describe** the reasons for this.
6. **Which would be more efficient:** The hydrolysis of PET conducted in this experiment or the hydrolysis of the polyamide shown below under the same conditions? The reasons for your answer should be also described.



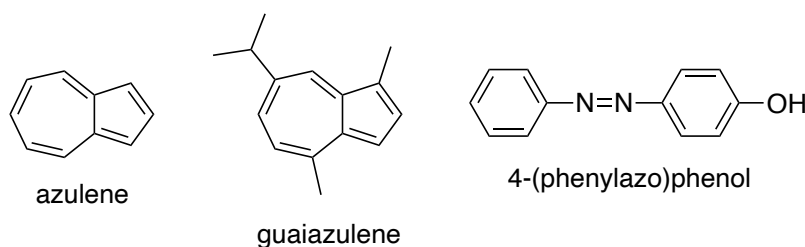
Task 7. Separation of blue and red components from a green mixture

In 1903, Tswett reported the first example of chromatography: Leaves were ground and developed on filter paper to separate pigments such as chlorophyll, carotenes, and xanthophylls. The term chromatography is derived from the Greek *chroma*, which means ‘color’, and *graphein*, which means ‘to write’. While chromatography was initially applied to colored compounds, nowadays, it is also applied to colorless compounds.

Chromatography is a very powerful method to separate the individual constituents of compound mixtures. In this task, chromatography is compared to recrystallization, which is another popular separation/purification method.

For that purpose, we will use a mixture of guaiazulene and 4-(phenylazo)phenol (henceforth denoted as the ‘mixture’) in this task. Guaiazulene is a natural pigment that is found in some essential oils. Given the special electronic structure of the azulene skeleton (*vide infra*), guaiazulene exhibits a deep blue color, which stands in stark contrast to other isomeric naphthalene derivatives. The second component of our mixture, 4-(phenylazo)phenol, is a product of one of the simplest diazo coupling reactions. Conjugated azo compounds represent an important class of chromophores, and various azo dyes have found applications in e.g. the textile and food industry.

In this task, considering the historic origins of ‘chromatography’, we will separate the two individual colored compounds from the ‘mixture’.



Chemicals

Substance	Name	State	GHS Codes
C ₁₅ H ₁₈	Guaiazulene	Solid	H302
C ₆ H ₅ N=NC ₆ H ₄ OH	4-(Phenylazo)phenol	Solid	H302, H315, H319
C ₂ H ₅ OH	Ethanol	Liquid	H225, H320
C ₆ H ₁₄	Hexane	Liquid	H225, H315, H319, H361, H335 H336, H304, H401, H372
CH ₃ COOC ₂ H ₅	Ethyl acetate	Liquid	H225, H320, H332, H335, H336
SiO ₂	Silica gel	Solid	H351, H402
	Sea sand	Solid	

Samples

A ‘mixture’ for the recrystallization; ca. 1:5 (w/w) mixture of guaiazulene and 4-(phenylazo)phenol.

A ‘mixture’ for the column chromatography; ca. 1:1 (w/w) mixture of guaiazulene and 4-(phenylazo)-phenol.

Solutions

A solution for the recrystallization; 1:1 (v/v) mixture of ethanol and hexane.

A solution to charge the sample; 1:1 (v/v) mixture of hexane and ethyl acetate.

Second eluent; 4:1 (v/v) mixture of hexane and ethyl acetate.

Glassware and equipment

- 2 Short test tubes
- 1 Test tube rack
- 5 Pasteur pipettes
- 3 Spatulas
- 1 Weighing balance (accuracy: 0.001 g)
- 1 Hot water bath
- 1 Ice bath
- 1 Graduated cylinder (50 mL)
- 1 Graduated cylinder (5 mL)
- 1 Filter funnel (small)
- 1 Filter paper
- 1 Filtering flask
- 1 Aspirator
- 1 Petri dish
- 1 Laboratory stand
- 1 Clamp
- 1 Glass column with stopcock (inner diameter: 12 mm)
- 1 Vial tube (4 mL)
- 4 Erlenmeyer flasks (100 mL)
- 1 Erlenmeyer flask (50 mL)
- 3 Funnels
- Cotton wool
- 1 Glass rod
- 2 Round-bottom flasks (100 mL)
- 1 Rotary evaporator

Procedure

Recrystallization of the 'mixture'

1. **Weigh** out a test tube and **place** ca. 0.5 g of the 'mixture' for the recrystallization into it; **weigh** the test tube again.
2. **Heat** the water bath to 80 °C.
3. **Add** 1.0 mL of the 1:1 (v/v) mixture of ethanol and hexane to the test tube. **Clamp** the test tube and **heat** it in the water bath until all of the 'mixture' has dissolved.
4. **Allow** the green solution **to cool** to room temperature. After crystals have formed, further **cool** the test tube with iced water.
5. **Place** the filter funnel on the filtering flask and **insert** the filter paper. **Connect** the filtering flask to the aspirator and **start** the suction. **Wet** the filter paper with a small amount of ethanol and press it to the filter funnel using a spatula.
6. **Add** the 1:1 mixture of ethanol and hexane to another test tube and **cool** it with iced water.
7. **Transfer** all of the precipitate onto the filter funnel with the cold ethanol-hexane mixture. **Wash** the crystals with a small amount of the cold ethanol-hexane mixture and **dry** them using continued suction.
8. **Weigh** the empty petri dish and **transfer** the product to the petri dish; **weigh** the petri dish again.

Separation of the 'mixture' by column chromatography on silica gel

Packing the silica gel column

1. Use a glass rod to loosely **insert** a small plug of cotton wool into the small glass tube just before the stopcock inside the column.
2. **Clamp** the column onto a laboratory stand. **Add** sea sand to fill the curved part on the bottom of the column.
3. **Place** silica gel (20 g) in an Erlenmeyer flask (50 mL), **add** hexane (30 mL) as the eluent, and **stir** the mixture to make a slurry.
4. Carefully **pour** the slurry into the column using a funnel.
5. **Rinse** off any silica gel adhered to the side of the column with a small amount of hexane.
6. Use something soft to gently **tap** on the side of the column to help the silica gel to settle uniformly.

Loading the sample onto the column

7. **Place** ca. 0.2 g of the 'mixture' for the column chromatography in a vial tube and **weigh** it. **Dissolve** the 'mixture' by adding a small amount of the 1:1 (v/v) mixture of hexane and ethyl acetate.
8. **Place** an Erlenmeyer flask under the column. **Open** the stopcock of the column and **lower** the eluent level to reach the top of the silica gel. Be sure that the silica gel is always covered by the eluent.
9. **Close** the stopcock and gently **load** the green solution in the vial onto the top of the silica gel using a Pasteur pipette.
10. **Open** the stopcock and **lower** the solvent level to reach the top of the silica gel.
11. **Close** the stopcock, **rinse** the vial with a small amount of the 1:1 hexane-ethyl acetate mixture, and **add** the washings onto the top of silica gel using the Pasteur pipette.
12. **Open** the stopcock and **lower** the solvent level to reach the top of the silica gel.
13. **Repeat** steps 11 and 12 one or two more times.
14. **Close** the stopcock, **place** sea sand on top of the silica gel, and **add** hexane to the column.

Eluting and collecting the sample

15. **Open** the stopcock; after collecting the first colorless fraction, **change** to the next Erlenmeyer flask to collect the first colored fraction. **Add** more hexane to the column if necessary.
16. After collecting the first colored fraction, **change** the Erlenmeyer flask to collect the subsequent colorless eluate. **Add** the 4:1 (v/v) mixture of hexane and ethyl acetate as the second eluent to the column and **continue** collecting.
17. After collecting the colorless eluate, **change** the Erlenmeyer flask to collect the second colored fraction. **Add** more of the 4:1 hexane-ethyl acetate mixture to the column if necessary. After collecting the second colored eluate, **close** the stopcock.
18. **Weigh** the empty round-bottom flasks.
19. **Transfer** each colored fraction from the Erlenmeyer flasks to individual round-bottom flasks using a funnel (use a clean funnel for each fraction).
20. **Remove** the solvent(s) from each flask using a rotary evaporator.
21. **Submit** the flask for evaluation.

Questions

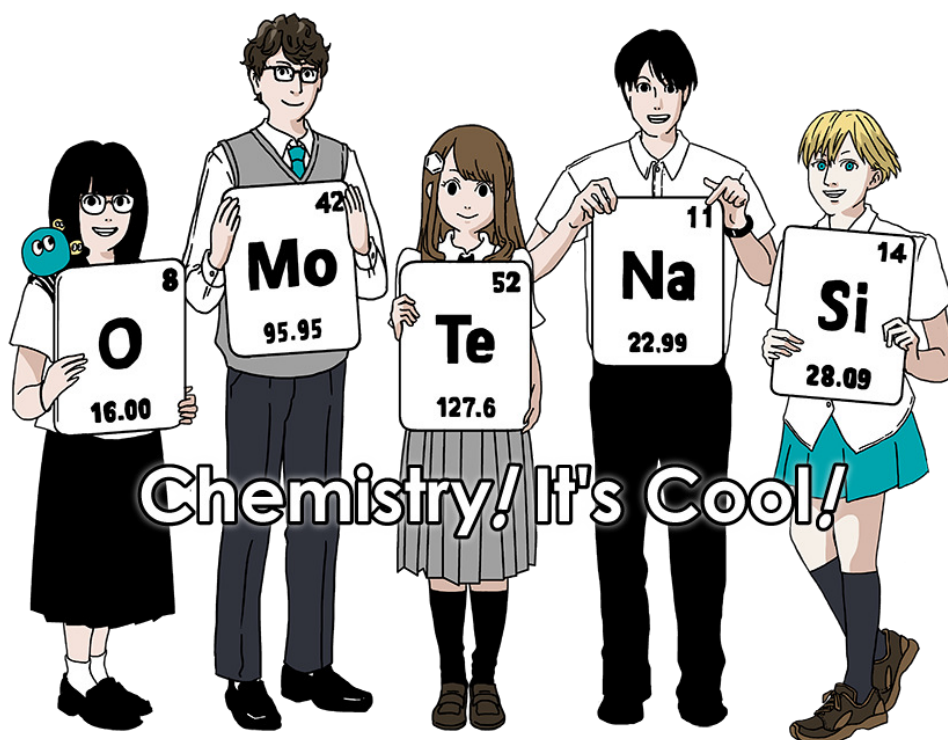
1. **Name** the constituent obtained from recrystallization.
2. **Name** the constituent in each colored fraction obtained from column chromatography.
3. **Explain** why the recovery from recrystallization is almost never quantitative.
4. Chromatography is based on the interaction of the eluite (eluted molecules) with the stationary phase (in this case: Silica gel). **Which molecule engages** in stronger interactions with silica gel, guaiazulene or 4-(phenylazo)phenol? **Name** the functional group and the type of interaction that characterizes the affinity.

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Preparatory Problems Solutions and Comments

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Preface

We are very pleased to introduce the Preparatory Problems for the 53rd International Chemistry Olympiad. These problems cover a wide range of challenging and important topics in modern chemistry. We hope that both students and their mentors will enjoy solving these problems and prepare for the Olympics. The problems include 6 topics of advanced difficulty for the Theoretical part and 3 topics of advanced difficulty for the Practical part, in addition to the subjects normally covered in high school chemistry courses. These topics are explicitly listed under "Fields of Advanced Difficulty" and their applications are shown in the preparatory problems consisting of 31 theoretical problems and 6 practical tasks. The solutions will be emailed to the head mentor of each country by February, 2021 and will be published online in July, 2021. We welcome any comments, corrections and questions about the problems via email to:

preparatory@icho2021.org.

The International Chemistry Olympiad is a great opportunity for young people from all over the world to deepen their understanding of the wonders of chemistry, and inspire each other. At the same time, it is a wonderful opportunity to make friends around the world, and enjoy the history and culture of the host country. COVID-19 is widespread all over the world and the situation is very severe, but we hope that we can meet you in Osaka, Japan in July.

Acknowledgement

We would like to express our deepest gratitude to all the authors for their great efforts in creating both preparatory and competition problems. We would also like to thank the reviewers for their valuable comments and suggestions.

Appendix

The preparatory problems are published to help the students and the mentors prepare for the usual real IChO including the theoretical problems and the practical tasks. However, because of the pandemic of COVID-19, the Organizing Committee finally decided to hold the IChO2021 Japan as the remote IChO to ensure the safety of the participants. Since the practical tasks will not be conducted in the remote IChO2021, the practical tasks in the preparatory problems are out of use for the IChO2021. It is not necessary for the students who want to participate the IChO2021 to study and/or examine the practical tasks and the advanced skills included in the preparatory problems.

Instead of the deletion of the practical tasks from the preparatory problems, however, we moved them to the Appendix part. Even though the practical tasks will not be conducted in IChO2021, the importance of laboratory experiments does not change in the chemistry. We hope to have any opportunity where the practical tasks prepared for the IChO2021 Japan are fully utilized. The practical tasks included in the Appendix part will help such an event.

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Theoretical Problems

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Problem 1. Revision of SI unit

1-1.

$$8 \times \frac{1}{8} + 6 \times \frac{1}{2} + 4 = 8 \quad \underline{n=8}$$

1-2. $nm = a^3 d$ is modified to give:

$$\underline{d = \frac{nm}{a^3} \text{ kg m}^{-3}}$$

1-3. Combining the relationships $nm u = a^3 d$ and $u = 1/N_A$ yields:

$$w = \frac{4}{3} \pi r^3 d = \frac{4\pi r^3}{3} \frac{nm}{a^3} = \frac{4\pi r^3}{3} \frac{n}{a^3} 28.09 u = \frac{4\pi r^3}{3} \frac{n}{a^3} \frac{28.09 \times 10^{-3}}{N_A} \quad N_A = \underline{6.07 \times 10^{23}}$$

2-1. As the Avogadro and Planck constants are dependent on each other, having the Planck constant is the same as having the Avogadro constant.

■ N_A alone is sufficient □ both N_A and h are required ■ h alone is sufficient

2-2. As the Planck constant is:

$$h = 6.62607015 \times 10^{-34} \text{ kg m}^2 \text{ s}^{-1} = 6.62607015 \times 10^{-34} \times 1 \text{ kg (1 m)}^2 (1 \text{ s})^{-1},$$

we obtain:

$$1 \text{ kg} = \frac{h}{6.62607015 \times 10^{-34}} \frac{1 \text{ s}}{(1 \text{ m})^2} = 1.4755214 \times 10^{40} \frac{h \Delta \nu_{\text{Cs}}}{c^2}$$

2-3. Given that the wavelength is correlated to the frequency according to $c = \nu \lambda$, mass can be calculated by:

$$m = \frac{h}{c \lambda} = \underline{3.48 \times 10^{-36} \text{ kg}}$$

Problem 2. Does water boil or evaporate?

1. When 1 mol of liquid water evaporates to water vapor at p_0 [bar] the entropy change is ΔS_v° . The entropy of the water vapor at p_1 [bar] is by $-R \ln (p_1/p_0)$ larger than that at p_0 . Therefore, when 1 mol of liquid water evaporates to water vapor at p_1 , the change in entropy can be derived from (1) as:

$$\Delta S_v = \Delta S_v^\circ - R \ln (p_1/p_0) \quad (1')$$

2. The boiling point corresponds to the temperature where the Gibbs energy change is 0 when liquid water evaporates to water vapor at 1 bar.

From:

$$\Delta G_v = \Delta H_v^\circ - T_v \Delta S_v^\circ = 0$$

follows that:

$$T_v = \frac{\Delta H_v^\circ}{\Delta S_v^\circ} = 373.05 \text{ K} = 99.9^\circ\text{C} (100^\circ\text{C}).$$

3. The saturated vapor pressure at a given temperature is the pressure where the Gibbs energy change is 0 when water evaporates at that temperature. The Gibbs energy change when water is evaporated at a pressure p_1 and temperature T_1 can be derived from (1') as

$$\Delta G_v = \Delta H_v^\circ - T_1 \Delta S_v = \Delta H_v^\circ - T_1 (\Delta S_v^\circ - R \ln (p_1/p_0))$$

When p_1 is equal to the saturated vapor pressure:

$$\Delta H_v^\circ - T_1 (\Delta S_v^\circ - R \ln (p_1/p_0)) = 0$$

then:

$$\Delta H_v^\circ - T_1 \Delta S_v^\circ = -RT_1 \ln(p_1/p_0) \quad (2')$$

From $p_0 = 1$ bar, $T_1 = 360.15$ K, $\Delta H_v^\circ = 4.070 \times 10^4 \text{ J mol}^{-1}$, and $\Delta S_v^\circ = 1.091 \times 10^2 \text{ J K}^{-1} \text{ mol}^{-1}$, it follows that:

$$p_1 = 0.62 \text{ bar}$$

4. The Gibbs energy change when 1 mol of liquid water evaporates at 0.5 p_1 of water vapor can be derived from (1') as:

$$\begin{aligned} \Delta G_v &= \Delta H_v^\circ - T_1 \Delta S_v = \Delta H_v^\circ - T_1 (\Delta S_v^\circ - R \ln (0.5 p_1/p_0)) \\ &= \Delta H_v^\circ - T_1 \Delta S_v^\circ + RT_1 \ln(p_1) - RT_1 \ln 2 = -RT_1 \ln 2 \quad [\text{from } (2')] \end{aligned}$$

For $p_0 = 1$ bar, $T_1 = 360.15$ K, it follows that:

$$\Delta G_v = -2.07 \text{ kJ mol}^{-1}$$

5. Before moving the piston, the partial pressure of water vapor is $p_s(87^\circ\text{C}) = 0.62$ bar (c), the partial pressure of Ar is $1 - 0.62 = 0.38$ bar (b), and the volume of gas is:

$$\frac{0.10 \times 8.31 \times 10^3 \times 360.15}{0.38 \times 10^5 \text{ Pa}} = 7.88 (7.9) \text{ L (d)}.$$

Let n be the number of moles of water vapor:

$$62000 \text{ Pa} \times 7.88 \text{ L} = n \times 8.31 \times 10^3 \times 360.15 \text{ K}$$

$$n = 0.16 \text{ mol}$$

Therefore, the number of moles of liquid water is:

$$n_1 = 1.00 - 0.16 = 0.84 \text{ mol (e)}$$

When the piston is pulled back quickly and the volume is increased to 15.8 L, the partial pressures of water and Ar decrease to:

$$(\text{partial pressure of Ar}) = 0.38 \times \frac{7.88}{15.8} = 0.19 \text{ bar (f)}$$

$$(\text{partial pressure of water vapor}) = 0.62 \times \frac{7.88}{15.8} = 0.31 \text{ bar (g)}.$$

Here, as a realistic non-equilibrium state, it is assumed that the speed with which the piston is pulled back is sufficiently fast with respect to the speed with which water vaporizes.

Since the total pressure (0.5 bar) is smaller than the saturated vapor pressure of water $p_s(87^\circ\text{C}) = 0.62 \text{ bar}$, the water begins to boil. The boiling stops when the total pressure (partial pressure of Ar + partial pressure of water vapor) becomes equal to the saturated vapor pressure of water at 87°C :

$$\begin{aligned} 0.62 \text{ bar} &= 0.19 \text{ bar} + (\text{partial pressure of water vapor}) \\ (\text{partial pressure of water vapor}) &= 0.43 \text{ bar} \end{aligned}$$

Let n be the number of moles of water vapor:

$$\begin{aligned} 43000 \text{ Pa} \times 15.8 \text{ L} &= n \times 8.31 \times 10^3 \times 360.15 \text{ K} \\ n &= 0.23 \text{ mol} \end{aligned}$$

Therefore, the number of moles of liquid water is:

$$n_1 = 1.00 - 0.23 = 0.77 \text{ mol (h)}$$

After this point, evaporation proceeds until equilibrium is reached, i.e., when the partial pressure of water vapor reaches the saturation value of $p_s(87^\circ\text{C}) = 0.62 \text{ bar}$. Therefore:

$$\begin{aligned} 62000 \text{ Pa} \times 15.8 \text{ L} &= n \times 8.31 \times 10^3 \times 360.15 \text{ K} \\ n &= 0.33 \text{ mol} \end{aligned}$$

Therefore, the number of moles of liquid water is:

$$n_2 = 1.00 - 0.33 = 0.67 \text{ mol (i)}.$$

Problem 3. Molecules meet water and metals

1-1. The density of seawater is $1.02 \text{ [g cm}^{-3}] = 1.02 \times 10^{-3} \text{ [kg cm}^{-3}] \times 10^6 \text{ [cm}^3 \text{ m}^{-3}] = 1.02 \times 10^3 \text{ [kg m}^{-3}]$. The mass of a seawater column with a height of 20 m and a horizontal area of 1 m^2 is $1 \times 20 \text{ [m]} \times 1.02 \times 10^3 \text{ [kg m}^{-3}] = 2.04 \times 10^4 \text{ [kg m}^{-2}]$. Thus, the pressure exerted by this seawater column on the 1 m^2 bottom surface is $2.04 \times 10^4 \times 9.81 \text{ N m}^{-2} [= \text{Pa}] = 2.00 \text{ bar}$. Adding the atmospheric pressure of 1.01 bar to this pressure, we obtain a total pressure of 3.01 bar.

1-2. According to Henry's law, the mole fraction of nitrogen dissolved at 3.00 bar is $3.00/(8.57 \times 10^4) = 3.50 \times 10^{-5}$. The amount of water molecules in 5 L of water is $5 \text{ [kg]}/18 \text{ [g mol}^{-1}] = 0.278 \times 10^3 \text{ mol}$. Thus, the amount of dissolved nitrogen is $0.278 \times 10^3 \times 3.50 \times 10^{-5} = 9.73 \times 10^{-3} \text{ mol}$.

1-3. The amount of nitrogen dissolved in water at $P = 0.800 \text{ bar}$ is $0.8/(8.57 \times 10^4) \times 0.278 \times 10^3 = 2.60 \times 10^{-3} \text{ mol}$. Thus, the volume of nitrogen gas is $V = (9.73 \times 10^{-3} - 2.60 \times 10^{-3}) \times 8.31 \times 298.15 / (0.8 \times 10^5) = 2.21 \times 10^{-4} \text{ m}^3 = 0.221 \text{ [L]}$.

2-1. Let $n_l \text{ [mol]}$ be the amount of CO_2 molecules dissolved in the water, $n_g \text{ [mol]}$ be amount of CO_2 molecules in the gas phase, and $n_w (= V_l[L] \times \frac{1000}{18}) \text{ [mol]}$ be the amount of water molecules.

The mole fraction of CO_2 can be estimated as $x = n_l/n_w$ because $n_w \gg n_l$.

We thus obtain the following equations:

According to Henry's law, $P = k_H x = k_H n_l/n_w$; thus, $n_l = P n_w/k_H$ (1).

From the equation of the state of the gaseous part, $P(V - V_l) = n_g RT$:

$$n_g = P(V - V_l)/RT \quad (2)$$

The equation of the state for the gas initially added to the container:

$$n_0 = P_0(V - V_l)/RT \quad (3)$$

Conservation of the amount of CO_2 at the initial and equilibrated conditions gives:

$$n_0 = n_g + n_l \quad (4)$$

Substituting equations (1)–(3) into equation (4) furnishes:

$$P = n_0 / (\alpha + \beta), \quad n_l = \beta P,$$

where

$$\alpha = \frac{V - V_l}{RT} (= 3.014 \times 10^{-3}), \quad \beta = \frac{n_w}{k_H} (= 2.671 \times 10^{-2}).$$

Thus, $P = 5.07 \text{ atm}$ and $n_l = 0.135 \text{ mol}$.

2-2. The volume of CO_2 dissolved in 0.5 L of water at 0°C under 1 atm is $V = 0.135 \times 0.08201 \times 273.15 / 1.0 = 3.03 \text{ L}$. Thus, 6.06 L of CO_2 is dissolved in 1 L of water. Therefore, this solution is 6 GV carbonated water.

2-3. Following the same procedure as in Q2-1, we obtain $P = 12.1 \text{ atm}$ and $n_l = 0.119 \text{ mol}$ at 50°C .

3-1. Using similar equations to those for Q2-1 with respect to oxygen at its partial pressure of 0.21 bar, the mole fraction of dissolved oxygen is calculated to be 4.8×10^{-6} and the mass is 8.4 mg.

3-2. Let $M^{(j)}$ be the quantities (M) after replacing the atmosphere with pure argon j times.

The equation of the state for the gas phase part affords:

$$(P_A + P_O)(V - V_l) = (n_{O:g} + n_{A:g})RT$$

Henry's law for each gas: $P_A = k_{H:A} x_A = \frac{n_A}{\beta_A}$, $P_O = k_{H:O} x_O = \frac{n_O}{\beta_O}$,

where $n_{i:g}$ and $n_{i:l}$ ($i = A$ or O) are the amount of chemical species i in the gas phase and in

water, respectively, while n_W is the amount of water and $\beta_i = \frac{n_W}{k_i}$.

Conservation of the amount of oxygen before Ar replacement ($j = 0$) gives:

$$n_O^{(0)} = n_{O:g}^{(0)} + n_{O:l}^{(0)}, \text{ where } n_{O:l}^{(0)} = \beta_O P_O^{(0)} = 2.64 \times 10^{-4} \text{ mol.}$$

After the first Ar replacement ($j = 1$):

$$P_O^{(1)}(V - V_l) = n_{O:g}^{(1)}RT \text{ leads to } n_{O:g}^{(1)} = \alpha P_O^{(1)} \text{ and } n_{O:l}^{(1)} = \beta_O P_O^{(1)},$$

where $\alpha = (V - V_l)/RT$.

Because the oxygen dissolved in water before the replacement is distributed between the gas phase and water after the replacement, we obtain the relationship:

$$n_{O:l}^{(0)} = n_{O:g}^{(1)} + n_{O:l}^{(1)} = (\alpha + \beta_O)P_O^{(1)}$$

leading to $P_O^{(1)} = \frac{n_{O:l}^{(0)}}{\alpha + \beta_O} = 6.35 \times 10^{-3} \text{ [bar]}$. Thus, the oxygen dissolved in the water after the Ar replacement is:

$$n_{O:l}^{(1)} = \beta_O P_O^{(1)} = \gamma n_{O:l}^{(0)} \text{ [mol]}, \text{ where } \gamma = \frac{\beta_O}{\alpha + \beta_O} = 3.02 \times 10^{-2}$$

Consequently: $x_O^{(1)} = \frac{n_{O:l}^{(1)}}{n_W} = 1.4 \times 10^{-7}$.

3-3. As found in Q3-2, the mole fraction of oxygen decreases by a factor of γ with each argon replacement. Here, $\gamma = 3.02 \times 10^{-2}$. Thus, the mole fraction of oxygen is 4.3×10^{-9} (after the second substitution), 1.3×10^{-10} (3rd), 4.0×10^{-12} (4th), 1.2×10^{-13} (5th). Therefore, 5 replacements are required to reduce the dissolved oxygen to 1 ppt or less.

4-1. The amounts of A and B are conserved before and after equilibrium:

$$n_A^0 = n_{A:l} + n_{A:g} + n_{AB;l} \quad (1)$$

$$n_B^0 = n_{B:l} + n_{B:g} + n_{AB;l} \quad (2)$$

The equations of state for the gases give:

$$n_A^0 = \alpha P_A^0, \quad n_B^0 = \alpha P_B^0, \quad (3)$$

$$n_{A:g} = \alpha P_A, \quad n_{B:g} = \alpha P_B \quad (4), \text{ where } \alpha = (V - V_l)/RT.$$

According to Henry's law,

$$n_{A:l} = \beta_A P_A, \quad n_{B:l} = \beta_B P_B \quad (5)$$

where $\beta_i = \frac{n_W}{k_{H,i}}$ ($i = A, B$).

$$\text{From } K_{AB} = x_{AB}/x_A x_B, \quad n_{AB} = K_{AB} \beta_A \beta_B P_A P_B / n_W, \quad (6)$$

where n_W is the amount of water.

Substituting equations (3)–(6) into equations (1) and (2), we obtain:

$$\alpha P_A^0 = (\alpha + \beta_A)P_A + K_{AB} \beta_A \beta_B P_A P_B / n_W \quad (7)$$

$$\alpha P_B^0 = (\alpha + \beta_B)P_B + K_{AB} \beta_A \beta_B P_A P_B / n_W \quad (8)$$

Solving the simultaneous equations with respect to P_A and P_B , we obtain:

$$P_A = 1.75, P_B = 1.86 \text{ [bar]},$$

$$x_A = 1.75 \times 10^{-4}, x_B = 9.30 \times 10^{-5}.$$

4-2. Similarly, the mole fraction of B is calculated to be $x_B = 9.10 \times 10^{-5}$ at $P_A^0 = 10 \text{ bar}$ and $P_B^0 = 2 \text{ bar}$. Thus, this is 97.8% of the mole fraction of B in Q4-1.

5-1. Adsorption rate : $r_a = k_a PS$, desorption rate: $r_d = k_d a$

5-2. Because $r_a = r_d$ at equilibrium:

$$k_a PS = k_d a.$$

Thus:

$$\frac{a}{PS} = \frac{k_a}{k_d} = K$$

Dividing each side of the equation by S_0 and using $S = S_0 - a$ and $\theta = a/S_0$, we obtain:

$$\theta = \frac{KP}{1 + KP}$$

5-3. Solving the above equation for P , we obtain:

$$P = \frac{\theta}{K(1-\theta)}.$$

In the case of $\theta \ll 1$, P can be approximated as:

$$P = \theta/K.$$

5-4. The total amount n_t of gas molecules introduced into the container is given as:

$$n_t = \frac{P_0 V}{RT}$$

At equilibrium, the number of molecules in the gas phase (n_g) and the number of molecules adsorbed on the metal surface (n_a) are $n_g = \frac{PV}{RT}$ and $n_a = \theta S_0 A m$, respectively.

As the total number of molecules is conserved before and after equilibrium:

$$n_t = n_g + n_a$$

From these equations, we obtain $P = 58.7$ Pa and $\theta = 0.998$.

6-1. Similarly to Q5, we obtain:

$$\frac{a}{P_A S} = \frac{k_a^A}{k_d^A} = K_A \quad \frac{b}{P_B S} = \frac{k_a^B}{k_d^B} = K_B$$

Using $S = S_0 - a - b$, we obtain:

$$\theta_A = \frac{K_A P_A}{1 + K_A P_A + K_B P_B} \quad (1)$$

$$\theta_B = \frac{K_B P_B}{1 + K_A P_A + K_B P_B} \quad (2)$$

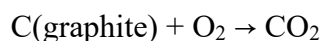
6-2. Using expressions (1) and (2), we obtain $\theta_A = 0.538$ and $\theta_B = 0.462$.

6-3. $\theta_A = K_A P_A$, $\theta_B = K_B P_B$

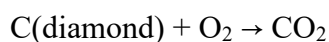
6-4. When $P_B = 60.0$ Pa, $\theta_A = 0.368$, thus, it is 68.4% of the coverage θ_A at $P_B = 30.0$ Pa.

Problem 4. Synthesis of diamonds

1.

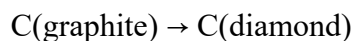


$$\Delta_c H^\circ(\text{graphite}) = -393.5 \text{ kJ mol}^{-1}$$



$$\Delta_c H^\circ(\text{diamond}) = -395.3 \text{ kJ mol}^{-1}$$

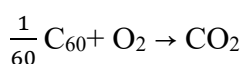
Therefore,



$$\Delta H = +1.8 \text{ kJ mol}^{-1}$$

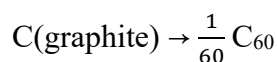
For the reaction above, the change in entropy is $\Delta S = -3.25 \text{ J K}^{-1} \text{ mol}^{-1}$.

$$\Delta G = \Delta H - T\Delta S = +2.77 \text{ kJ mol}^{-1}$$



$$\Delta_c H^\circ(\text{C}_{60}) = -\frac{25965}{60} = -432.8 \text{ kJ mol}^{-1}$$

Therefore,



$$\Delta H = +39.3 \text{ kJ mol}^{-1}$$

For the reaction above, the change in entropy is $\Delta S = +1.54 \text{ J K}^{-1} \text{ mol}^{-1}$.

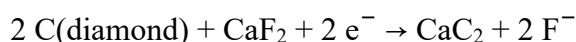
$$\Delta G = \Delta H - T\Delta S = +38.8 \text{ kJ mol}^{-1}$$

The order of stability is thus graphite > diamond > C₆₀.

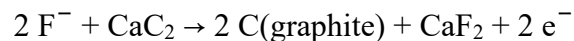
2. The reaction rate is very slow due to the high activation energy.

3.

Cathode:

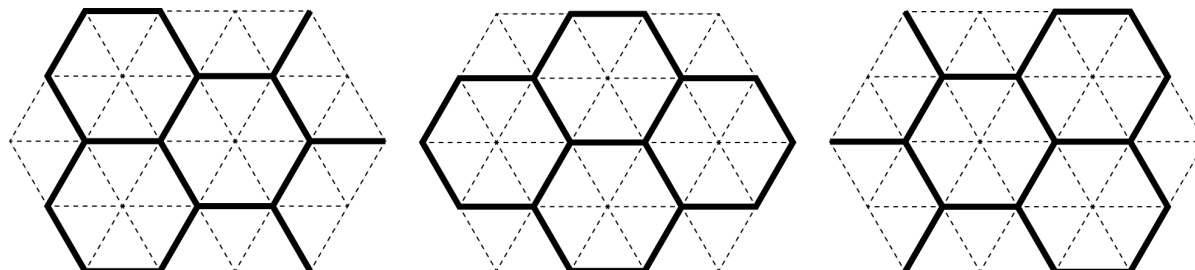


Anode:



4. The change in Gibbs free energy of the conversion reaction from diamond to graphite is $\Delta G = -nFE = -1100 - 4.64T$ (n is the number of moles of electrons transferred per 1 mole of carbon, which is $n = 1$ in this case). The thermodynamic quantities for the conversion reaction of graphite to diamond are obtained by changing the sign. By comparing the result with $\Delta G = \Delta H - T\Delta S$, the enthalpy and entropy are found to be $\Delta H = +1.10 \text{ kJ mol}^{-1}$ and $\Delta S = -4.64 \text{ J K}^{-1} \text{ mol}^{-1}$.

5.



6. Left: 3R, center: 2H, right: 1H.

7. Left: lonsdaleite, right: diamond.

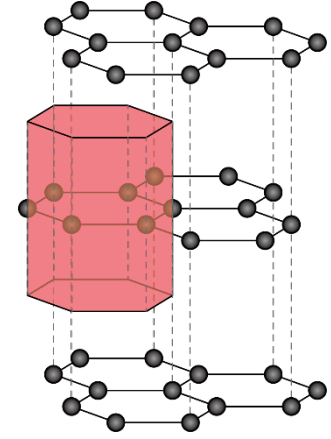
8. The area of the hexagonal cell that constitutes graphene is

$$1.42 \times (1.42 \times \sin 60^\circ) \times \frac{1}{2} \times 6 = 5.24 \text{ \AA}^2.$$

The number of carbon atoms within this hexagonal cell is two.

Based on these values, the volume occupied by two carbon atoms (see the right figure) can be calculated as $5.24 \times 3.35 = 17.55 \text{ \AA}^3$.

Therefore, the density of graphite is $\frac{12.01 \times 2 / 6.02 \times 10^{23}}{17.55 \times 10^{-24}} = 2.27 \text{ g cm}^{-3}$.



The side length of the unit cell of a diamond is $4/\sqrt{3}$ times the distance between covalently bonded carbon atoms, which can be calculated to be $3.56 \text{ \AA}$.

There are eight carbon atoms in the unit cell.

Based on these values, the volume occupied by eight carbon atoms can be calculated as $3.56^3 = 44.98 \text{ \AA}^3$.

Therefore, the density of diamond is $\frac{12.01 \times 8 / 6.02 \times 10^{23}}{44.98 \times 10^{-24}} = 3.55 \text{ g cm}^{-3}$.

9. If there is no volume change between graphite and diamond, the density of graphite and diamond should be the same. Using the results of question 8, the distance between layers can be calculated as $3.35 \times \frac{2.27}{3.55} = 2.14 \text{ \AA}$.

The distance between graphene layers is estimated to be as large as $2.78 \text{ \AA}$ even under 30 GPa (300,000 bar). Therefore, the direct conversion method requires high temperature in addition to high pressure to accelerate the reaction.

10. $v_g = v'_g \rightarrow k_g C_C = k'_g C_H, C_h = \frac{k_g}{k'_g} C_C$

11. $v_d - v'_d = v_d - k'_d \frac{k_g}{k'_g} C_C = v_d \left(1 - \frac{k'_d k_g}{k_d k'_g} \right)$

Based on this result, the conditions that the reaction constants should satisfy is given by $\frac{k'_d k_g}{k_d k'_g} < 1$.

12. Let the growth rate of the diamond be r_c . (From here on, we assume that r and A are non-dimensional normalized by the unit $\mu\text{m h}^{-1}$.)

$$r_c = A_{c,13\%} \exp \left(-\frac{E_a^c}{RT} \right) \rightarrow \ln r_c = \ln A_{c,13\%} - \frac{E_a^c}{RT}$$

Substituting in the experimental results gives:

$$\ln 30.34 = \ln A_{c,13\%} - \frac{E_a^c}{1173.15R}$$

$$\ln 63.43 = \ln A_{c,13\%} - \frac{E_a^c}{1373.15R}$$

From these equations, the value $E_a^c = 49.4 \text{ kJ mol}^{-1}$ is obtained.

13. Let the etching rate of the diamond be $r_h (> 0)$:

$$r_h = A_h \exp \left(-\frac{E_a^h}{RT} \right) \rightarrow \ln r_h = \ln A_h - \frac{E_a^h}{RT}$$

Substituting in the experimental results gives:

$$\ln 1.58 = \ln A_h - \frac{E_a^h}{1173.15R}$$

$$\ln 5.52 = \ln A_h - \frac{E_a^h}{1373.15R}$$

From these equations, the values $A_h = 8486$ and $E_a^h = 83.8 \text{ kJ mol}^{-1}$ are obtained.

14. At 1000 °C, the condition $r_c = r_h$ is fulfilled.

$$\ln A_{c,1\%} - \frac{E_a^c}{1273.15R} = \ln A_h - \frac{E_a^h}{1273.15R}$$

From this equation, the value $A_{c,1\%} = 330$ is obtained.

The condition that must be satisfied can be expressed as follows:

$$A_{c,1\%} \exp\left(-\frac{E_a^c}{RT}\right) - A_h \exp\left(-\frac{E_a^h}{RT}\right) = 0.50$$

By substituting in the calculated values above and calculating the left-hand side of the above equation with different T values, $T = 900 \text{ °C}$ is obtained.

Problem 5. Count the number of states

1.

$$W(40,60) = {}_{100}C_{40} = \frac{100!}{40! 60!}$$

Using the approximate formula:

$$100! \simeq 9.4 \times 10^{157}$$

$$40! \simeq 8.2 \times 10^{47}$$

$$60! \simeq 8.4 \times 10^{81}$$

we obtain $W(40,60) = 1.4 \times 10^{28}$. Similarly:

$$W(50,50) = {}_{100}C_{50} = \frac{100!}{50! 50!} = \frac{9.4 \times 10^{157}}{(3.1 \times 10^{64})^2} = 9.9 \times 10^{28}$$

2. As the number of states is maximized when an equal number of molecules is present in each of the two chambers A and B, $n^* = 5$ and 50, *i.e.*, the arrangements (5,5) and (50,50) are most probable for $N = 10$ and $N = 100$, respectively.

Given that each molecule has two possible locations, *i.e.*, in either of the two chambers, the total number of possible arrangements of N molecules is 2^N . Thus, the probability of the occurrence of the arrangement (n, m) is given by $P(n,m) = W(n,m)/2^N$. Consequently:

$$P(5,5) = W(5,5)/2^{10} = 252/1024 = 0.246$$

$$P(50,50) = W(50,50)/2^{100} = 1.012 \times 10^{29}/1.267 \times 10^{30} = 0.0799$$

In the case of $N = 10$, only the arrangement (5,5) falls within the specified range. In the case of $N = 100$, the following 5 arrangements are within this range: (48,52), (49,51), (50,50), (51,49), (52,48).

The numbers of states for each arrangement are:

$$W(48,52) = W(52,48) = 9.34404 \times 10^{28}$$

$$W(49,51) = W(51,49) = 9.91608 \times 10^{28}$$

$$W(50,50) = 1.01144 \times 10^{29}$$

Thus, we obtain:

$$P(48,52) = P(52,48) = 0.0737$$

$$P(49,51) = P(51,49) = 0.0782$$

$$P(50,50) = 0.0798$$

Therefore:

$$P_{total} = (0.0737 + 0.0782) \times 2 + 0.0798 = 0.384$$

This indicates that the probability of finding a state in the given n^* range is larger for $N = 100$ than for $N = 10$.

3. Using the analogy of one molecule in the container:

$$\frac{W_{AB}}{W_A} = \left(\frac{V_2}{V_1}\right)^{nN_A}$$

when n moles of molecules are present in the container, where N_A is the Avogadro constant.

Thus:

$$\Delta S = S_2 - S_1 = k_B \ln W_{AB} - k_B \ln W_A = k_B \ln \frac{W_{AB}}{W_A} = nR \ln \frac{V_2}{V_1}$$

4.

$$\Delta S = 0.30 \times 8.3 \times \ln \frac{0.40}{0.10} = 3.5 \text{ [J K}^{-1}\text{]}$$

5. The temperature, number of molecules, and volume do not change from State 1 to State 2. Thus, the entropy of the system does not change.

$$\Delta S = 0$$

6. According to the equation derived in question 3, the entropy changes upon the expansion of gases of α and β is given by:

$$\Delta S = n_{\alpha} R \ln \frac{V_A + V_B}{V_A} + n_{\beta} R \ln \frac{V_A + V_B}{V_B}$$

The volume ratios can be replaced by the ratios of the amounts of gas molecules to give:

$$\frac{V_A}{V_A + V_B} = \frac{n_{\alpha}}{n_{\alpha} + n_{\beta}}$$

$$\frac{V_B}{V_A + V_B} = \frac{n_{\beta}}{n_{\alpha} + n_{\beta}}$$

Thus:

$$\Delta S = -R(n_{\alpha} \ln \frac{n_{\alpha}}{n_{\alpha} + n_{\beta}} + n_{\beta} \ln \frac{n_{\beta}}{n_{\alpha} + n_{\beta}})$$

7. As both chambers are filled with identical molecules of type α , we cannot distinguish whether a molecule was originally present in chamber A or B after mixing. Furthermore, because the pressure is kept constant, there is no entropy change by removing the boundary wall. Therefore, the entropy does not change from State 1 to State 2.

$$\Delta S = 0$$

8. Given that a H_3CD molecule in a crystal has four different orientations, the molar residual entropy is given by:

$$S = R \ln 4 = 11.5 \text{ [J K}^{-1} \text{ mol}^{-1}\text{]}$$

- 9-1. Along the O–O axis of two adjacent oxygen atoms there are two stable positions for a hydrogen atom, and each water molecule possesses two hydrogen atoms. Thus, the number of configurations for the hydrogen atoms of one water molecule without the constraints of the ice rules is $2^2 = 4$. Thus, the number of configurations for 1 mole of water is $(2^2)^{N_A}$.

9-2. $2^2 \times 4 = 16$

9-3.

$$(\text{H}_4\text{O})^{2+} : W = 1$$

$$(\text{H}_3\text{O})^+ : W = 4$$

$$(\text{OH})^- : W = 4$$

$$\text{O}^{2-} : W = 1$$

Thus, the number of configurations satisfying the ice rules is $16 - 10 = 6$.

- 9-4. The number of configurations satisfying the ice rules in an ice crystal with one mole of water can be calculated by:

$$W = (2^2)^{N_A} \left(\frac{6}{16} \right)^{N_A} = \left(\frac{3}{2} \right)^{N_A}$$

Thus, the molar residual entropy is given by:

$$S = k_B \ln W = R \ln \frac{3}{2} = 3.37 \text{ [J K}^{-1} \text{ mol}^{-1}\text{]}$$

Problem 6. The path of chemical reactions

1.

$$T = \frac{1}{2}m_A \mathbf{v}_A^2 + \frac{1}{2}m_B \mathbf{v}_B^2 = \frac{1}{2}m_A \mathbf{v}_A^2 + \frac{1}{2}m_B \mathbf{v}_B^2 - \frac{1}{2}\mu(\mathbf{v}_A - \mathbf{v}_B)^2 + \frac{1}{2}\mu(\mathbf{v}_A - \mathbf{v}_B)^2$$

To summarize 1–3 items in the equation

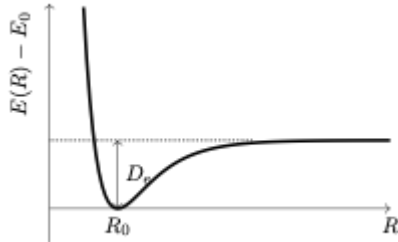
$$\begin{aligned} \frac{1}{2}m_A \mathbf{v}_A^2 + \frac{1}{2}m_B \mathbf{v}_B^2 - \frac{1}{2}\left(\frac{1}{m_A} + \frac{1}{m_B}\right)^{-1}(\mathbf{v}_A - \mathbf{v}_B)^2 &= \frac{1}{2}m_A \mathbf{v}_A^2 + \frac{1}{2}m_B \mathbf{v}_B^2 - \frac{1}{2}\frac{m_A m_B}{m_A + m_B}(\mathbf{v}_A - \mathbf{v}_B)^2 \\ &= \frac{1}{2(m_A + m_B)} \{m_A(m_A + m_B)\mathbf{v}_A^2 + m_B(m_A + m_B)\mathbf{v}_B^2 - m_A m_B(\mathbf{v}_A - \mathbf{v}_B)^2\} \\ &= \frac{1}{2(m_A + m_B)} \{m_A^2 \mathbf{v}_A^2 + m_B^2 \mathbf{v}_B^2 + 2m_A m_B \mathbf{v}_A \mathbf{v}_B\} = \frac{1}{2(m_A + m_B)} (m_A \mathbf{v}_A + m_B \mathbf{v}_B)^2 \\ &= \frac{m_A + m_B}{2} \left(\frac{m_A \mathbf{v}_A + m_B \mathbf{v}_B}{m_A + m_B} \right)^2 \equiv \frac{1}{2}M_1 \mathbf{v}_1^2 \end{aligned}$$

Thus

$$\begin{aligned} M_1 &= m_A + m_B \\ \mathbf{v}_1 &= \frac{m_A \mathbf{v}_A + m_B \mathbf{v}_B}{m_A + m_B} \end{aligned}$$

2. $k^S < k^D$ and $R^{S_0} > R^{D_0}$

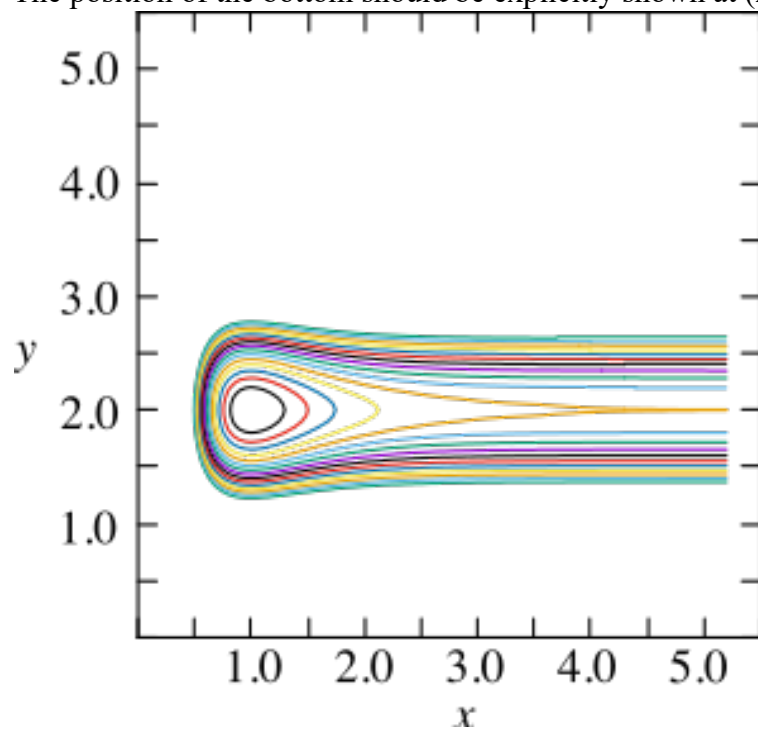
3.



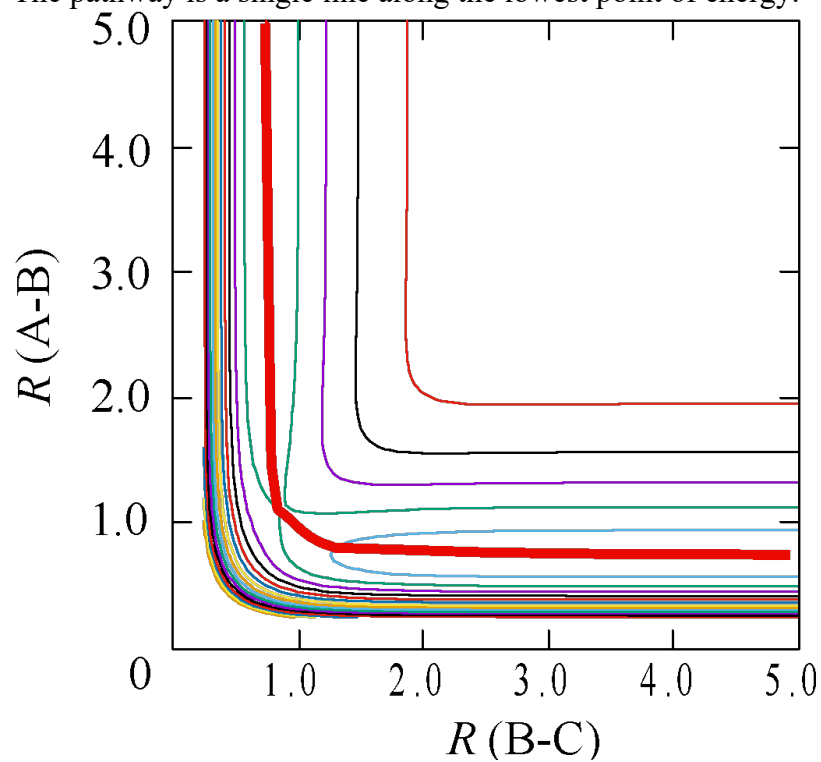
4.

- For the harmonic oscillator approximation (Eq. 4) and the Morse potential approximation (Eq. 6), the equilibrium internuclear distance is the same.
- In the region where R is long, the Morse potential approximation is lower in energy than the harmonic oscillator approximation.
- In the region where R is short, the Morse potential approximation and the harmonic oscillator approximation coincide.
- As a increases in the Morse potential approximation, the width of the well becomes narrower.

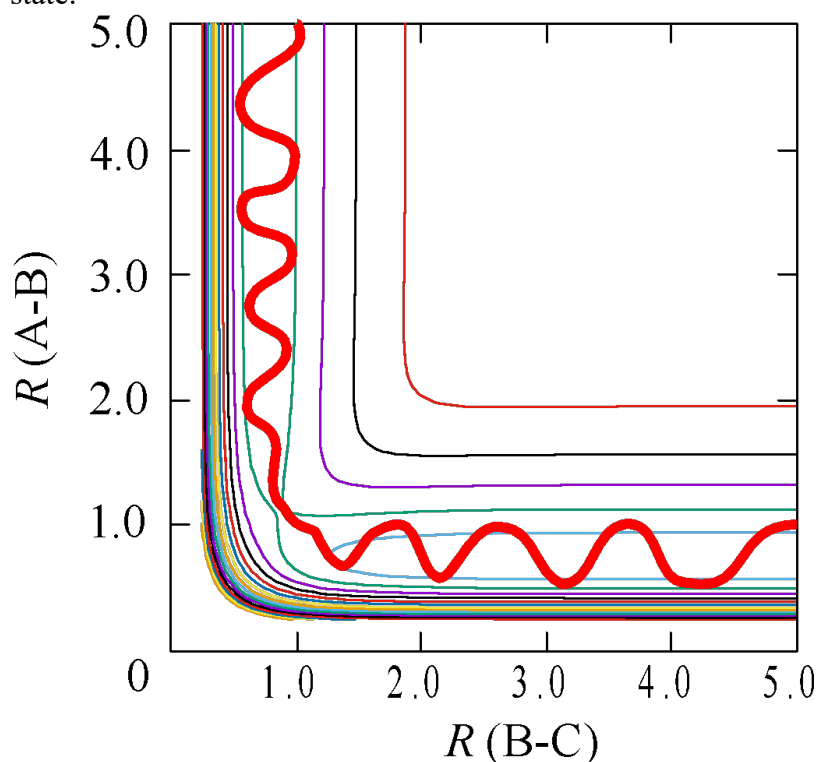
5. The position of the bottom should be explicitly shown at $(x,y)=(1,2)$.



6. The pathway is a single line along the lowest point of energy.



7. The pathway is a single line, oscillating in a direction normal to the progress of the reaction (when the reaction goes the vertical direction, the oscillation occurs horizontally or vice versa). Details of the amplitude and phase are not so important, but the amplitude is the narrowest in the transition state.



8. A: R_{CM} , B: R_{CH} , C: R_{CC} , D: R_{HF}

Problem 7. Molecular vibrations and infrared spectroscopy

- Given that the spring constant is identical in both compounds, ν_{DF} can be calculated by:

$$\nu_{\text{DF}} = \frac{1}{2\pi} \sqrt{\frac{k}{\mu_{\text{DF}}}} \text{ with a reduced mass of } \mu_{\text{DF}} = \frac{m_{\text{D}}m_{\text{F}}}{m_{\text{D}} + m_{\text{F}}}.$$

As the wavenumber, $\tilde{\nu}$, is related to the frequency, ν , via $\nu = c\tilde{\nu}$ (c : velocity of light):

$$\tilde{\nu}_{\text{DF}} = \tilde{\nu}_{\text{HF}} \sqrt{\frac{\mu_{\text{HF}}}{\mu_{\text{DF}}}} \text{ is obtained } (\tilde{\nu}_{\text{HF}} = 3953.8 \text{ cm}^{-1}).$$

Consequently, we can reach the conclusion: $\tilde{\nu}_{\text{DF}} = \underline{2866 \text{ cm}^{-1}}$.

(cf. experimentally observed position: 2896 cm^{-1})

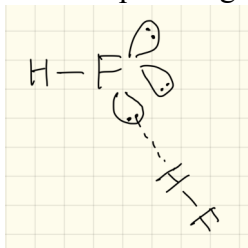
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$$q_{\text{vib}} = \sum_{v=0}^{\infty} \exp\left(-\frac{E_v}{k_{\text{B}}T}\right) = \exp\left(-\frac{h\nu}{2k_{\text{B}}T}\right) \sum_{v=0}^{\infty} \exp\left(-\frac{v h\nu}{k_{\text{B}}T}\right) = \frac{\exp\left(-\frac{h\nu}{2k_{\text{B}}T}\right)}{1 - \exp\left(-\frac{h\nu}{k_{\text{B}}T}\right)} = \frac{\exp\left(-\frac{\theta}{2T}\right)}{1 - \exp\left(-\frac{\theta}{T}\right)}$$

- When calculating the frequency in wavenumbers using $\tilde{\nu} = 1/\lambda$, take care regarding the unit conversion, especially for cm^{-1} .

$$\theta = \frac{h\nu}{k_{\text{B}}} = \frac{hc\tilde{\nu}}{k_{\text{B}}} = \underline{5689 \text{ K}}$$

- A bent structure as depicted below should be drawn, because the fluorine atom has three lone pairs with an sp^3 configuration.



L. Andrews and G.L. Johnson, *J. Phys. Chem.* **88**, 425 (1984).

- (2) k becomes smaller and m becomes larger, which results in a shift to a lower wavenumber.
- The wavenumber, where a peak appears in an IR spectrum corresponds to the energy gap between the two levels, $h\nu$, which can directly be used as ΔE in the Boltzmann factor.

$$\frac{g_1}{g_0} = \exp\left(-\frac{\Delta E}{k_{\text{B}}T}\right) = \exp\left(-\frac{h\nu}{k_{\text{B}}T}\right) = \exp\left(-\frac{hc\tilde{\nu}}{k_{\text{B}}T}\right)$$

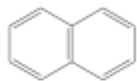
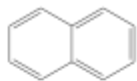
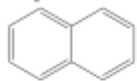
$$\text{At } 12 \text{ K: } g_1/g_0 = \underline{1.327 \times 10^{-206}}$$

$$\text{At } 25 \text{ }^\circ\text{C: } g_1/g_0 = \underline{5.174 \times 10^{-9}}$$

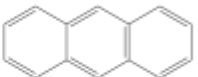
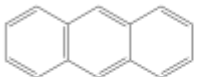
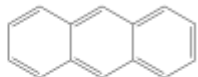
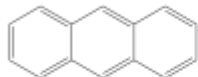
Problem 8. Quantum chemistry of aromatic molecules

1.

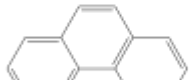
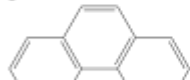
(a) naphthalene



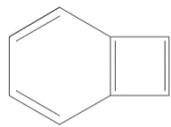
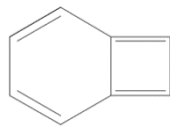
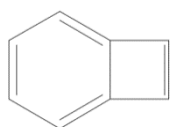
(b) anthracene



(c) phenanthrene



(d)



2. In anthracene, the resonance structure shows that the fraction of double-bond character for each of the bonds is $R_3 = 3/4$, $R_1 = 1/2$, and $R_2 = 1/4$.

$$R_D (1.34) < R_3 (1.356) < R_1 (1.410) < R_2 (1.430) < R_S (1.53)$$

3. benzene: 3; naphthalene: 5; pyrrole: 3

4. (c)

5. (a), (c), (b)

Problem 9. Protic ionic liquids



1-2. $[\text{CH}_3\text{OH}_2^+] = [\text{CH}_3\text{O}^-] = (10^{-16.7})^{1/2} = 4 \times 10^{-9} \text{ mol L}^{-1}$

2-1.

$$C_H = [\text{HB}]_0 \frac{V_0}{V_0 + V_i} + [\text{CH}^+]_{\text{sol}}$$

$$C_{\text{im}} = [\text{C}]_0 \frac{V_i}{V_0 + V_i} + [\text{CH}^+]_{\text{sol}}$$

2-2.

$$E_i = E^\circ + \frac{RT}{F} \ln [\text{HB}] = E^\circ + \frac{RT}{F} \ln \frac{[\text{HB}]_0 V_0 - [\text{C}]_0 V_i}{V_0 + V_i}$$

Based on the above equation and the numerical values provided:

$$E^\circ = 0.796 - \frac{8.314 \cdot 298.15}{96485} \ln \frac{0.35 \cdot 7.3 \times 10^{-3} - 3.2 \cdot 0.5 \times 10^{-3}}{(7.3 + 0.5) \times 10^{-3}} = 0.85 \text{ V}$$

3-1. $[\text{HB}] = K_s / [\text{C}]$

By using the approximation $C_H \approx [\text{CH}^+]$,

$$[\text{C}] = C_{\text{im}} - [\text{CH}^+] = C_{\text{im}} - C_H$$

From these equations: $[\text{HB}] = K_s / (C_{\text{im}} - C_H)$

3-2.

$$E_i = E^\circ + \frac{RT}{F} \ln [\text{HB}] = E^\circ + \frac{RT}{F} \ln \frac{K_s}{C_{\text{im}} - C_H}$$

This equation can be rearranged into the following form (Gran's plot):

$$\frac{(E_i - E^\circ)F}{RT} = \ln \frac{K_s(V_0 + V_i)}{[\text{C}]_0 V_i - [\text{HB}]_0 V_0} \rightarrow \exp \left[\frac{E_i F}{RT} \right] = \exp \left[\frac{E^\circ F}{RT} \right] \frac{K_s(V_0 + V_i)}{[\text{C}]_0 V_i - [\text{HB}]_0 V_0}$$

$$\rightarrow (V_0 + V_i) \exp \left[-\frac{E_i F}{RT} \right] = \exp \left[-\frac{E^\circ F}{RT} \right] \frac{[\text{C}]_0 V_i - [\text{HB}]_0 V_0}{K_s}$$

By substituting in the numerical values, $K_s = 5.1 \times 10^{-13} \text{ mol}^2 \text{ L}^{-2}$ is obtained.

$$\exp \left[-\frac{E^\circ F}{RT} \right] \frac{[\text{C}]_0}{K_s} = \exp \left[-\frac{0.85 \cdot 96485}{8.314 \cdot 298.15} \right] \frac{3.2}{K_s} = 0.0271 \rightarrow K_s = 5.1 \times 10^{-13} \text{ mol}^2 \text{ L}^{-2}$$

4-1. When $\text{pH} = 9.27 (= \text{p}K_a)$, $f_a = 0.50$.

$$1/2 = 1 - \exp(-0.50 k' t)$$

By solving the equation for t : $t = 28 \text{ s}$.

4-2. $1/3 = 1 - \exp(-f_a k' 500)$

By solving the equation for f_a : $f_a = 1.62 \times 10^{-2}$.

$$K_a = \frac{[\text{R}^1 - \text{NH}_2][\text{H}_3\text{O}^+]}{[\text{R}^1 - \text{NH}_3^+]} \approx f_a [\text{H}_3\text{O}^+] = 10^{-9.27}$$

By solving the equation for $[\text{H}_3\text{O}^+]$: $[\text{H}_3\text{O}^+] = 3.26 \times 10^{-8}$ and $\text{pH} = 7.49$.

[Note] Proof of eq. 12 (for mentors only, students do not have to calculate by themselves):

$$\begin{aligned}\frac{d[\text{NHCO}]}{dt} &= ([\text{R}^1-\text{NH}_2]_0 + [\text{R}^1-\text{NH}_3^+]_0)k[\text{R}^2-\text{CO}-\text{NHS}]f_a \exp(-k[\text{R}^2-\text{CO}-\text{NHS}]f_a t) \\ &= [\text{R}^1-\text{NH}_2]_0 k[\text{R}^2-\text{CO}-\text{NHS}] \exp(-k[\text{R}^2-\text{CO}-\text{NHS}]f_a t) \\ &= k[\text{R}^1-\text{NH}_2][\text{R}^2-\text{CO}-\text{NHS}]\end{aligned}$$

Note that $([\text{R}^1-\text{NH}_2]_0 + [\text{R}^1-\text{NH}_3^+]_0)f_a = [\text{R}^1-\text{NH}_2]_0$.

5-1.

$$K_a^C = \frac{[\text{C}][\text{HB}]}{[\text{CH}^+]} = 10^{-14.90}$$

Let $[\text{HB}] = x$,

$$\frac{x^2}{(6.00 \times 10^{-3} - x)} \approx \frac{x^2}{6.00 \times 10^{-3}} = 10^{-14.90}$$

By solving the equation for x : $x = 2.75 \times 10^{-9} \text{ mol L}^{-1}$.

5-2. $[\text{R}^1-\text{NH}_2]_0$ is calculated to be $10.00 \times 10^{-3} \text{ mol L}^{-1}$.

$$K_a^A = \frac{[\text{R}^1-\text{NH}_2][\text{HB}]}{[\text{R}^1-\text{NH}_3^+]} = \frac{(10.00 \times 10^{-3} - [\text{R}^1-\text{NH}_3^+])[\text{HB}]}{[\text{R}^1-\text{NH}_3^+]} = 10^{-16.40}$$

By solving the equation for $[\text{R}^1-\text{NH}_3^+]$ with $[\text{HB}] = 5.39 \times 10^{-17} \text{ mol L}^{-1}$,

$[\text{R}^1-\text{NH}_3^+] = 5.75 \times 10^{-3} \text{ mol L}^{-1}$ is obtained.

$[\text{R}^1-\text{NH}_2] = 10.00 \times 10^{-3} \text{ mol L}^{-1} - [\text{R}^1-\text{NH}_3^+] = 4.25 \times 10^{-3} \text{ mol L}^{-1}$.

$$K_a^C = \frac{[\text{C}][\text{HB}]}{[\text{CH}^+]} = \frac{(6.00 \times 10^{-3} - [\text{CH}^+])[\text{HB}]}{[\text{CH}^+]} = 10^{-14.90}$$

By solving the equation for $[\text{CH}^+]$, $[\text{CH}^+] = 2.46 \times 10^{-4} \text{ mol L}^{-1}$.

$[\text{C}] = 6.00 \times 10^{-3} \text{ mol L}^{-1} - [\text{CH}^+] = 5.75 \times 10^{-3} \text{ mol L}^{-1}$.

The result shows that $[\text{C}] = [\text{R}^1-\text{NH}_3^+]$, which means that all the protons dissociated from CH^+ are transferred to R^1-NH_2 .

5-3. Solve the following simultaneous equations. Note that $2.00 \times 10^{-3} \text{ mol L}^{-1}$ of R^1-NH_2 is consumed by the reaction between R^1-NH_2 and $\text{R}^2-\text{CO}-\text{NHS}$, which generates $2.00 \times 10^{-3} \text{ mol L}^{-1}$ of protons. Therefore, the total proton concentration becomes 6.00×10^{-3} (concentration of CH^+/B^- solution) + $2.00 \times 10^{-3} = 8.00 \times 10^{-3} \text{ mol L}^{-1}$.

$$K_a^A = \frac{[\text{R}^1-\text{NH}_2][\text{HB}]}{[\text{R}^1-\text{NH}_3^+]} = \frac{(8.00 \times 10^{-3} - [\text{R}^1-\text{NH}_3^+])[\text{HB}]}{[\text{R}^1-\text{NH}_3^+]} = 10^{-16.40} \quad (20)$$

$$K_a^C = \frac{[\text{C}][\text{HB}]}{[\text{CH}^+]} = \frac{(6.00 \times 10^{-3} - [\text{CH}^+])[\text{HB}]}{[\text{CH}^+]} = 10^{-14.90} \quad (21)$$

$$[\text{R}^1-\text{NH}_3^+] + [\text{CH}^+] + [\text{HB}] \approx [\text{R}^1-\text{NH}_3^+] + [\text{CH}^+] = 8.00 \times 10^{-3} \quad (22)$$

By substituting eq. 22 into eq. 21, the following is obtained:

$$[\text{R}^1-\text{NH}_3^+][\text{HB}] = 1.007 \times 10^{-17} - 10^{-14.9}[\text{R}^1-\text{NH}_3^+] + 2.00 \times 10^{-3}[\text{HB}] \quad (23)$$

By substituting eq. 23 into eq. 20, the following is obtained:

$$[\text{HB}] = 1.679 \times 10^{-15} - 2.032 \times 10^{-13}[\text{R}^1-\text{NH}_3^+] \quad (24)$$

By substituting eq. 24 into eq. 23, the following is obtained:

$$2.032 \times 10^{-13}[\text{R}^1-\text{NH}_3^+]^2 - 3.344 \times 10^{-15}[\text{R}^1-\text{NH}_3^+] + 1.343 \times 10^{-17} = 0 \quad (25)$$

By solving eq. 25, $[\text{R}^1-\text{NH}_3^+] = 6.96 \times 10^{-3} \text{ mol L}^{-1}$ is obtained.

$[\text{R}^1-\text{NH}_2] = 8.00 \times 10^{-3} \text{ mol L}^{-1} - [\text{R}^1-\text{NH}_3^+] = 1.04 \times 10^{-3} \text{ mol L}^{-1}$.

By substituting these values into eq. 20, $[\text{HB}] = 2.65 \times 10^{-16} \text{ mol L}^{-1}$ is obtained.

By substituting these values into eq. 21, $[\text{CH}^+] = 1.04 \times 10^{-3} \text{ mol L}^{-1}$ is obtained.
 $[\text{C}] = 6.00 \times 10^{-3} \text{ mol L}^{-1} - [\text{CH}^+] = 4.96 \times 10^{-3} \text{ mol L}^{-1}$.

The result shows that $[\text{R}^1\text{-NH}_3^+] = [\text{C}] + 2.00 \times 10^{-3} \text{ mol L}^{-1}$, which means that all the protons dissociated from CH^+ and the protons generated by the reaction ($2.00 \times 10^{-3} \text{ mol L}^{-1}$) are transferred to $\text{R}^1\text{-NH}_2$.

5-4. From eq. 18, $[\text{HB}] = K_a^{\text{C}} [\text{CH}^+] / [\text{C}]$

(By rearranging the above equation, the Henderson–Hasselbalch equation is obtained:

$$\text{pH} = \text{p}K_a^{\text{C}} - \log([\text{CH}^+] / [\text{C}])$$

5-5. $1/3 = 1 - \exp(-f_a k' 2000)$

By solving the equation for f_a : $f_a = 0.253$.

$$K_a^{\text{A}} = \frac{[\text{R}^1\text{-NH}_2][\text{HB}]}{[\text{R}^1\text{-NH}_3^+]} = \frac{0.253[\text{HB}]}{1 - 0.253} = 10^{-16.40}$$

By solving the equation for $[\text{HB}]$, $[\text{HB}] = 1.173 \times 10^{-16}$.

From the equation of Q5-4, $[\text{C}] / [\text{CH}^+] = 10.73$ and $[\text{C}] = 1.07 \text{ mol L}^{-1}$ are obtained.

Problem 10. The Yamada universal indicator

1-1. At pH = 2.00, only the protonated form is present. At pH = 12.00, only the deprotonated form is present. For example, the molar absorption coefficient of the protonated form at 420 nm can be calculated using the absorbance at pH = 2.00 as follows:

$$\varepsilon(420 \text{ nm}) \cdot 200 \times 10^{-6} \text{ mol L}^{-1} \cdot 1 \text{ cm} = 1.74 \rightarrow \varepsilon(420 \text{ nm}) = 8.7 \times 10^3 \text{ mol}^{-1} \text{ L cm}^{-1}$$

The other molar absorption coefficients are calculated in a similar way (unit: $\text{mol}^{-1} \text{ L cm}^{-1}$).

Wavelength	420 nm	501 nm	520 nm
Protonated	8.7×10^3	3.5×10^3	1.8×10^3
Deprotonated	3.0×10^3	3.5×10^3	5.3×10^3

1-2. Let the concentration of the protonated form be $x \text{ mol L}^{-1}$ and let that of the deprotonated form be $y \text{ mol L}^{-1}$. Using the conditions given in the problem, the following two equations are obtained:

$$8.7 \times 10^3 x + 3.0 \times 10^3 y = 1.13$$

$$1.8 \times 10^3 x + 5.3 \times 10^3 y = 0.52$$

By solving these equations, the values $x = 1.09 \times 10^{-4}$ and $y = 0.61 \times 10^{-4}$ are obtained. From the definition of the acid dissociation constant of BTB:

$$10^{-7.1} = [\text{H}^+] y/x, [\text{H}^+] = 1.41 \times 10^{-7} \text{ mol L}^{-1} \rightarrow \text{pH} = 6.85$$

1-3, 4.

The pH does not matter, because 501 nm corresponds to the isosbestic point of BTB. The concentration of the indicator of the solution used in Q1-2 is $x + y = 1.70 \times 10^{-4} \text{ mol L}^{-1}$. Therefore, the absorbance at 501 nm before dilution is 0.595. After the five-fold dilution, the absorbance is 0.119.

2. As examples, let us focus on the absorbance values that are highlighted in the following table:

		Wavelength [nm]					
Color		400	450	500	550	600	650
pH = 1.0	Red	0.236	0.407	0.655	0.609	0.028	0.000
(1)	Yellow	0.323	0.455	0.460	0.352	0.018	0.002
(2)	Green	0.435	0.440	0.176	0.121	0.179	0.089
(3)	Blue	0.466	0.360	0.645	1.979	0.673	0.275
pH = 12.0	Purple	0.490	0.384	0.793	2.498	0.701	0.276

The concentrations of the indicators in the final solutions are as follows (unit: mol L^{-1}):

Indicator	TB	MR	BTB	PP
Concentration	3.572×10^{-6}	1.547×10^{-5}	2.669×10^{-5}	1.047×10^{-4}

(1) The pH of the solution is estimated to be 3–6 because the color of the solution is yellow. In this pH region, it is reasonable to assume that all the TB and PP exist as HA^- . Most of the BTB will exist as HA^- , although there may be a small amount of A^{2-} . Therefore, it is only necessary to focus on the $\text{HA}^-/\text{A}^{2-}$ ratio of MR. In principle, we can calculate this ratio using any wavelength. Because the molar absorption coefficients of the HA^- and A^{2-} forms of BTB are the same at 500 nm, we can ignore the $\text{HA}^-/\text{A}^{2-}$ ratio of BTB by using the absorbance at 500 nm. The contributions to the absorbance of the solution at 500 nm from TB, BTB, and PP are as follows:

TB: $\varepsilon(\text{HA}^-, 500 \text{ nm}) = 3000$, concentration: $3.572 \times 10^{-6} \text{ mol L}^{-1} \rightarrow$ Absorbance: 0.011

BTB: $\varepsilon(500 \text{ nm}) = 3500$, concentration: $2.669 \times 10^{-5} \text{ mol L}^{-1} \rightarrow$ Absorbance: 0.093

PP: $\varepsilon(\text{HA}^-, 500 \text{ nm}) = 0$, concentration: $1.047 \times 10^{-4} \text{ mol L}^{-1} \rightarrow$ Absorbance: 0.000

From these results, the absorbance at 500 nm originating from MR can be calculated to be $0.460 - 0.011 - 0.093 = 0.356$.

By considering the concentration of the protonated form of MR, $[HA^-]_{MR}$, and that of the deprotonated form, $[A^{2-}]_{MR}$, which is $1.547 \times 10^{-5} \text{ mol L}^{-1} - [A^{2-}]_{MR}$, the following equation is obtained:

$$35000 [HA^-]_{MR} + 4000 (1.547 \times 10^{-5} - [HA^-]_{MR}) = 0.356$$

By solving the above equation, the values $[HA^-]_{MR} = 9.49 \times 10^{-6} \text{ mol L}^{-1}$ and $[A^{2-}]_{MR} = 5.98 \times 10^{-6} \text{ mol L}^{-1}$ are obtained.

By substituting these results into the definition of the acid dissociation constant of MR:

$$10^{-5.1} = [H^+] [A^{2-}]_{MR} / [HA^-]_{MR} \rightarrow [H^+] = 1.26 \times 10^{-5} \text{ mol L}^{-1}, \text{pH} = 4.9$$

- (2) The pH of the solution is estimated to be 6–8 because the color of the solution is green. In this pH region, it is reasonable to assume that all the PP exists as HA^- . However, it is difficult to estimate the ratios of the protonated forms of the other indicators in this pH region. From Table 4, we can see that the absorbance at 650 nm is governed by the deprotonated form of BTB. Although the A^{2-} form of TB also contributes to the absorption, this contribution will be negligible because the concentration of TB is one order of magnitude smaller than that of BTB.

The following equation is then obtained for the concentration of the deprotonated form of BTB, $[A^{2-}]_{BTB}$:

$$10000 [A^{2-}]_{BTB} = 0.089$$

By solving the above equation, the values $[A^{2-}]_{BTB} = 8.9 \times 10^{-6} \text{ mol L}^{-1}$ and $[HA^-]_{BTB} = 2.669 \times 10^{-5} \text{ mol L}^{-1} - [A^{2-}]_{BTB} = 1.78 \times 10^{-5} \text{ mol L}^{-1}$ are obtained.

By substituting these results into the definition of the acid dissociation constant of BTB:

$$10^{-7.1} = [H^+] [A^{2-}]_{BTB} / [HA^-]_{BTB} \rightarrow [H^+] = 1.59 \times 10^{-7} \text{ mol L}^{-1}, \text{pH} = 6.8$$

From this pH, the ratio of TB that exists in the form of A^{2-} can be calculated to be 0.8%. This confirms that the absorption of the A^{2-} form of TB at 650 nm is negligible.

- (3) The pH of the solution is estimated to be 8–11 because the color of the solution is blue. Additionally, based on the significant increase of the absorbance at 500 nm originating from the A^{2-} form of PP, the pH of the solution is estimated to be 10–11. In this pH region, it is reasonable to assume that all TB, MR, and BTB exist as A^{2-} . Therefore, it is only necessary to focus on the HA^-/A^{2-} ratio of PP. Similar to the case of Q2-1, let us use the absorbance at 500 nm so that we can ignore the HA^-/A^{2-} ratio of BTB. The contributions to the absorbance of the solution at 500 nm from TB, MR, and BTB are as follows:

TB: $\varepsilon (A^{2-}, 500 \text{ nm}) = 3500$, concentration: $3.572 \times 10^{-6} \text{ mol L}^{-1} \rightarrow$ Absorbance: 0.013

MR: $\varepsilon (A^{2-}, 500 \text{ nm}) = 4000$, concentration: $1.547 \times 10^{-5} \text{ mol L}^{-1} \rightarrow$ Absorbance: 0.062

BTB: $\varepsilon (500 \text{ nm}) = 3500$, concentration: $2.669 \times 10^{-5} \text{ mol L}^{-1} \rightarrow$ Absorbance: 0.093

From these results, the absorbance at 500 nm originating from PP can be calculated to be $0.645 - 0.013 - 0.062 - 0.093 = 0.477$.

The following equation is then obtained for the concentration of the deprotonated form of PP, $[A^{2-}]_{PP}$:

$$6000 [A^{2-}]_{PP} = 0.477$$

By solving the above equation, the values $[A^{2-}]_{PP} = 7.95 \times 10^{-5} \text{ mol L}^{-1}$ and $[HA^-]_{PP} = 1.047 \times 10^{-4} \text{ mol L}^{-1} - [A^{2-}]_{PP} = 2.52 \times 10^{-5} \text{ mol L}^{-1}$ are obtained.

By substituting these results into the definition of the acid dissociation constant of PP:

$$10^{-9.7} = [H^+] [A^{2-}] / [HA^-] \rightarrow [H^+] = 6.32 \times 10^{-11} \text{ mol L}^{-1}, \text{pH} = 10.2$$

Problem 11. Silver electroplating

1. Because $[\text{Ag}^+]$ and $[\text{Ag}(\text{OH})(\text{CN})^-]$ are significantly lower than the concentrations of the other three species, these two will be considered later.

The three highest concentrations are:

$$[\text{Ag}(\text{CN})_2^-] = C_{\text{Ag,tot}} \frac{\beta_2[\text{CN}^-]^2}{\beta_2[\text{CN}^-]^2 + \beta_3[\text{CN}^-]^3 + \beta_4[\text{CN}^-]^4} = C_{\text{Ag,tot}} \frac{1}{1 + \frac{\beta_3}{\beta_2}[\text{CN}^-] + \frac{\beta_4}{\beta_2}[\text{CN}^-]^2}$$

$$= C_{\text{Ag,tot}} \frac{1}{1 + 10^{1.0} + 10^{0.4}} = 0.07 \text{ mM}$$

$$[\text{Ag}(\text{CN})_3^{2-}] = C_{\text{Ag,tot}} \frac{\beta_3[\text{CN}^-]^3}{\beta_2[\text{CN}^-]^2 + \beta_3[\text{CN}^-]^3 + \beta_4[\text{CN}^-]^4} = C_{\text{Ag,tot}} \frac{\frac{\beta_3}{\beta_2}[\text{CN}^-]}{1 + \frac{\beta_3}{\beta_2}[\text{CN}^-] + \frac{\beta_4}{\beta_2}[\text{CN}^-]^2}$$

$$= C_{\text{Ag,tot}} \frac{10^{1.0}}{1 + 10^{1.0} + 10^{0.4}} = 0.74 \text{ mM}$$

$$[\text{Ag}(\text{CN})_4^{3-}] = C_{\text{Ag,tot}} \frac{\beta_4[\text{CN}^-]^4}{\beta_2[\text{CN}^-]^2 + \beta_3[\text{CN}^-]^3 + \beta_4[\text{CN}^-]^4} = C_{\text{Ag,tot}} \frac{\frac{\beta_4}{\beta_2}[\text{CN}^-]^2}{1 + \frac{\beta_3}{\beta_2}[\text{CN}^-] + \frac{\beta_4}{\beta_2}[\text{CN}^-]^2}$$

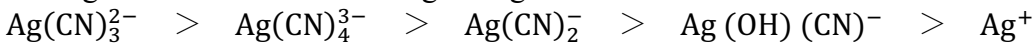
$$= C_{\text{Ag,tot}} \frac{10^{0.4}}{1 + 10^{1.0} + 10^{0.4}} = 0.19 \text{ mM}$$

The relative concentrations of $[\text{Ag}^+]$ and $[\text{Ag}(\text{OH})(\text{CN})^-]$ can be addressed with the following equation:

$$K_{\text{OHCN}} = 10^{13.20} = \frac{[\text{Ag}(\text{OH})(\text{CN})^-]}{[\text{Ag}^+][\text{CN}^-][\text{OH}^-]} = \frac{[\text{Ag}(\text{OH})(\text{CN})^-]}{[\text{Ag}^+]} \quad (\because [\text{CN}^-] = [\text{OH}^-] = 1.00 \text{ M})$$

Therefore, $[\text{Ag}(\text{OH})(\text{CN})^-] \gg [\text{Ag}^+]$.

Putting the above information together gives:



The dissolved species with the highest concentration is $[\text{Ag}(\text{CN})_3^{2-}] = 0.74 \text{ mM}$.

2. $\text{Ag}(\text{CN})_3^{2-} + \text{e}^- \rightleftharpoons \text{Ag}(\text{s}) + 3\text{CN}^-$

$$E^\circ = 0.799 - \frac{RT}{nF} \ln \beta_3$$

$$= -0.467 \text{ [V]}$$

3. At the upper limit of $[\text{CN}^-]$, $[\text{Ag}(\text{CN})_3^{2-}] = [\text{Ag}(\text{CN})_4^{3-}]$
 $\beta_3[\text{CN}^-]^3 = \beta_4[\text{CN}^-]^4$

$$[\text{CN}^-] = \frac{\beta_3}{\beta_4} = 10^{0.60} = 4.0 \text{ M}$$

At the lower limit, $[\text{Ag}(\text{CN})_2^-] = [\text{Ag}(\text{CN})_4^{3-}]$

(note: $[\text{Ag}(\text{CN})_2^-] = [\text{Ag}(\text{CN})_3^{2-}]$ is satisfied at even lower $[\text{CN}^-]$)

$$\beta_2[\text{CN}^-]^2 = \beta_4[\text{CN}^-]^4$$

$$[\text{CN}^-] = \sqrt{\frac{\beta_2}{\beta_4}} = 10^{-0.20} = 0.63 \text{ M}$$

The $[\text{CN}^-]$ range is thus 0.63–4.0 M.

4. $\text{Ag}^+ + \text{e}^- \rightleftharpoons \text{Ag}(\text{s})$

$$E = E^\circ - \frac{RT}{F} \ln \frac{1}{[\text{Ag}^+]}$$

$$E = E^\circ - \frac{RT}{F} \ln \frac{\beta_3[\text{CN}^-]^3}{[\text{Ag}(\text{CN})_3^{2-}]}$$

$$E = 0.799 - \frac{R}{F} 298.2 \ln \frac{10^{21.4} \times 1.0^3}{0.74 \times 10^{-3}} = -0.652 \text{ [V]}$$

5. From $2\text{H}^+ + 2\text{e}^- \rightleftharpoons \text{H}_2(\text{g})$, the HER equilibrium potential is:

$$E = 0 - \frac{RT}{2F} \ln \frac{1}{[\text{H}^+]^2} = -0.0592 \text{ pH}$$

$$-0.0592 \text{ pH} \leq -0.652$$

$$\text{pH} \geq 11.0$$

6. From $p = K_{\text{H}}^{-1} [\text{HCN}(\text{aq})]$ and $[\text{HCN}(\text{aq})] = \frac{[\text{H}^+][\text{CN}^-]}{K_{\text{a}}}$

$$p = K_{\text{H}}^{-1} \frac{[\text{H}^+][\text{CN}^-]}{K_{\text{a}}} \leq 10^{-5.0}$$

$$10^{-1.0} \frac{[\text{H}^+] 10^{0.0}}{10^{-9.2}} \leq 10^{-5.0}$$

$$\text{pH} \geq 13.2$$

Problem 12. How does CO_2 in the atmosphere affect the pH value of seawater?

1. $[\text{H}^+] = [\text{OH}^-] + [\text{HCO}_3^-] + 2[\text{CO}_3^{2-}]$

$[\text{OH}^-]$ is negligible because the solution becomes acidic, and $[\text{CO}_3^{2-}]$ is also negligible because $\text{pH} \ll \text{p}K_{\text{a}2}$. Therefore,

$$[\text{H}^+] = [\text{HCO}_3^-]$$

$$[\text{H}^+] = \frac{K_{\text{a}1}[\text{H}_2\text{CO}_3]}{[\text{H}^+]}$$

$$[\text{H}^+] = \frac{K_{\text{a}1}(K_{\text{hyd}}[\text{CO}_2])}{[\text{H}^+]}$$

$$[\text{H}^+] = \frac{K_{\text{a}1}K_{\text{hyd}}(K_{\text{gas}}x_{\text{CO}_2})}{[\text{H}^+]}$$

$$[\text{H}^+] = \sqrt{K_{\text{a}1}K_{\text{hyd}}K_{\text{gas}}x_{\text{CO}_2}} = 2.5 \times 10^{-6} \text{ M}$$

$$\text{pH} = 5.60$$

$$(\text{pH} = \frac{\text{p}K_{\text{a}1} + \text{p}K_{\text{hyd}} + \text{p}K_{\text{gas}} - \log_{10}[x_{\text{CO}_2}]}{2})$$

2. The total concentration of carbon dioxide-related species is:

$$[\text{CO}_2] + [\text{H}_2\text{CO}_3] + [\text{HCO}_3^-] + [\text{CO}_3^{2-}]$$

Among these four concentrations, $[\text{CO}_3^{2-}]$ is negligible as in Q1. Moreover, $[\text{H}_2\text{CO}_3]$ can also be neglected based on the relationship $[\text{H}_2\text{CO}_3]/[\text{CO}_2] = 10^{-2.70}$. Therefore, it is sufficient to consider the quantity:

$$[\text{CO}_2] + [\text{HCO}_3^-].$$

The relationship between these two concentrations is:

$$[\text{HCO}_3^-] = \frac{K_{\text{a}1}(K_{\text{hyd}}[\text{CO}_2])}{[\text{H}^+]} = 10^{-6.35 + \text{pH}}[\text{CO}_2]$$

Using this relationship, we compare the ratio of the initial and final values of $[\text{CO}_2] + [\text{HCO}_3^-]$ for the cases where $\Delta\text{pH} = \pm 1$.

(a) In the case of $\Delta\text{pH} = +1$,

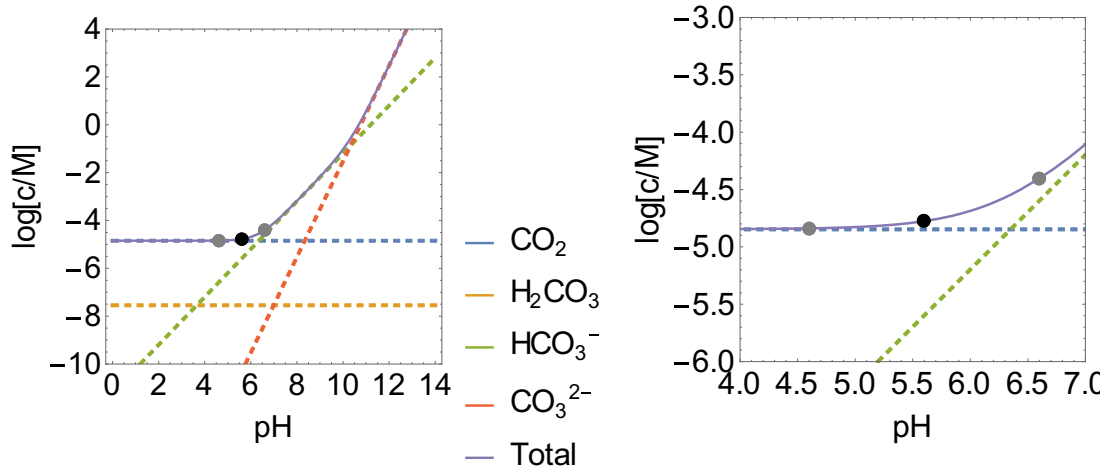
$$\frac{10^{-6.35+6.60}[\text{CO}_2] + [\text{CO}_2]}{10^{-6.35+5.60}[\text{CO}_2] + [\text{CO}_2]} = \frac{10^{+0.25} + 1}{10^{-0.75} + 1} = \frac{2.78}{1.18} = 2.4$$

Because this is more than double, the answer is (1).

(b) For $\Delta\text{pH} = -1$,

$$\frac{10^{-1.75} + 1}{10^{-0.75} + 1} = \frac{1.02}{1.18} = 0.86$$

The answer is (3).



(The total concentration significantly increases on the higher pH side, whereas the change is small on the lower pH side.)

3. Using the relationship $\text{pH} = \frac{\text{p}K_{\text{a1}} + \text{p}K_{\text{hyd}} + \text{p}K_{\text{gas}} - \log_{10} [x_{\text{CO}_2}]}{2}$ obtained in Q1,

$$\begin{aligned} \Delta \text{pH} &= \frac{\text{p}K_{\text{a1}} + \text{p}K_{\text{hyd}} + \text{p}K_{\text{gas}} - \log_{10} [2x_{\text{CO}_2}]}{2} - \frac{\text{p}K_{\text{a1}} + \text{p}K_{\text{hyd}} + \text{p}K_{\text{gas}} - \log_{10} [x_{\text{CO}_2}]}{2} \\ &= \frac{\log_{10} [x_{\text{CO}_2}] - \log_{10} [2x_{\text{CO}_2}]}{2} \\ &= \frac{-\log_{10} 2}{2} = -0.15 \end{aligned}$$

(This is the behavior of a weak acid.)

$$\text{pH} = 5.60 - 0.15 = 5.45$$

4. $[\text{H}^+] + C_{\text{C-A}} = [\text{OH}^-] + [\text{HCO}_3^-] + 2[\text{CO}_3^{2-}]$
 $[\text{CO}_3^{2-}]$ is negligible as in Q1. Moreover, because the pH is ~ 8 , $[\text{H}^+]$ and $[\text{OH}^-]$ are negligible.
 Therefore,

$$\begin{aligned} C_{\text{C-A}} &= [\text{HCO}_3^-] \\ &= \frac{K_{\text{a1}} K_{\text{hyd}} K_{\text{gas}} x_{\text{CO}_2}}{[\text{H}^+]} \\ \text{pH} &= -\log_{10} \left\{ \frac{K_{\text{a1}} K_{\text{hyd}} K_{\text{gas}} x_{\text{CO}_2}}{C_{\text{C-A}}} \right\} \\ \Delta \text{pH} &= -\log_{10} \left\{ \frac{K_{\text{a1}} K_{\text{hyd}} K_{\text{gas}} (2x_{\text{CO}_2})}{C_{\text{C-A}}} \right\} + \log_{10} \left\{ \frac{K_{\text{a1}} K_{\text{hyd}} K_{\text{gas}} x_{\text{CO}_2}}{C_{\text{C-A}}} \right\} \\ &= -\log_{10} 2 = -0.30 \end{aligned}$$

(This behavior is based on the Henderson–Hasselbalch equation, and the pH change is double that in the pure water case in Q3.)

5. $2[\text{Mg}^{2+}] + [\text{H}^+] + C_{\text{C-A}} = [\text{OH}^-] + [\text{HCO}_3^-] + 2[\text{CO}_3^{2-}]$

Similar to Q4, $[\text{CO}_3^{2-}]$, $[\text{H}^+]$, and $[\text{OH}^-]$ are negligible.

$$\begin{aligned} 2[\text{Mg}^{2+}] + C_{\text{C-A}} &= [\text{HCO}_3^-] \\ 2C_{\text{Mg}} \frac{1}{1+K_f[\text{CO}_3^{2-}]} + C_{\text{C-A}} &= [\text{HCO}_3^-] \\ 2C_{\text{Mg}} (1 - K_f[\text{CO}_3^{2-}]) + C_{\text{C-A}} &= [\text{HCO}_3^-] \\ 2C_{\text{Mg}} + C_{\text{C-A}} &= [\text{HCO}_3^-] + 2C_{\text{Mg}} K_f [\text{CO}_3^{2-}] \\ 2C_{\text{Mg}} + C_{\text{C-A}} &= \frac{K_{\text{a1}} K_{\text{hyd}} K_{\text{gas}} x_{\text{CO}_2}}{[\text{H}^+]} + 2C_{\text{Mg}} K_f \frac{K_{\text{a1}} K_{\text{hyd}} K_{\text{gas}} x_{\text{CO}_2}}{[\text{H}^+]} \frac{K_{\text{a2}}}{[\text{H}^+]} \end{aligned}$$

By solving this quadratic equation for $[H^+]$, we find $pH = 8.05$.

In the same way, with $x_{CO_2} \rightarrow 2x_{CO_2}$ we find $pH = 7.80$.

$$\Delta pH = 7.80 - 8.05 = -0.25$$

(The pH shift is milder than -0.30 due to the $MgCO_3$ equilibrium although ΔpH is still more negative than -0.2 , the threshold for coral survival).

- | | | | |
|----|------------|---------------------------|---------|
| 6. | (Region A) | $pH = (pC_{HA} + pK_a)/2$ | -0.15 |
| | (Region B) | $pH = pC_{HA}$ | -0.30 |
| | (Region C) | $pH = pK_w/2$ | 0 |

Region A.

7. -0.30 $(pH = pC_{HA} + pK_a - pC_{NaA})$.

Problem 13. How to produce sulfuric acid and dilute it without explosion

- Reaction 1: $2 \text{CuFeS}_2 + 2 \text{SiO}_2 + 4 \text{O}_2 \rightarrow \text{Cu}_2\text{S} + 2 \text{FeSiO}_3 + 3 \text{SO}_2$
 Reaction 2: $\text{Cu}_2\text{S} + \text{O}_2 \rightarrow 2 \text{Cu} + \text{SO}_2$
- When the reaction proceeds completely, 1 mol of Cu and 2 mol of SO_2 can be obtained with respect to 1 mol of CuFeS_2 .
 $\text{CuFeS}_2 = 183.527 \text{ g mol}^{-1}$
 When the reaction proceeds completely from 100 kg of CuFeS_2 ,
 Cu: $100 \times 10^3 \times (63.546 / 183.527) [\text{g}] = 3.46 \times 10^4 [\text{g}] = 34.6 [\text{kg}]$
 SO_2 : $100 \times 10^3 / 183.527 \times 2 [\text{mol}] = 1.09 \times 10^3 [\text{mol}]$
 will be obtained.
 According to the equation $PV = nRT$, $V = nRT/P = 1.09 \times 10^3 [\text{mol}] \times 8.3145 [\text{J mol}^{-1} \text{K}^{-1}] \times (273 + 25) [\text{K}] / 1.00 \times 10^5 [\text{Pa}] = 27.0 [\text{m}^3] = 2.70 \times 10^4 [\text{L}]$
Answer: 34.7 kg of Cu and $2.70 \times 10^4 \text{ L}$ of SO_2 are obtained.
- Based on the exothermic reaction $2 \text{SO}_2 + \text{O}_2 \rightleftharpoons 2 \text{SO}_3$ and according to Le Chatelier's principle, the reaction is shifted toward the product side at low temperature and high pressure.
Answer: (2)
- $2 \text{SO}_2 + \text{O}_2 \rightleftharpoons 2 \text{SO}_3$
 Let the number of moles of sulfur trioxide after the reaction be $n(\text{SO}_3) = n$. The number of moles of SO_2 and O_2 can then be calculated as $n(\text{SO}_2) = 7 - n$ and $n(\text{O}_2) = 3 - n/2$. Thus, the total number of moles of gas molecules in the reaction vessel is $n + (7 - n) + (3 - n/2) = 10 - n/2$ [mol].
 According to the equation $PV = nRT$:
 $8.60 \times 10^5 [\text{Pa}] \times 50.0 \times 10^{-3} [\text{m}^3] = (10 - n/2) [\text{mol}] \times 8.3145 [\text{J mol}^{-1} \text{K}^{-1}] \times 623 [\text{K}]$
 $n = 3.40 [\text{mol}]$
Answer: 3.40 mol
- 20 kg of 32% fuming sulfuric acid consist of:
 SO_3 : $20 \times 10^3 \times 0.32 = 6.4 \times 10^3 [\text{g}] = 6.4 \times 10^3 / 80.07 = 79.9 [\text{mol}]$
 H_2SO_4 : $20 \times 10^3 \times 0.68 = 13.6 \times 10^3 [\text{g}] = 1.36 \times 10^4 / 98.08 = 138.7 [\text{mol}]$.
 1 kg of 60% sulfuric acid consists of:
 $\text{H}_2\text{SO}_4 = 600 / 98.08 = 6.12 [\text{mol}]$ and $\text{H}_2\text{O} = 400 / 18.02 = 22.2 [\text{mol}]$.
 Let x [kg] equal the mass of 60% sulfuric acid required for the dilution:
 $79.9 + 138.7 + (6.12 \times x) = (20.0 + x) \times 10^3 \times 0.98 / 98.08$
 $x = 4.84$, Answer: 4.8 kg
- Let x [kg] equal the mass of water required for the dilution:
 $8.0 \times 10^3 \times 0.98 = (8.0 + x) \times 10^3 \times 0.60 \rightarrow x = 5.07$. Thus, 5.07 kg of water are needed for the dilution.
 Now, let $m(98)$ equal the number of moles of water required for the dilution of 1 mol of H_2SO_4 to 98%:

$$\frac{98}{18 \times m(98) + 98} = 0.98$$

$$m(98) = 0.111 [\text{mol}]$$

In this dilution process, the heat of dilution $Q_1[\text{J}]$ is calculated as follows:

$$Q_1 = \frac{7.47 \times 10^4 \times 0.111}{0.111 + 1.80} = 4340 [\text{J}]$$

Let $m(60)$ equal the number of moles of water required to dilute 1 mol of H_2SO_4 to 60%:

$$\frac{98}{18 \times m(60) + 98} = 0.60$$

$$m(60) = 3.63 \text{ mol}$$

In this dilution process, the heat of dilution Q_2 [J] is calculated as follows:

$$Q_2 = \frac{7.47 \times 10^4 \times 3.63}{3.63 + 1.80} = 4.99 \times 10^4 \text{ [J]}$$

From the values shown above, the heat of dilution when 98% sulfuric acid containing 1 mol of H_2SO_4 is diluted to 60% sulfuric acid can be calculated as:

$$Q_2 - Q_1 = 45600 \text{ [J]}$$

8.0 kg of 98% sulfuric acid contain $8.0 \times 10^3 \times 0.98 / 98 = 80.0$ mol of H_2SO_4 . Thus, the heat of dilution when 8.0 kg of 98% sulfuric acid is diluted from 98% to 60% is $Q = 45600 \times 80.0 = 3.65 \times 10^6$ [J].

Answer: 3.7×10^6 J

The produced heat Q [J] can raise the temperature of 10 kg of water (0 °C) by:

$$3.65 \times 10^6 / (10.0 \times 10^3 \times 4.18) = 87.3$$

Answer : 87 °C

Problem 14. Hydrolysis of C vs Si and the electronegativity of N vs Cl

1-1. (1) $\Delta H = (335 + 467 - 392 - 426) \text{ [kJ mol}^{-1}] = -16 \text{ [kJ mol}^{-1}]$

(2) $\Delta H = (451 + 467 - 500 - 426) \text{ [kJ mol}^{-1}] = -8 \text{ [kJ mol}^{-1}]$

1-2. Let $\text{BE}(\text{Si-Cl}^a) = x \text{ [kJ mol}^{-1}]$ and $\text{BE}(\text{Si-Cl}^e) = y \text{ [kJ mol}^{-1}]$

From Eq.(2-1): $451 \times 4 - (400 + x + 3y) = 14$; from Eq.(3): $451 \times 4 - (2x + 3y) = 50$

$x + 3y = 1390, 2x + 3y = 1754 \rightarrow x = 364, y = 342$

Answer: $\text{BE}(\text{Si-Cl}^a) = 364 \text{ [kJ mol}^{-1}]$, $\text{BE}(\text{Si-Cl}^e) = 342 \text{ [kJ mol}^{-1}]$

1-3. (1) A one-step reaction with a larger reaction barrier relative to the silicon case: (ii)

(2) A two-step reaction with a small barrier for the first step: (iii)

2-1. According to the definition equation: $(\chi_A - \chi_B)^2 = D_{AB} - (D_{AA} + D_{BB}) / 2$

$(\chi_N - \chi_H)^2 = D_{NH} - (D_{NN} + D_{HH}) / 2$

Thus, $D_{NH} = (\chi_N - \chi_H)^2 + (D_{NN} + D_{HH}) / 2 = (3.04 - 2.10)^2 + ((158 / 96.5) + (436 / 96.5)) / 2$
 $= 0.8836 + 3.0777 = 3.961 \text{ [eV]} = 382 \text{ [kJ mol}^{-1}]$

Similarly, $(\chi_{Cl} - \chi_H)^2 = D_{ClH} - (D_{ClCl} + D_{HH}) / 2$

Thus, $D_{ClCl} = 2 \times (D_{ClH} - (\chi_{Cl} - \chi_H)^2) - D_{HH} = 2 \times ((426 / 96.5) - (3.16 - 2.1)^2) - (436 / 96.5)$
 $= 2 \times 3.291 - 4.518 = 2.064 \text{ [eV]} = 199 \text{ [kJ mol}^{-1}]$

Furthermore, $(\chi_{Cl} - \chi_N)^2 = D_{NCl} - (D_{ClCl} + D_{NN}) / 2$

Thus, $D_{NCl} = (\chi_{Cl} - \chi_N)^2 + (D_{ClCl} + D_{NN}) / 2 = (3.16 - 3.04)^2 + (199 / 96.5 + 158 / 96.5) / 2 = 1.864 \text{ [eV]} = 179.9 \text{ [kJ mol}^{-1}]$

Answer: $D_{NH} = 382 \text{ [kJ mol}^{-1}]$, $D_{ClCl} = 199 \text{ [kJ mol}^{-1}]$, $D_{NCl} = 180 \text{ [kJ mol}^{-1}]$.

2-2. Answer: A: H_2NOH ; B: HCl ; C: NH_3 ; D: HOCl

Broken bonds: N-Cl (180 $\text{[kJ mol}^{-1}]$), O-H (467 $\text{[kJ mol}^{-1}]$)

Formed bonds: N-H (382 $\text{[kJ mol}^{-1}]$), Cl-O (206 $\text{[kJ mol}^{-1}]$)

Accordingly, $\Delta H = (180 + 467) - (382 + 206) = 59 \text{ [kJ mol}^{-1}]$

Answer: $Q = 59 \text{ [kJ]}$

2-3. Considering the electron distributions of nitrogen and chlorine below, their $Z^{\text{VE}}_{\text{eff}}$ values can be estimated as follows:

N: $(1s)^2(2s)^2(2p)^3$, $Z^{\text{VE}}_{\text{eff}}(\text{N}) = 7 - (0.35 \times 4) - (0.85 \times 2) = 3.9$

Cl: $(1s)^2(2s)^2(2p)^6(3s)^2(3p)^5$, $Z^{\text{VE}}_{\text{eff}}(\text{Cl}) = 6.1$

Accordingly, their Allred-Rochow electronegativities are:

$\chi_{\text{AR}}(\text{N}) = 3590 \times ((3.9 - 0.35) / 70^2) + 0.744 = 3.34$

$\chi_{\text{AR}}(\text{Cl}) = 3590 \times ((6.1 - 0.35) / 99^2) + 0.744 = 2.85$

Thus, the polarity of the N-Cl bond should be considered to be $\text{N}^-\text{-Cl}^+$, based on the Allred-Rochow electronegativities.

Problem 15. Sulfur in hot springs and volcanoes

1. Molecular weight of CdS = 144.482

CdS 9.50 [mg] = $(9.50 / 144.482) = 6.58 \times 10^{-5}$ [mol] $\rightarrow$ number of moles of H₂S

According to the reaction equation: $\text{I}_2 + 2 \text{S}_2\text{O}_3^{2-} \rightarrow 2 \text{I}^- + \text{S}_4\text{O}_6^{2-}$, the number of moles of $\text{S}_2\text{O}_3^{2-}$ is:

$$2.50 \times 10^{-2} \times (7.30 \times 10^{-3}) \times 2 = 3.65 \times 10^{-4} \text{ [mol]}$$

The mass of sulfur is: $(6.58 \times 10^{-5} + 3.65 \times 10^{-4} \times 2) \times 32.068 = 255.2 \times 10^{-4} \text{ [g]} = 25.5 \text{ [mg]}$

Accordingly, the mass of sulfur in 1 kg of hot spring water is 255 [mg kg⁻¹]

Answer: 255 mg kg⁻¹

2. $\text{H}_2\text{S} \rightleftharpoons \text{H}^+ + \text{HS}^-$; $K_1 = 9.50 \times 10^{-8}$

$$K_1 = \frac{[\text{H}^+][\text{HS}^-]}{[\text{H}_2\text{S}]}$$

$\text{HS}^- \rightleftharpoons \text{H}^+ + \text{S}^{2-}$; $K_2 = 1.30 \times 10^{-14}$

$$K_2 = \frac{[\text{H}^+][\text{S}^{2-}]}{[\text{HS}^-]}$$

pH = 8.00 corresponds to $[\text{H}^+] = 1.00 \times 10^{-8} \text{ [mol L}^{-1}\text{]}$

Accordingly,

$$[\text{HS}^-] = \frac{[\text{H}^+][\text{S}^{2-}]}{K_2} = \frac{1.00 \times 10^{-8} \times 1.00 \times 10^{-8}}{1.3 \times 10^{-14}} = 7.692 \times 10^{-3} \text{ [mol L}^{-1}\text{]}, \text{ and}$$

$$[\text{H}_2\text{S}] = \frac{[\text{H}^+][\text{HS}^-]}{K_1} = \frac{[\text{H}^+]^2[\text{S}^{2-}]}{K_1 K_2} = \frac{(1.00 \times 10^{-8})^2 \times 1.00 \times 10^{-8}}{9.5 \times 10^{-8} \times 1.3 \times 10^{-14}} = 8.097 \times 10^{-4} \text{ [mol L}^{-1}\text{]}$$

Thus, $[\text{S}^{2-}] + [\text{HS}^-] + [\text{H}_2\text{S}] = 1.00 \times 10^{-8} + 7.692 \times 10^{-3} + 8.097 \times 10^{-4} = 8.502 \times 10^{-3} \text{ [mol L}^{-1}\text{]}$

The amount of S atoms derived from S^{2-} , HS^- , and H_2S is:

$$8.502 \times 10^{-3} \times 32.068 = 2.7274 \times 10^{-1} \text{ [g]} = 272.74 \text{ [mg]}.$$

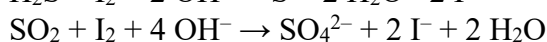
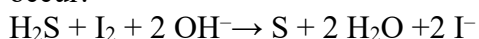
The hot spring water contains 5.90 mg of $\text{S}_2\text{O}_3^{2-}$, and the mass of the S atoms from $\text{S}_2\text{O}_3^{2-}$ is:

$$5.90 \times (64.136 / 112.1342) = 3.375 \text{ [mg]}$$

Finally, the total amount of sulfur is $272.74 + 3.375 = 276.12 \text{ [mg]}$

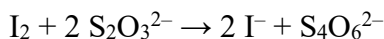
Answer: 276 mg kg⁻¹

3. When the volcanic gas is absorbed by the aqueous solution of I_2/KI , both the following reactions occur:



Thus, both H_2S and SO_2 should react with I_2 in a 1:1 ratio.

In the titration test in beaker **B**, the residual I_2 should react with sodium thiosulfate as follows:



The number of moles of sodium thiosulfate consumed is $2.00 \times 10^{-2} \times (73.0 \times 10^{-3}) = 1.46 \times 10^{-3} \text{ [mol]}$. Accordingly, the residual amount of I_2 in beaker **B** is $1.46 \times 10^{-3} / 2 = 7.30 \times 10^{-4} \text{ [mol]}$.

Based on these calculated values, the amount of residual I_2 in the initial absorption solution (1.00 L) is $7.30 \times 10^{-3} \text{ [mol]}$.

Because the absorption solution contains $2.00 \times 10^{-2} \text{ [mol L}^{-1}\text{]} \times 500 \text{ [mL]} = 1.00 \times 10^{-2} \text{ [mol]}$ of I_2 before the absorption, $1.00 \times 10^{-2} \text{ [mol]} - 7.30 \times 10^{-3} \text{ [mol]} = 2.70 \times 10^{-3} \text{ [mol]}$ of I_2 was consumed through the gas absorption.

Additionally, 41.5 mg of BaSO_4 (molecular weight: 233.3926), i.e., $(41.5 \times 10^{-3}) / 233 = 1.778 \times 10^{-4} \text{ [mol]}$ of BaSO_4 , was obtained from the reaction in beaker **A**, meaning that $1.778 \times 10^{-4} \times 10 = 1.778 \times 10^{-3} \text{ mol}$ of SO_2 reacted in the absorption solution. Accordingly, when the volcano gas was absorbed into the solution, $1.778 \times 10^{-3} \text{ mol}$ of I_2 was consumed in the absorption solution.

Thus, the amount of I_2 consumed by the reaction with H_2S is $2.70 \times 10^{-3} - 1.778 \times 10^{-3} = 9.22 \times 10^{-4}$ mol, which is the same as the amount of H_2S absorbed from the volcanic gas.

Considering the combined results, the concentrations of H_2S and SO_2 in the volcanic gas can be calculated as $9.22 \times 10^{-5} [\text{mol L}^{-1}]$ and $1.78 \times 10^{-4} [\text{mol L}^{-1}]$, respectively.

Answer: $[\text{H}_2\text{S}] = 9.22 \times 10^{-5} [\text{mol L}^{-1}]$, $[\text{SO}_2] = 1.78 \times 10^{-4} [\text{mol L}^{-1}]$.

Problem 16. Identification of unknown compounds and allotropes

1-1.

A	<u>MgH₂</u>
B	<u>Mg(OH)₂</u>
C	<u>MgO</u>
D	<u>NH₃</u>

1-2. (i) $3\text{Mg} + \text{N}_2 \rightarrow \text{Mg}_3\text{N}_2$

(ii) $\text{Mg}_3\text{N}_2 + 6\text{H}_2\text{O} \rightarrow 3\text{Mg(OH)}_2 + 2\text{NH}_3\uparrow$

1-3. 2 mol of NH₃ gas is generated from 3 mol of Mg.

$$M = M_w(\text{Mg}) \cdot n(\text{Mg}) = 24.305 \times \frac{PV}{RT} \times \frac{3}{2} = 0.18 \text{ [g]}$$

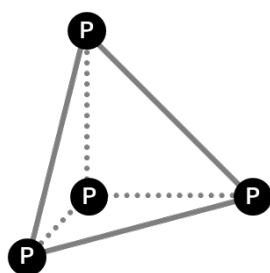
2-1.

E	<u>1</u>
F	<u>2</u>

2-2. One cubic unit cell contains 4 molecules of C₆₀, which corresponds to a total of 240 C atoms.

Their weight is $\frac{M_w(\text{C}) \times 240}{N_A}$ [g]. The volume of one cubic unit cell is $(1.41 \times 10^{-7})^3$ [cm³]. The density is therefore 1.71 [g cm⁻³].

2-3.



(Tetrahedral structure)

2-4. (iii) $\text{O}_3 + 2\text{KI} + \text{H}_2\text{O} \rightarrow \text{I}_2 + 2\text{KOH} + \text{O}_2$

2-5. N [mol] of I₂ is generated from N [mol] of ozone according to the equation in Q2-4.

In the titration, $\text{I}_2 + 2\text{Na}_2\text{S}_2\text{O}_3 \rightarrow 2\text{NaI} + \text{Na}_2\text{S}_4\text{O}_6$.

The required amount of Na₂S₂O₃ = 0.20×0.0035 [mol], therefore the amount of I₂ is 3.5×10^{-4} [mol].

2-6. (iv) $\text{NO} + \text{O}_3 \rightarrow \text{NO}_2 + \text{O}_2$

(v) $\text{NO}_2 + \text{O} \rightarrow \text{NO} + \text{O}_2$

(vi) $\text{O}_3 + \text{O} \rightarrow 2\text{O}_2$

Problem 17. Metal Oxides

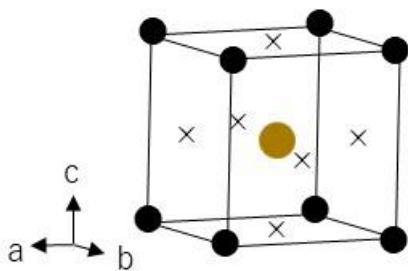
1-1. $\{1 - (4/3\pi r^3 \times 4) / (4r / 2^{1/2})^3\} \times 100 = 26\%$

1-2. Octahedral void: $(8^{1/2}r - 2r) / 2 = 0.05799\dots$ 0.0580 nm

Tetrahedral void: $(6^{1/2}r - 2r) / 2 = 0.03146\dots$ 0.0315 nm

1-3. The number of octahedral and tetrahedral voids formed by n oxide ions is n and $2n$, respectively. Therefore, the chemical formula is AB_2O_4 ($x = 1, y = 2, z = 4$).

1-4.



2-1. $\Delta H_{\text{Lexp}} = (635 + 193 + 498 \times 0.5 + 590 + 1010 + 878 - 141) = 3414 \text{ kJ mol}^{-1}$

2-2.

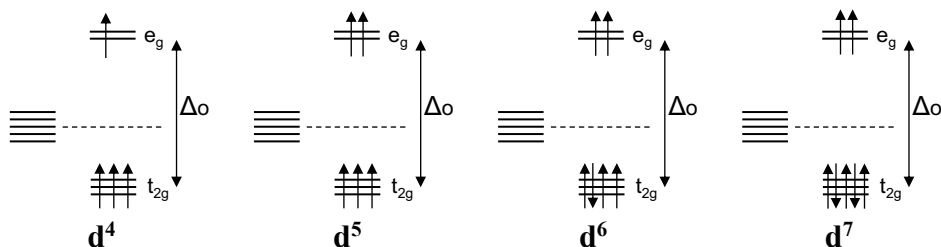
$$E_1 = -\frac{6e^2}{\pi\epsilon_0 d} \quad E_2 = +\frac{6\sqrt{2}e^2}{\pi\epsilon_0 d}$$

2-3. $\Delta H_{\text{Lcalc}} = 3.47 \times 10^3 \text{ kJ mol}^{-1}$ (answer with three significant digits).

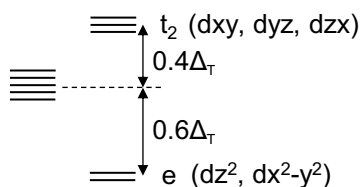
Note that the difference in ΔH_{Lexp} and ΔH_{Lcalc} is small (less than 1.5%).

Problem 18. Coordination chemistry and its application to solid-state catalysts

- The e_g orbitals are: d_{z^2} and $d_{x^2-y^2}$; the t_{2g} orbitals are: d_{xy} , d_{yz} , and d_{zx}
- The e_g orbitals: $+0.6\Delta_o$; the t_{2g} orbitals: $-0.4\Delta_o$
- CFSE d^4 : $-0.6\Delta_o$; d^5 : 0; d^6 : $-0.4\Delta_o$; d^7 : $-0.8\Delta_o$



4.



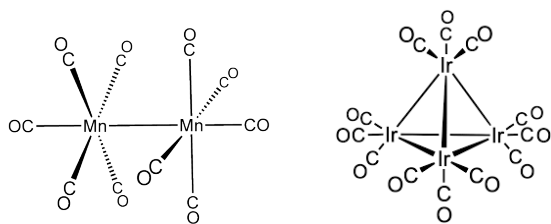
5.

$$E = h \frac{c}{\lambda} \times N_A = (6.626 \times 10^{-34}) \times (2.998 \times 10^8) \div (500 \times 10^{-9}) \times (6.022 \times 10^{23}) \times 10^{-3}$$

$$= 2.392 \times 10^2 = 2.39 \times 10^2$$

$$2.39 \times 10^2 [\text{kJ mol}^{-1}]$$

6.



Mn (group 7) supplies 7 electrons, the five CO ligands supply 10 electrons, and 1 electron is supplied by the neighboring Mn atom, thus satisfying the 18-electron rule. Ir (group 9) supplies 9 electrons, the three CO ligands supply 6 electrons, and 3 electrons are supplied by the neighboring Ir atoms, thus satisfying the 18-electron rule.

$$7-1. [\{(0.55 \text{ mL} / (R \times 273 \times 10^6 / 10^5) \text{ mL mol}^{-1}) \times 195 \text{ g mol}^{-1}\} / 0.010 \text{ g} \times 1.0] \times 100 = 47.3 \% = 47\%$$

$$7-2. \text{Number of CO molecules (A): } (0.55 \text{ mL} / (R \times 273 \times 10^6 / 10^5) \text{ mL mol}^{-1}) \times (6.02 \times 10^{23} \text{ mol}^{-1}) = 1.463 \times 10^{19} / \text{g-cat}$$

$$\text{Number of CO molecules per 1.0 g of Pt (B): } A / \{(0.01 \times 1)\} = 1.463 \times 10^{21} / \text{g-Pt}$$

$$7-3. \text{Surface area per 1 g of Pt (C)} [\text{m}^2 \text{ g}^{-1}] = B \times (8.0 \times 10^{-2} \text{ nm}^2) \times 10^{-18} = 117.0 \dots \text{ m}^2 \text{ g}^{-1} = 117 \text{ m}^2 \text{ g}^{-1}$$

7-4. α : number of Pt metal particles; r : radius of a Pt metal particle [m]; ρ : density of Pt metal [g cm^{-3}]

Surface area of 1.0 g of Pt metal (D): $\{4\pi r^2 \times \alpha\} / 0.01 = C$

Volume of 1.0 g of Pt metal (E): $\{(4/3)\pi r^3 \times \alpha\} / 0.01 = 1 / (\rho \times 10^6)$

α can be eliminated by taking (E)/(D) to obtain the following equation: $r / 3 = 1 / (C \times \rho \times 10^6)$

Since d [nm] is $2 r \times 10^9$, $d = 6000 / (C \times \rho) = 2.39 \text{ nm} = 2.4 \text{ nm}$

Problem 19. Acids and bases

1. $\text{HClO} < \text{HClO}_2 < \text{HClO}_3 < \text{HClO}_4$

The more stable the conjugate base, the stronger the acid is. The stability of the conjugate base increases with the number of resonance structures. The number of resonance structures of the conjugate base of oxoacids of chlorine increases in the order of $\text{ClO}^- < \text{ClO}_2^- < \text{ClO}_3^- < \text{ClO}_4^-$.

2. $567 + 1312 - 328 = 1551 \text{ kJ mol}^{-1}$

3. $298 + 1312 - 295 = 1315 \text{ kJ mol}^{-1}$

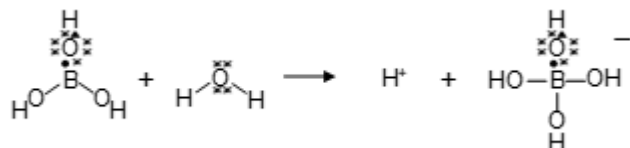
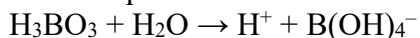
4. $|\Delta H_{\text{HF}}| > |\Delta H_{\text{HI}}|$, $\text{HF} < \text{HCl} < \text{HBr} < \text{HI}$

5. $[\text{Na}(\text{H}_2\text{O})_6]^+ < [\text{Ca}(\text{H}_2\text{O})_6]^{2+} < [\text{Zn}(\text{H}_2\text{O})_6]^{2+} < [\text{Fe}(\text{H}_2\text{O})_6]^{3+}$

The strength of aqua acids typically increases with increasing positive charge of the central metal ion and with decreasing ionic radius. The ionic radius decreases moving from left to right in any given period.

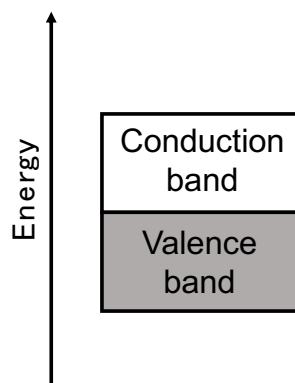
6. (i) Lewis acid: BF_3 ; Lewis base: NH_3
 (ii) Lewis acid: Ni ; Lewis base: CO
 (iii) Lewis acid: CO_2 ; Lewis base: OH^-
 (iv) Lewis acid: SiF_4 ; Lewis base: F^-

7. The boron atom in H_3BO_3 is electron deficient; thus, H_3BO_3 is a Lewis acid and reacts with water via the equation:



Problem 20. Semiconductors

1.



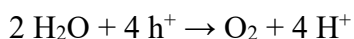
2. As the electron configuration of Si is $[\text{Ne}]3s^23p^2$, the hole-doping of Si requires elements with a smaller number of valence electrons than Si. Therefore, doping Si with B, which has the electron configuration $[\text{He}]2s^22p^1$, or Ga, which has the configuration $[\text{Ar}]3d^{10}4s^24p^1$, would result in the appearance of p-type properties.

3-1. The following reaction proceeds under an H_2 flow, resulting in the loss of oxide ions from TiO_2 :
 $\text{TiO}_2 + x \text{H}_2 \rightarrow \text{TiO}_{2-x} + x \text{H}_2\text{O}$
 Accordingly, TiO_2 is doped with electrons and the resulting TiO_{2-x} exhibits n-type semiconductor properties.

3-2.

$$1.23 \text{ V from } \Delta G = -2FE$$

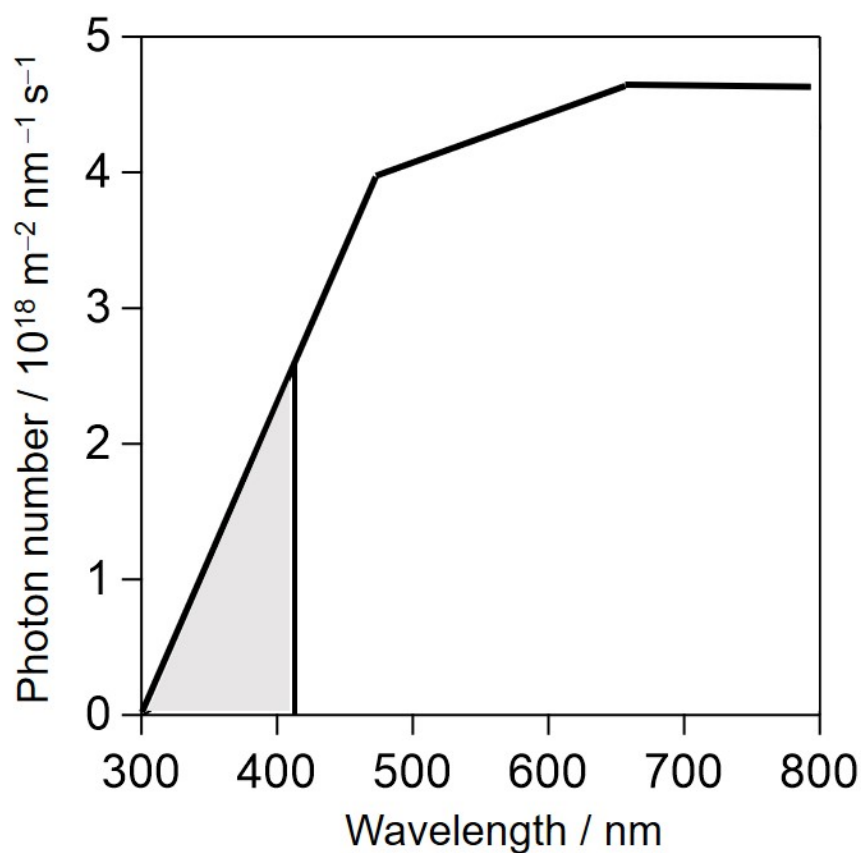
3-3.



3-4. From $E = hc/\lambda$

$$\lambda = 1240/3 = 413 \text{ nm}$$

The conversion efficiency is ca. 6.5% when the sunlight spectrum is approximated as shown in the figure below. $\Rightarrow$ (b)



3-5. $E = hc/\lambda = 1240/350 = 3.543 \text{ eV} = 5.675 \times 10^{-19} \text{ J}$

Photon number = (light intensity) / (energy per photon)

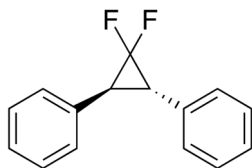
$$= 1 \text{ [J s}^{-1}] / (5.675 \times 10^{-19})$$

$$= 1.762 \times 10^{18}$$

$$\{(0.05 \times 10^{-6} [\text{mol s}^{-1}] \times 2 \times 6.02 \times 10^{23}) / (1.762 \times 10^{18})\} \times 100 = 3.42\%$$

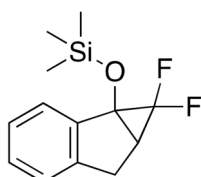
Problem 21. Carbenes and non-benzenoid aromatic compounds

1.



Similar to the Ruppert-Prakash reagent (Me_3SiCF_3), $\text{Me}_3\text{Si-CF}_2\text{Br}$ is converted into a difluorocarbene in the presence of bromide, which attacks the silicon atom. The NMR spectra indicate a symmetric structure for **A**.

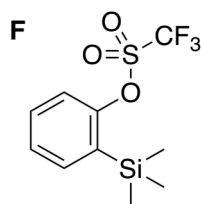
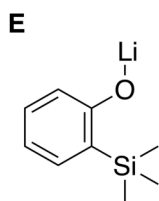
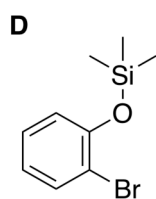
2.



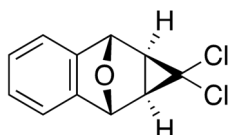
Me_3SiBr (TMSBr) is generated together with the fluorocarbene. TMSBr then transforms the ketone into a silylenol ether, before a subsequent cyclopropanation affords **B**.

3. The ring-opening of the cyclopropane followed by rearomatization furnishes **C**.

4.

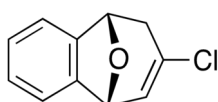


5.



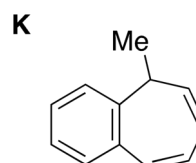
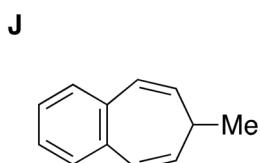
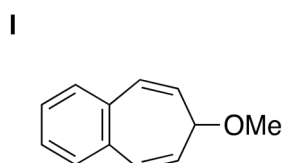
G is obtained after the addition of a dichlorocarbene to the double bond and the formation of the cyclopropane moiety. Albeit that the stereochemistry is important for the ring-opening, it is not requested here.

6.

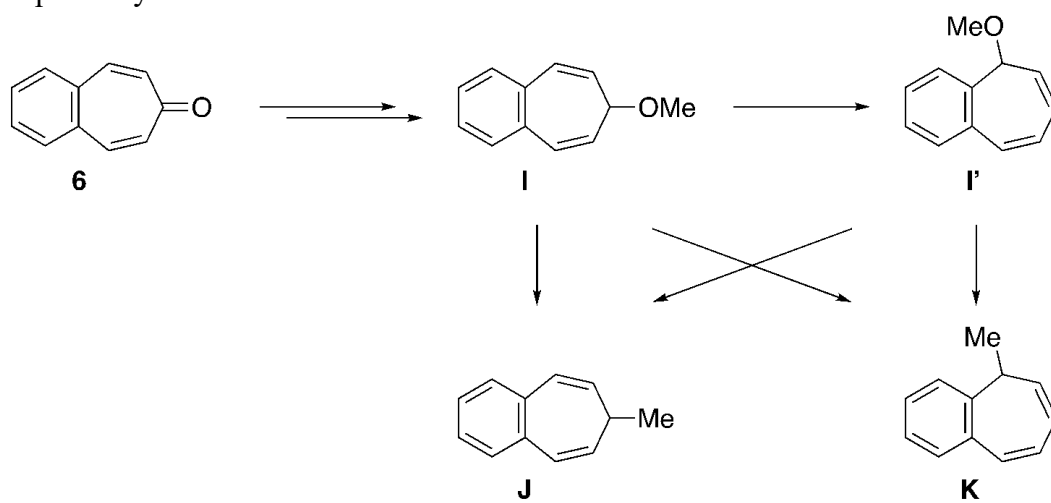


Based on the molecular formula, only one reduction has occurred.

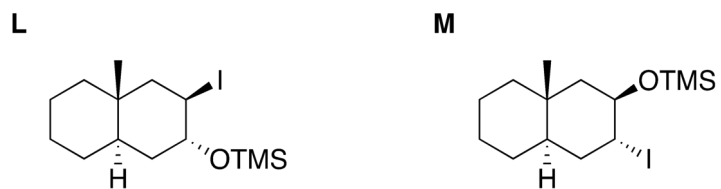
7.



The whole transformation is shown below, whereby the formation of the intermediary cycloheptatrienyl cation is crucial.



8.



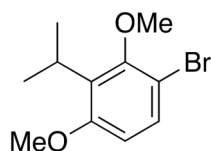
Diaxial ring opening dominates in six-membered ring systems.

Problem 22. Nazarov cyclization

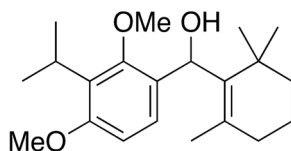
- a, d
Bicyclic structures that contain rigid five-membered rings rarely engage in a *trans* fusion.

2.

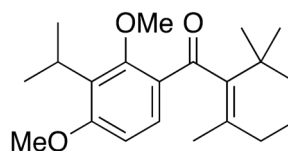
B



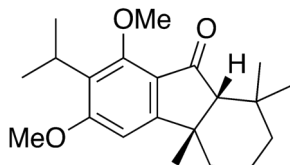
C



D

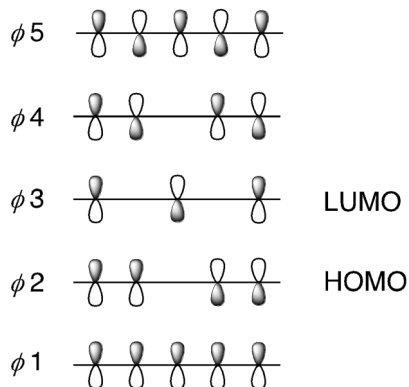


E



Compound **2** is brominated either at the *para*-position or at the *ortho*-position to give **B**. **C** is generated via a halogen-lithium exchange and a subsequent addition to the aldehyde. **D** is obtained from an oxidation of the OH group. **E** is formed via a Nazarov cyclization, followed by deprotonation and aromatization.

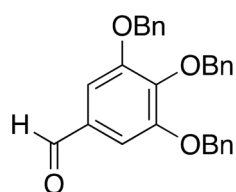
Optional problem



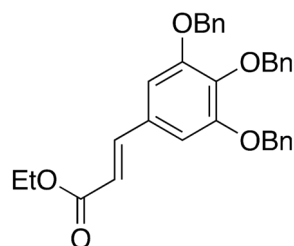
Problem 23. Tea party

1. $2R, 3R$
2. HCl, MeOH
3. PhCH₂Cl, NaH
- 4.

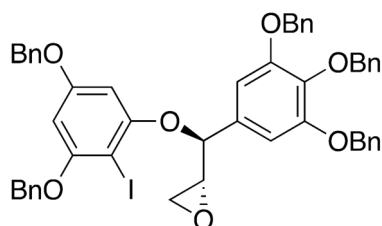
C



D

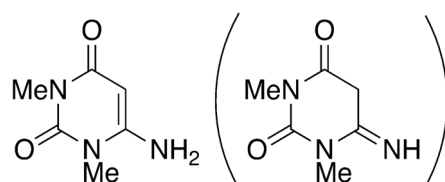


E

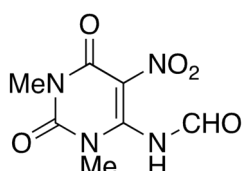


5.

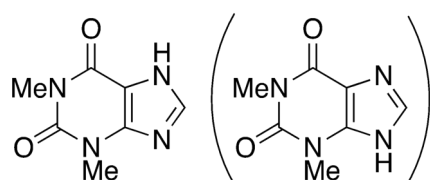
F



G



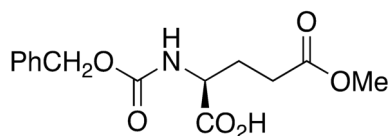
H



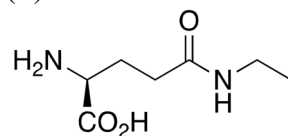
6. 1) NaH, 2) MeI

7.

J

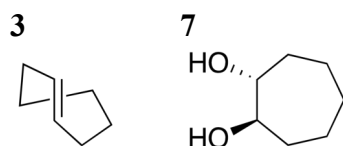


(+)-theanine

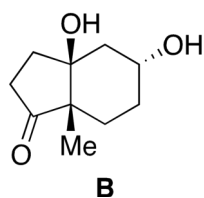


Problem 24. *E-Z* chemistry

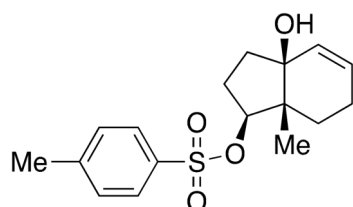
1.



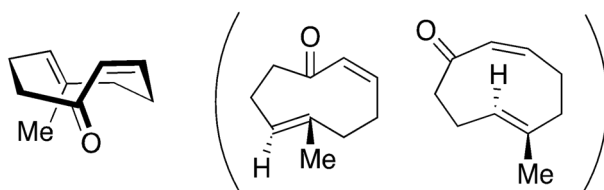
2.



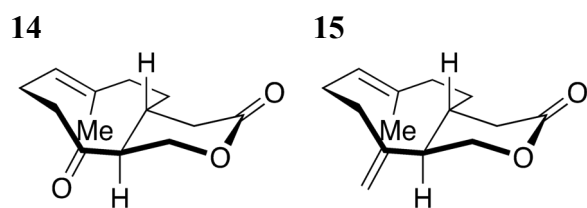
3.



4.

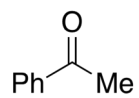


5.

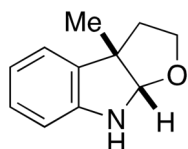


Problem 25. Fischer indole synthesis

1.

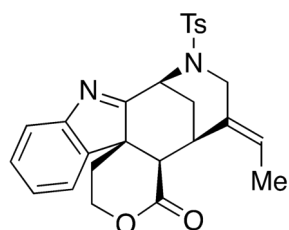


2.

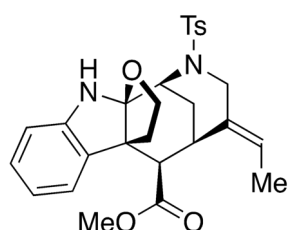


3.

14

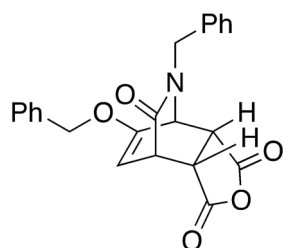


15

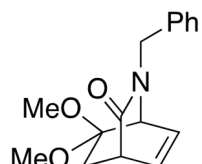


4.

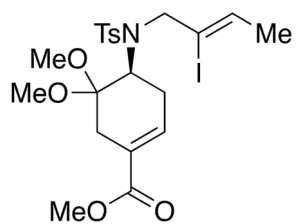
17



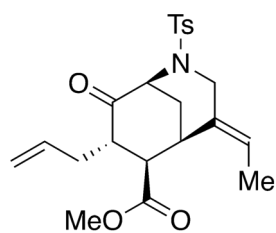
18



5.



6.

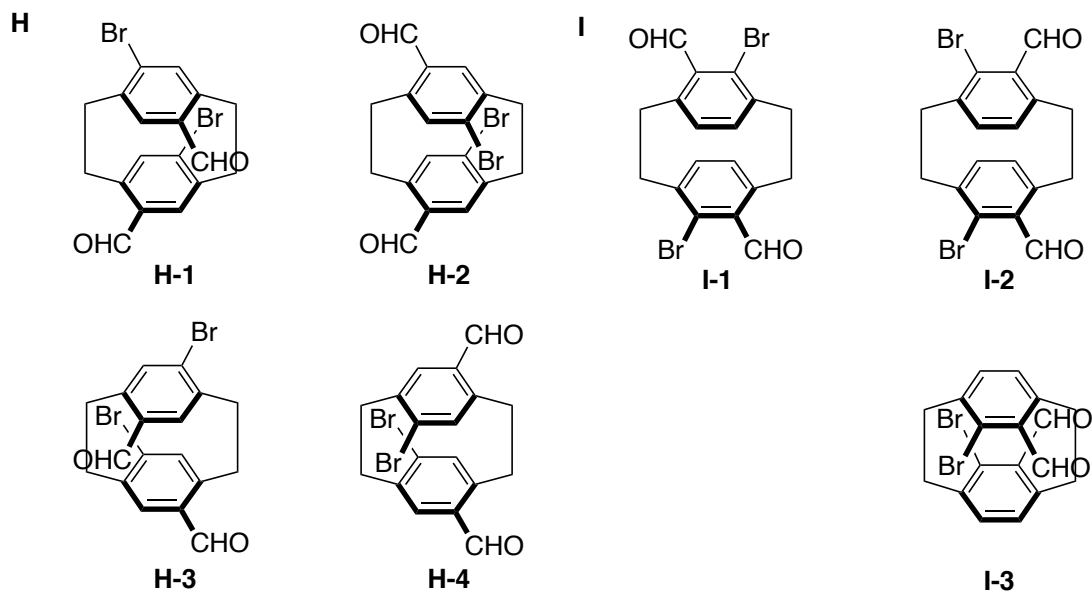


Problem 26. Planar chirality

1. **B, D, E**

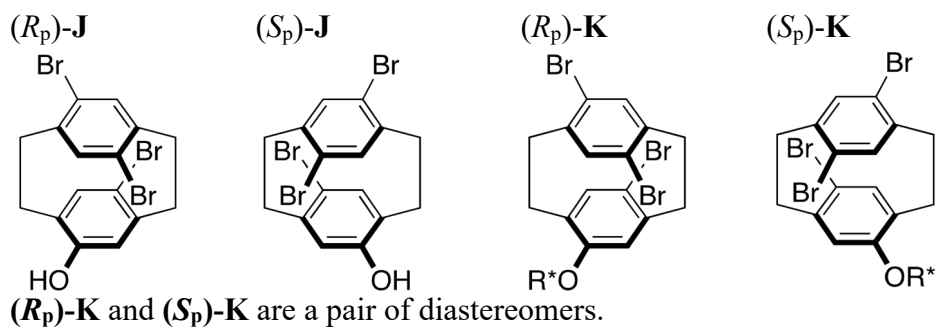
Only **C** is a *meso*-compound.

2.



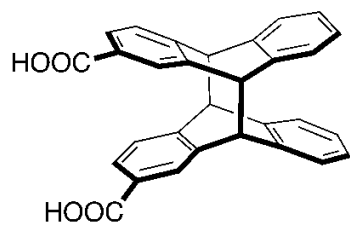
I-1 is a *meso*-compound. (**H-1**, **H-3**), (**H-2**, **H-4**), and (**I-2**, **I-3**) are pairs of enantiomers.

3.

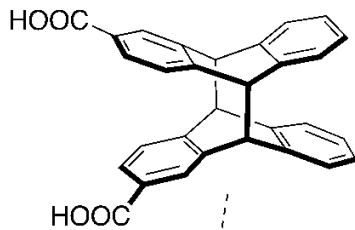


4.

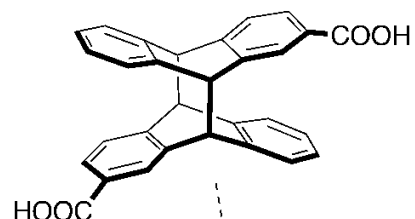
M-1



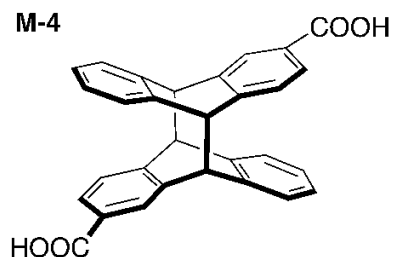
M-2



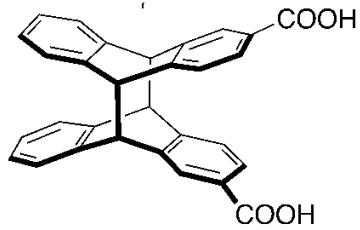
M-3



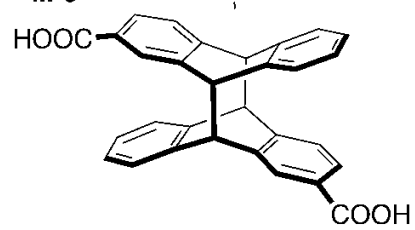
M-4



M-5



M-6



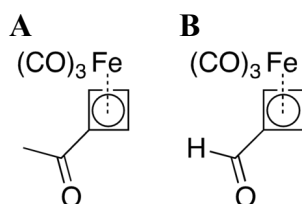
enantiomer

enantiomer

M-1 and **M-4** are *meso*-compounds.

Problem 27. Cyclobutadiene

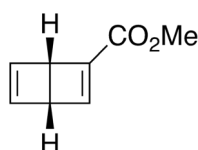
1.



A; Friedel-Crafts acylation. **B**; Vilsmeier formylation.

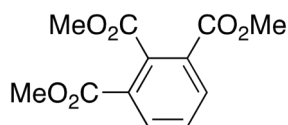
Both reactions furnish more electron-deficient products so that the subsequent second substitution is much slower than the first.

2.



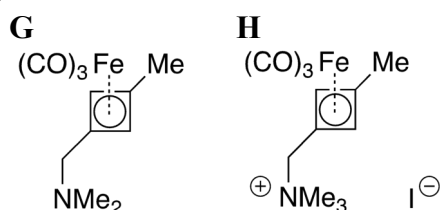
The reaction is a [2+2]-cycloaddition-like reaction to give a [2.2.0]-bicycle. The stereochemistry is not known exactly, as the reaction mechanism has not yet been elucidated unequivocally. So the stereochemistry is not required. In fact, the cis isomer is produced exclusively on account of the bicyclic ring strain.

3-1.

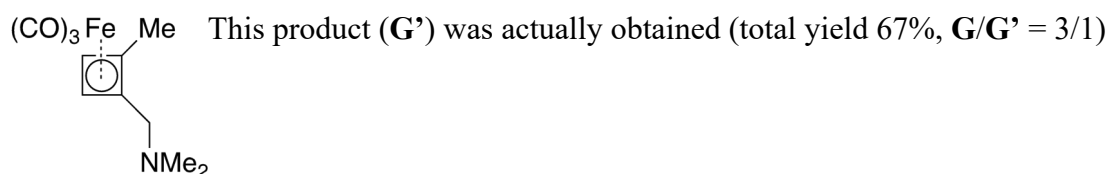


The target compound is obtained from a [4+2] cycloaddition reaction followed by decarboxylative aromatization.

3-2.

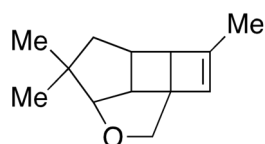


Compound **G** is formed via an electrophilic substitution reaction, wherein $\text{Me}_2\text{N-H}$ works as a leaving group.

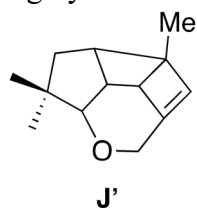


Compound **H** is an ammonium salt generated *in situ* that undergoes a substitution reaction with an alkoxide.

3-3.

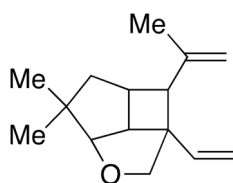


After demetallation by cerium ammonium nitrate, a [2+2]-cycloaddition-like reaction occurs to give product J. The steric effect of the methyl group and the ring strain can be expected to direct the reaction toward J. Another isomer (J') might be considered, albeit that its structure would be highly strained given the presence of a double bond at the bridgehead position.

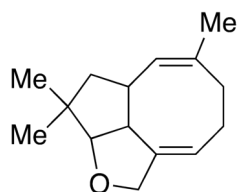


3-4.

K



L



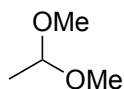
The ring-opening metathesis of **J** with ethylene gives **K**, which undergoes the Cope rearrangement to give **L**.

Problem 28. Onion-like complexes

- $0.120 \text{ nm} \times 6 + 0.143 \text{ nm} \times 12 + 0.140 \text{ nm} \times 12 = 4.116 \text{ nm} \sim 4.12 \text{ nm}$
 $4.12 \text{ nm} / \pi = 1.31 \text{ nm}$ (reported value: 1.32 nm)
- $0.120 \text{ nm} \times 9 + 0.143 \text{ nm} \times 18 + 0.140 \text{ nm} \times 18 = 6.174 \text{ nm} \sim 6.17 \text{ nm}$
 $6.17 \text{ nm} / \pi = 1.96 \text{ nm}$ (reported value: 1.98 nm)
- $(1.96 \text{ nm} - 1.31 \text{ nm}) / 2 = 0.325 \text{ nm} \sim 0.33 \text{ nm}$
- The half width of benzene (0.37 nm) is longer than the width of the interspace of the two rings (0.33 nm; cf. Q3). Therefore, the benzene ring cannot tilt, which means only configuration C is viable. This conclusion is also applicable to the interspace between benzene and alkyne moieties.
- $1.31 \text{ nm} - 0.65 \text{ nm} = 0.66 \text{ nm}$ (reported value: 0.71 nm)
- $\Delta G = -RT \ln K$
 $K = 8.14 \times 10^2$
 $K = (1-a)/ca^2$
 where a is the ratio of free [6]CPP (= free [11]CPP) and c the total concentration of [6]CPP.
 In this case, $c = 0.400 \text{ mmol L}^{-1}$ as two solutions are mixed in the same volume ratio.
 This affords $a = 0.794$ and consequently
 $[\text{free [6]CPP}] = ca = 3.18 \times 10^{-4} \text{ mol L}^{-1}$
- (a) and (d) are correct.
 b: The $[n]$ CPPs ($n = 9-12$) do not quantitatively form complexes because their peaks remain unchanged after the addition of the second equivalent of [13]CPP.
 c: As the complex precipitates from the solution, its peak must vanish.
 e: The peak attributed to [8]CPP disappears after the addition of the first equivalent of [13]CPP. The new peak should thus be ascribed exclusively to [13]CPP.

Problem 29. Hydrogen-bonded capsules

1.



2. (b)

3. (c)

The graph shows that two equivalents of DBU (0.5 mmol) lead to the complete dimerization of **D**. Accordingly, every molecule contains two deprotonated sites and each dimeric capsule of **D** should contain four deprotonated sites.

In the original report, this graph was obtained in the presence of pyrazine; this divergence can be ignored here.

4.

$$\frac{1300}{77} = \frac{[\text{pyrazine@host}][\text{free dioxane}]}{[\text{dioxane@host}][\text{free pyrazine}]} = \frac{75 [\text{pyrazine@host}]}{25 [\text{free pyrazine}]} = \frac{75}{25} \frac{[a]}{[1 - a]}$$

$a = 0.85$

Thus, 85% of pyrazine is encapsulated by **D**.

5. (a): (1)

The OH groups are acetylated, which leads to the retro-dimerization of the capsule and hence the release of benzene.

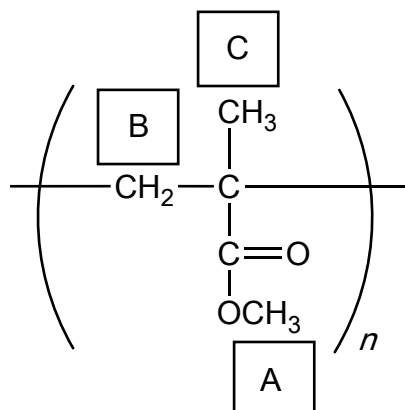
(b): (3)

Upon dilution with chloroform, chloroform is gradually encapsulated under concomitant release of benzene.

6. The reaction **B**→**C** affords a methylene-bridged capsule. Due to this covalent bridging, reversible association and dissociation is not possible anymore, and the guest molecule can no longer be released.

Problem 30. Synthesis and structural analysis of polymers

1.



2. (b)

3. (1) g A
- (2) d B
- (3) a D

4. C

$$5. \quad d[M_1]/d[M_2] = [M_1]/[M_2] \times (r_1[M_1] + [M_2]) / ([M_1] + r_2[M_2])$$

As the content of M_1 in the polymer is 50 mol%, $d[M_1]/d[M_2] = 1.0$, $r_1 = 0.40$, and $r_2 = 0.10$ can be substituted into the above equation:

$$1.0 = [M_1]/[M_2] \times (0.40[M_1] + [M_2]) / ([M_1] + 0.10[M_2])$$

$$[M_2] \times ([M_1] + 0.10[M_2]) = [M_1] \times (0.40[M_1] + [M_2])$$

$$0.10[M_2]^2 = 0.40[M_1]^2$$

$$([M_1]/[M_2])^2 = 0.10/0.40 = 0.25$$

$$[M_1]/[M_2] = 0.50$$

Therefore, the content of M_1 in the total monomer mixture ($[M_1]/([M_1] + [M_2])$) is 1/3.
33 mol%

6. Polymer obtained:

1 B

2 D

Site where the initiator reacts:

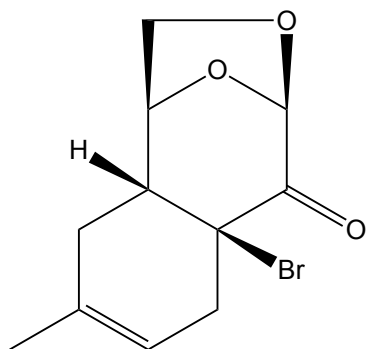
1 F

2 G

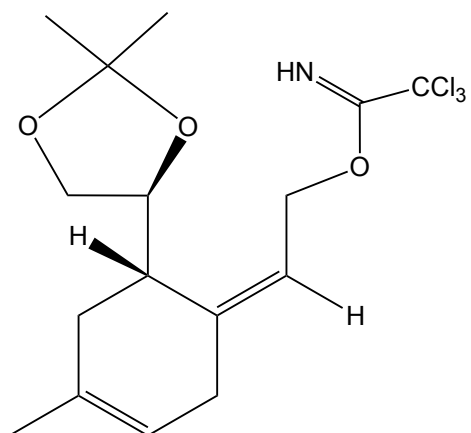
Problem 31. Total synthesis of tetrodotoxin

1.

2

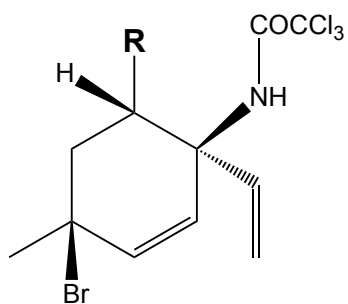


6

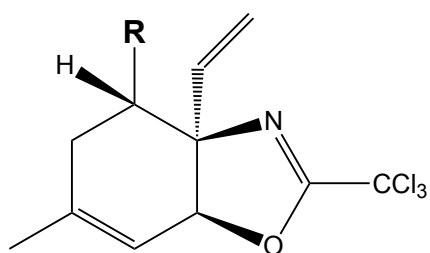


2.

9

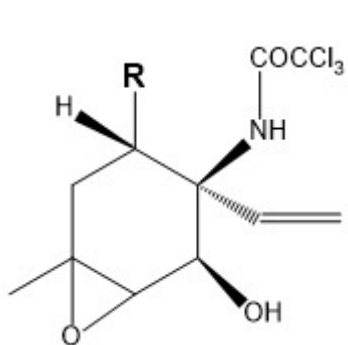


10

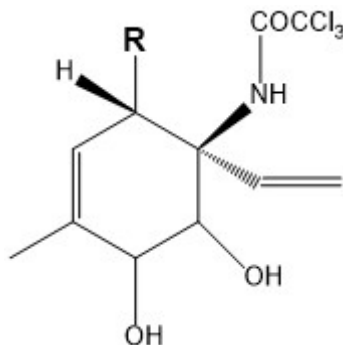


3.

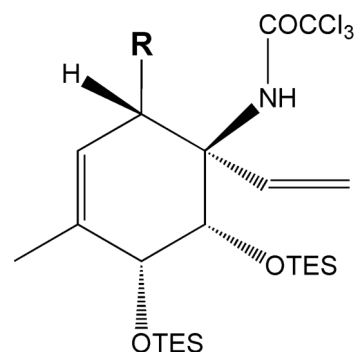
12



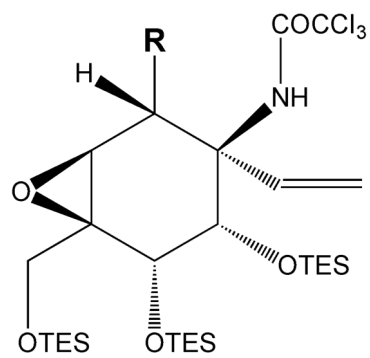
13



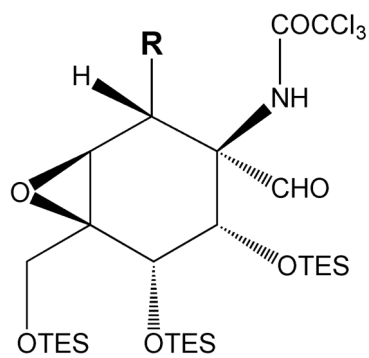
15



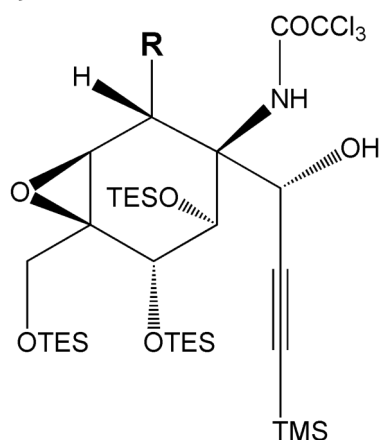
17



18

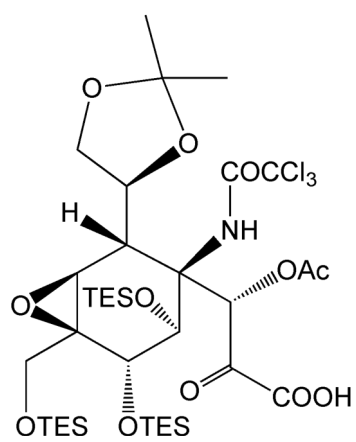


19

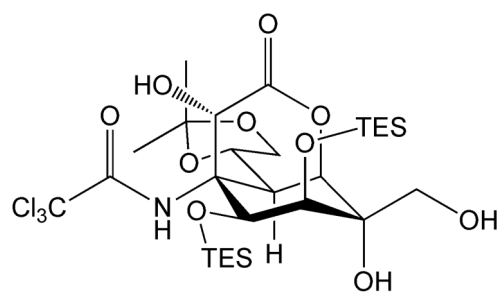


4.

21



23



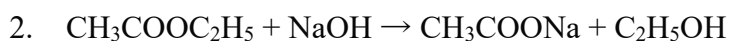
Appendix

Practical Tasks

Task 1. Analysis of the saponification rate using a pH meter

1.

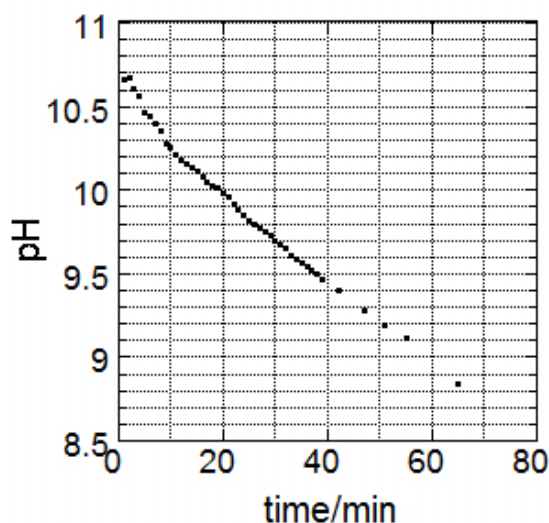
C_1 [mol L ⁻¹]	C_2 [mol L ⁻¹]
When 88.1 mg of ethyl acetate is used: $C_1 = \frac{88.1 \times 10^{-3} \text{ g} / 88.1 \text{ g mol}^{-1}}{0.100 \text{ L}}$ $= 0.0100 \text{ mol L}^{-1}$	When the concentration of aqueous solution of NaOH is 0.05005 mol L ⁻¹ : $C_2 = 0.05005 \times \frac{2}{100}$ $= 0.001001 \text{ mol L}^{-1}$



3.

Time (minutes)	Temperature (°C)	pH	Time (minutes)	Temperature (°C)	pH
5		10.46	35		9.56
10		10.26	40		9.45
15		10.11	47		9.28
20		9.81	51		9.19
25		9.82	55		9.11
30		9.70	65		8.84

4.



The slope is $-2.642 \times 10^{-2} \text{ min}^{-1}$.

$$-2.642 \times 10^{-2} \text{ min}^{-1} = -k'_1 / 2.303$$

Therefore, $k'_1 = 6.084 \times 10^{-2} \text{ min}^{-1}$

5. The concentration of ethyl acetate after mixing is $0.0100 \text{ mol L}^{-1} / 2 = 0.00500 \text{ mol L}^{-1}$

$$k'_1 = k_2 [\text{CH}_3\text{COOC}_2\text{H}_5]$$

$$k_2 = 6.084 \times 10^{-2} \text{ min}^{-1} / 0.00500 \text{ mol L}^{-1} = 13.61 \text{ mol}^{-1} \text{ L min}^{-1}$$

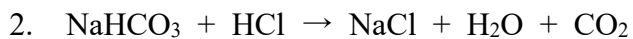
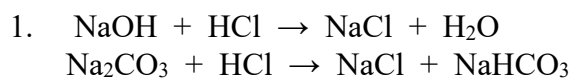
6.

$$-\ln \frac{[\text{OH}^-]}{[\text{OH}^-]_0} = k_1' t$$

$$-\ln \frac{1}{2} = 6.084 \times 10^{-2} \text{min}^{-1} \times t_{1/2}$$

$$t_{1/2} = 0.6931 / 6.084 \times 10^{-2} \text{min}^{-1} = 11.39 \text{ min}$$

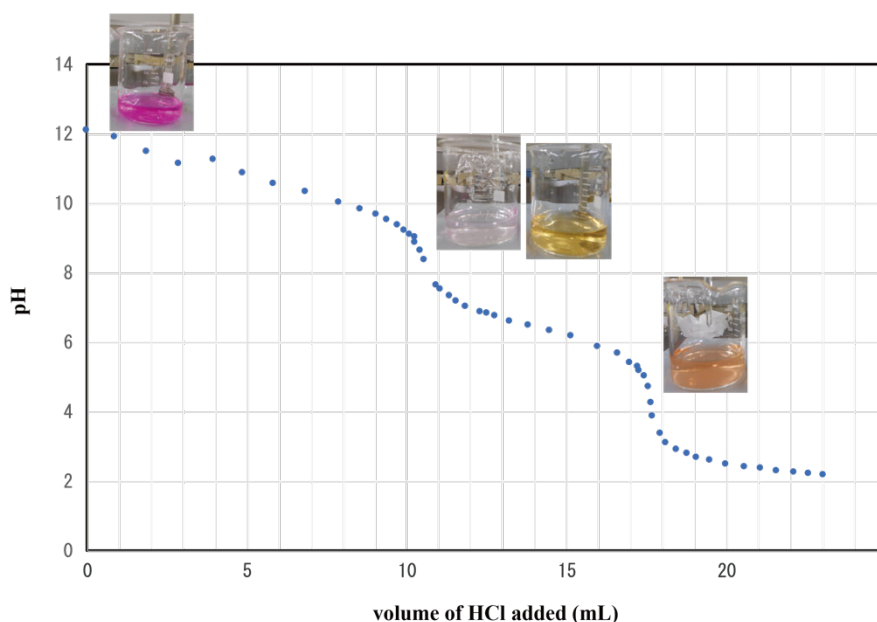
Task 2. Simultaneous acid–base titration



$$3. \quad \text{NaOH [g]} : 0.0040 \times (V_a - V_b) / \frac{20}{1000} \text{ [g]}$$

$$\text{Na}_2\text{CO}_3 \text{ [g]} : 0.0053 \times 2 \times (V_b) / \frac{20}{1000} \text{ [g]}$$

4. The horizontal axis is the amount of the standard solution added, while the vertical axis is the pH value of the unknown alkali solution. The following figure shows the actual measurement data (unknown alkali solution: 30.00 mL) where the unknown alkali solution was prepared from 1.0 L distilled water containing 0.5 g of NaOH and 2.5 g of Na₂CO₃.



Task 3. Synthesis and analysis of a cobalt(III) oxalate complex

1-4 The concentration of the potassium permanganate aqueous solution c is given by

$$c = w \times 2 / 134 / 5 / v \times 1000$$

where w is the weight of sodium oxalate used in step B-1 and v is the volume of the aqueous potassium permanganate solution (accepted) used in the titration in step B-1.



3. The weight% of the oxalate ion is given by

$$c \times x / 1000 \times 5 / 2 \times 88 / y \times 100$$

where c is the concentration of the potassium permanganate aqueous solution determined above, x is the volume of the potassium permanganate aqueous solution (accepted) used in the titration in step B-2 and y is the weight of cobalt oxalate complex analyzed in step B-2.

From the table below, if the weight% of oxalate ion is more than 50.8% ($= (53.4 + 48.3) / 2$), the product can be estimated to be a tris complex. Thus, cobalt ion to oxalate ligand composition ratio is 1:3.

Compound composition	Molecular weight	Weight% of oxalate ion
tris complex: $\text{K}_3[\text{Co}(\text{C}_2\text{O}_4)_3] \cdot 3\text{H}_2\text{O}$	494.3	53.4 %
bis complex: $\text{K}[\text{Co}(\text{C}_2\text{O}_4)_2(\text{H}_2\text{O})_2] \cdot 3\text{H}_2\text{O}$	364.1	48.3 %
mono complex: $[\text{Co}(\text{C}_2\text{O}_4)\text{Cl}(\text{H}_2\text{O})_3] \cdot 3\text{H}_2\text{O}$	290.5	30.3 %

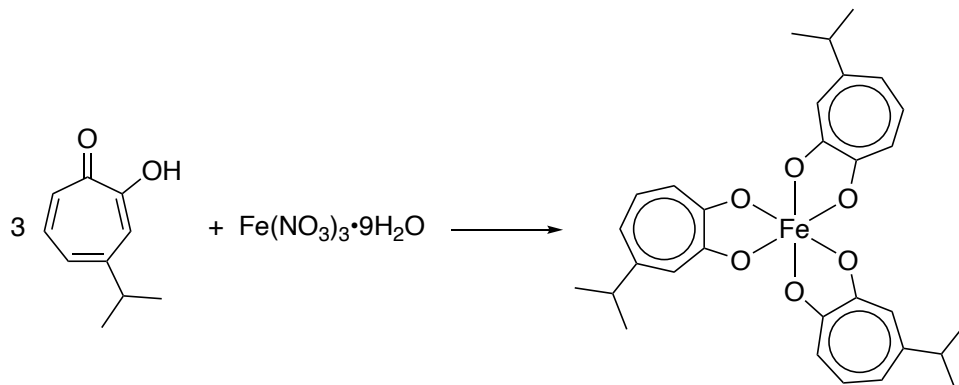
4. The molecular weight of cobalt(II) chloride hexahydrate is 238 g/mol. If it is estimated that a tris complex was formed, the yield is given by

$$z / 494.3 \times 238 \times 100$$

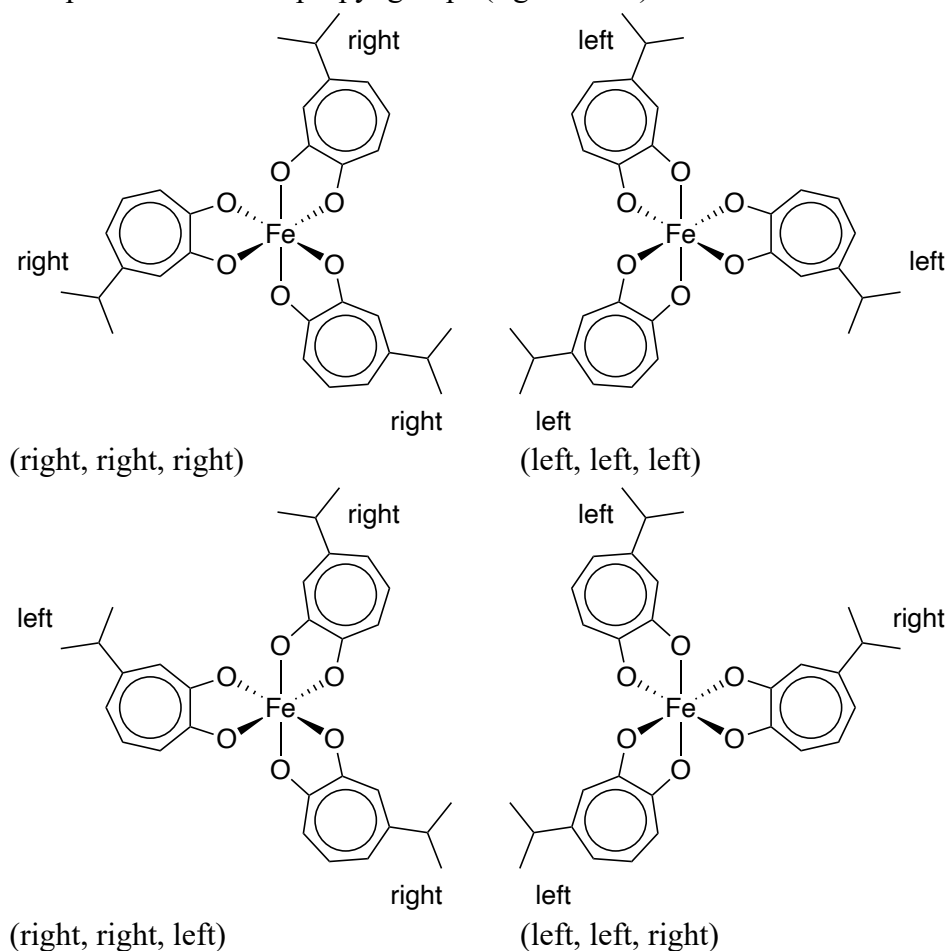
where z is the weight of the crystals of the complex obtained in step A.

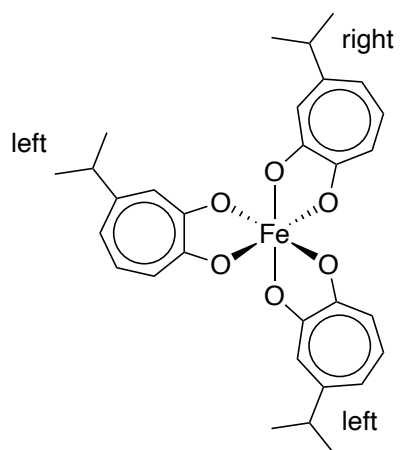
Task 4. Hinokitine: synthesis of a deep-red-colored natural product

- Hinokitine is a 3:1 complex of hinokitiol and iron(III) ion with the molecular formula (MF) $C_{30}H_{33}FeO_6$ and a molecular weight (MW) of $545.43 \text{ g mol}^{-1}$. The theoretical yield of hinokitine can be calculated from the amounts of the reactants hinokitiol (MF = $C_{10}H_{12}O_2$ and MW = 164.20) and iron(III) nitrate nonahydrate (MF = $FeH_{18}N_3O_{18}$ and MW = 403.99) used in the synthesis.

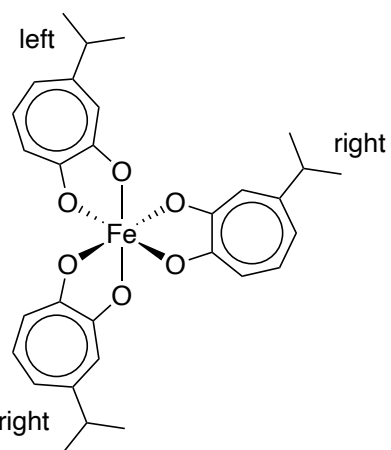


- Nitric acid (HNO_3)
- There are 8 isomers in total, including enantiomers (Δ and Λ) of hinokitine, depending on the position of the isopropyl groups (right or left)

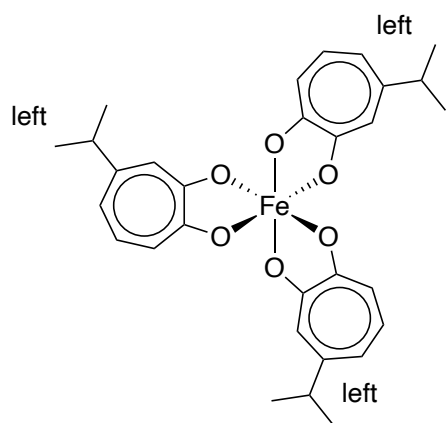




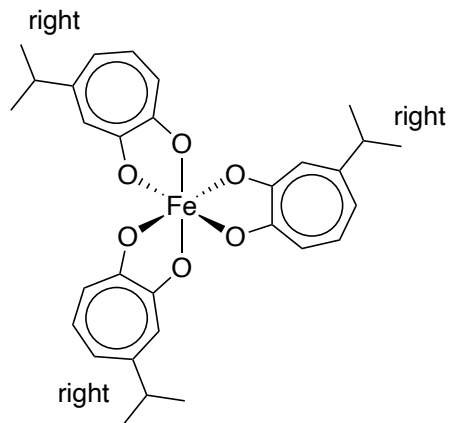
(right, left, left)



(left, right, right)



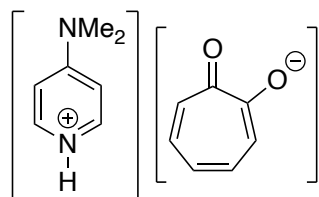
(left, left, left)



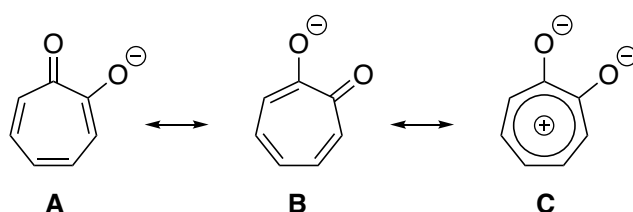
(right, right, right)

Task 5. Functionalization of a seven-membered ring: synthesis of tropolone tosylate

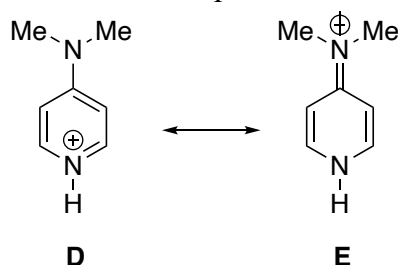
1.



4-Dimethylaminopyridine (DMAP) acts as a Brønsted base in this reaction. A tropolonate salt, 4-dimethylaminopyridinium tropolonate, is formed by proton transfer from the hydroxy group of tropolone to the nitrogen atom of the pyridine ring of DMAP. Tropolonate has an aromatic nature originating from the contribution of the canonical form with a tropylium ion structure (C).

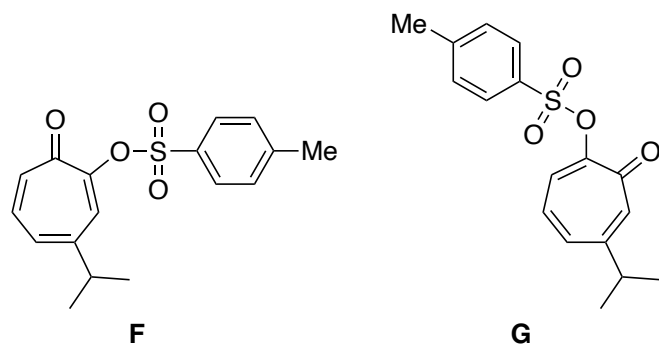


DMAP is more basic than pyridine due to the electron-donating effect of the dimethylamino group at the 4-position. The dimethylamino group can stabilize the positive charge on the protonated DMAP with the possible resonance structure (E).

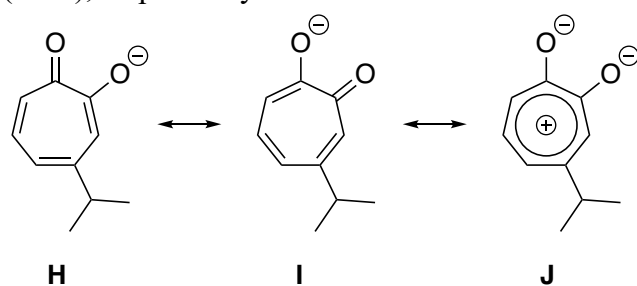


- After the tosylation, DMAP is transformed into DMAP hydrochloride, [(DMAP)H][Cl], which is soluble in water. The typical procedure for the recovery of DMAP is as follows. An appropriate organic solvent and water are added to the reaction mixture. While the organic layer mainly contains tropolone tosylate, the aqueous layer contains the DMAP hydrochloride. The aqueous layer is basified with an aqueous solution of sodium hydroxide (NaOH) followed by extraction into an appropriate organic solvent. The organic layer is dried over anhydrous sodium sulfate (Na₂SO₄) and evaporated under vacuum to afford solid DMAP. Sufficiently pure DMAP can be obtained using a further purification technique, such as crystallization from an appropriate organic solvent or chromatography on silica gel using an appropriate organic solvent as the eluent.

3.

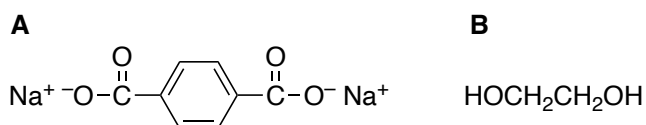


There are two tosylation products of hinokitiol (**F** and **G**), which are isomers. Hinokitiol is deprotonated by DMAP in a fashion similar to tropolone, affording the isopropyl-substituted tropolonate with three possible resonance forms (**H**, **I**, and **J**, which are analogous to **A**, **B**, and **C**). The products **F** and **G** are formally obtained from the reaction of **H** and **I** with tosyl chloride (TsCl), respectively.



Task 6. Hydrolysis of polyethylene terephthalate: A small experiment for us, but a giant leap toward a more sustainable society

1.



2. The theoretical weight of A can be calculated using the following equation:

$$\begin{aligned} \text{Theoretical weight of A} &= 1.00 \text{ [g]} * \frac{\text{molecular weight of disodium terephthalate}}{\text{formula weight of the repeating unit of PET}} \\ &= 1.00 \text{ [g]} * \frac{210.09}{192.17} = 1.09 \text{ [g]} \end{aligned}$$

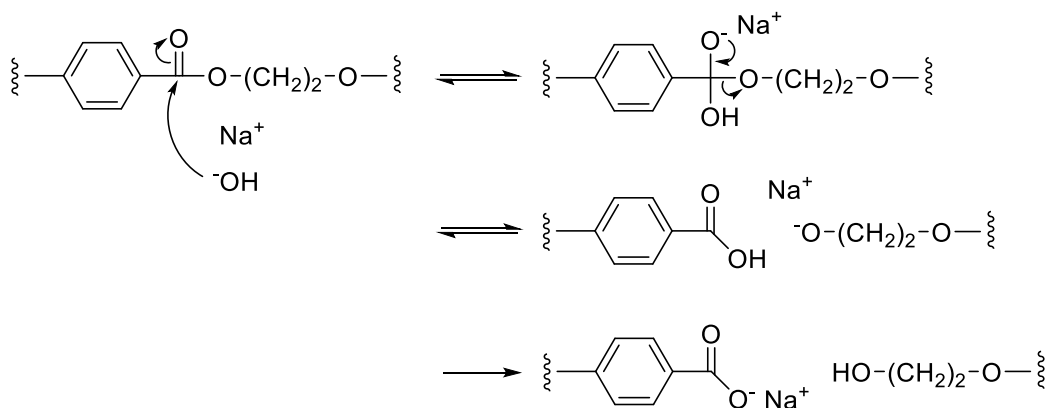
The yield of A based on the amount of PET used can be calculated using the following equation:

$$\text{Theoretical yield of A [\%]} = \frac{\text{weight of A obtained}}{\text{theoretical weight of A}} * 100$$

3. The yield of A based on the amount of PET reacted can be calculated using the following equation:

$$\text{Theoretical yield of A [\%]} = \frac{\text{weight of A obtained}}{\text{theoretical weight of A} * \frac{\text{weight of PET reacted}}{\text{weight of PET used}}} * 100$$

4.



5. As shown above, the first and the second steps are reversible. On the other hand, the final step is not reversible, because the neutralization reaction between the acidic carboxyl group and the highly basic alkoxide gives a carboxylate, which is not sufficiently basic to regenerate the alkoxide by deprotonation of the hydroxyl group. The irreversible nature of the final step makes the overall system irreversible. In addition, the hydroxyl group, which is much less nucleophilic than the alkoxide, is not able to attack the carbonyl group to induce the backward condensation reaction. Another reason is the poor solubility of the resulting disodium terephthalate, which precipitates from solution, which shifts the equilibrium toward the formation of the products.

6. Under the same conditions, the hydrolysis conducted in this experiment is much more efficient than the hydrolysis of the polyamide. The carbonyl carbon atom of the amide group is less electrophilic than that of the ester group on account of the greater extent of delocalization of the lone pair on the nitrogen atom compared to the lone pair on the oxygen. Consequently, the carbonyl carbon atom of the amide group is more resistant to the nucleophilic addition of the hydroxide ion than the ester group. Moreover, even if the nucleophilic addition of the hydroxide ion (OH^-) took place, the resulting intermediate would preferentially release OH^- rather than the amide anion (NHR^-), which is much more basic than OH^- and thus more difficult to produce. In other words, the intermediate preferentially dissociates to recover the amide bond.

Task 7. Separation of blue and red components from a green mixture

1. 4-(phenylazo)phenol
Recrystallization is effective or available when (1) the desired compound is major in the mixture and when (2) the desired compound is more easily crystallized than the impurity. The recrystallization of the 'mixture' for the column chromatography (1:1 mixture) to separate 4-(phenylazo)phenol will be unsuccessful.
2. Guaiazulene from the first colored fraction (blue) and 4-(phenylazo)phenol from the second colored fraction (orange).
3. Recrystallization is conducted by the difference of solubility at different temperatures. Although the solubility of the substance would decrease at lower temperature, it does not drop to zero. Because of some solubility of the substance at lower temperature, the yield of recrystallization cannot be quantitative.
4. Guaiazulene eluted first, and 4-(phenylazo)phenol eluted later. This means that 4-(phenylazo)phenol exhibits higher interaction (affinity) with the stationary phase, silica gel. The hydroxy group interacts with the OH group on the surface of the silica gel via hydrogen bonding. Nitrogen atoms in 4-(phenylazo)phenol may also contribute the interaction, although the basicity of sp^2 nitrogen is low, and strong interaction is not expected from the azo group. It should be noted the azobenzene itself is a neutral compound, and exhibits low affinity with silica gel.

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